

BINNING THE DATA

①

If N is large, one first "bins" the data otherwise the computational work to compute jackknife averages is too large.

It scales like N^2

Definitions = $\begin{cases} N & \text{number of data} \\ n & \text{number of bins} \\ N/n = m & \text{bin length} \end{cases}$

n should be chosen so that N/n is an integer.

Example $N=9$ $n=3$ $m=3$

$$\begin{array}{l} f(x_1) \\ f(x_2) \\ f(x_3) \end{array} \left. \vphantom{\begin{array}{l} f(x_1) \\ f(x_2) \\ f(x_3) \end{array}} \right\} \text{bin 1} \quad F_1 = \frac{1}{m} (f(x_1) + f(x_2) + f(x_3))$$

$(\frac{1}{3})$

$$\begin{array}{l} f(x_4) \\ f(x_5) \\ f(x_6) \end{array} \left. \vphantom{\begin{array}{l} f(x_4) \\ f(x_5) \\ f(x_6) \end{array}} \right\} \text{bin 2} \quad F_2 = \frac{1}{m} (f(x_4) + f(x_5) + f(x_6))$$

$$\begin{array}{l} f(x_7) \\ f(x_8) \\ f(x_9) \end{array} \left. \vphantom{\begin{array}{l} f(x_7) \\ f(x_8) \\ f(x_9) \end{array}} \right\} \text{bin 3} \quad F_3 = \frac{1}{m} (f(x_7) + f(x_8) + f(x_9))$$

In general we define

$$F_j = \frac{1}{m} \sum_{k=m(j-1)+1}^{mj} f(x_k)$$

$$\left. \begin{array}{c} f(x_1) \\ \vdots \\ f(x_m) \end{array} \right\} \rightarrow F_1 \quad \left. \begin{array}{c} f(x_{m+1}) \\ \vdots \\ f(x_{2m}) \end{array} \right\} \rightarrow F_2 \quad \text{and so on}$$

The JK method is applied to F_j .

We define

$$\bar{F}_i = \frac{1}{n-1} \sum_{\substack{j=1 \\ j \neq i}}^n F_j \quad J_i = J(\bar{F}_i)$$

and use the JK formula with

$$n \text{ (number of bins)} \leftrightarrow N \text{ (number of iterations)}$$

It is a good idea to take $n \approx 100$
