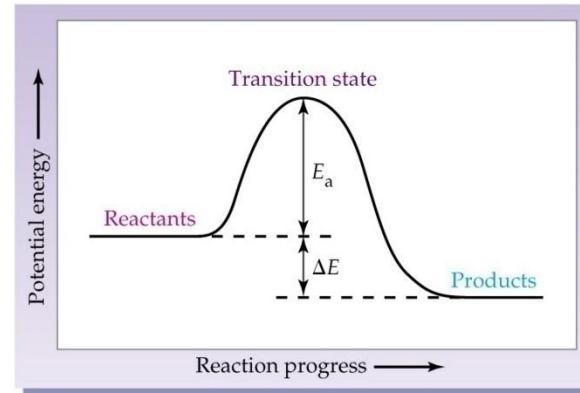


# Thermodynamics & kinetics

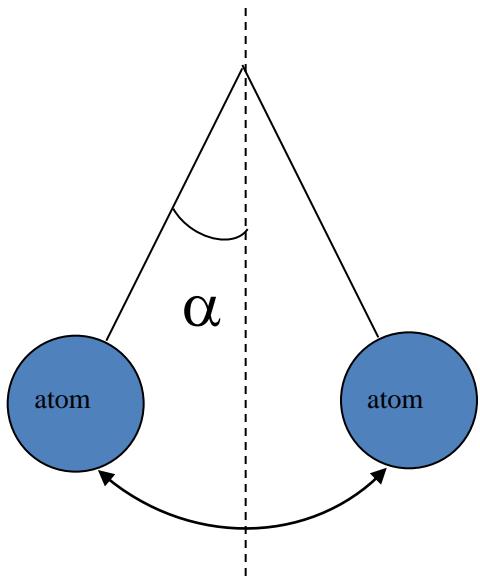


(a)

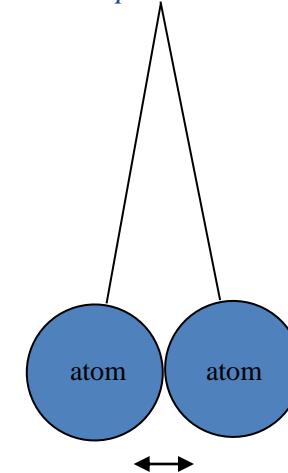


(b)

1

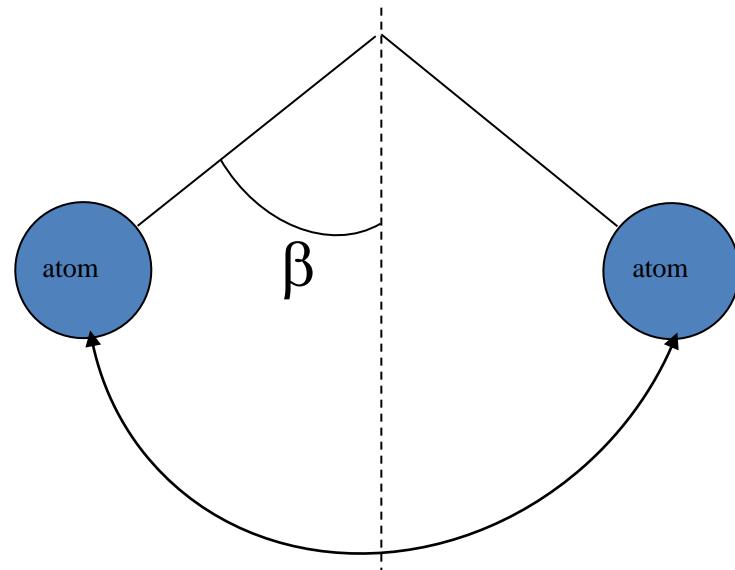


$$E_k = \frac{1}{2} m V^2 < E_a$$



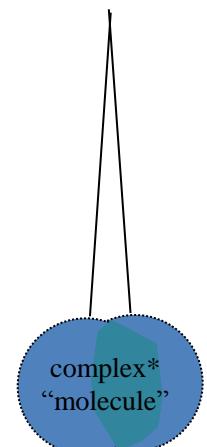
*not reacted*

2

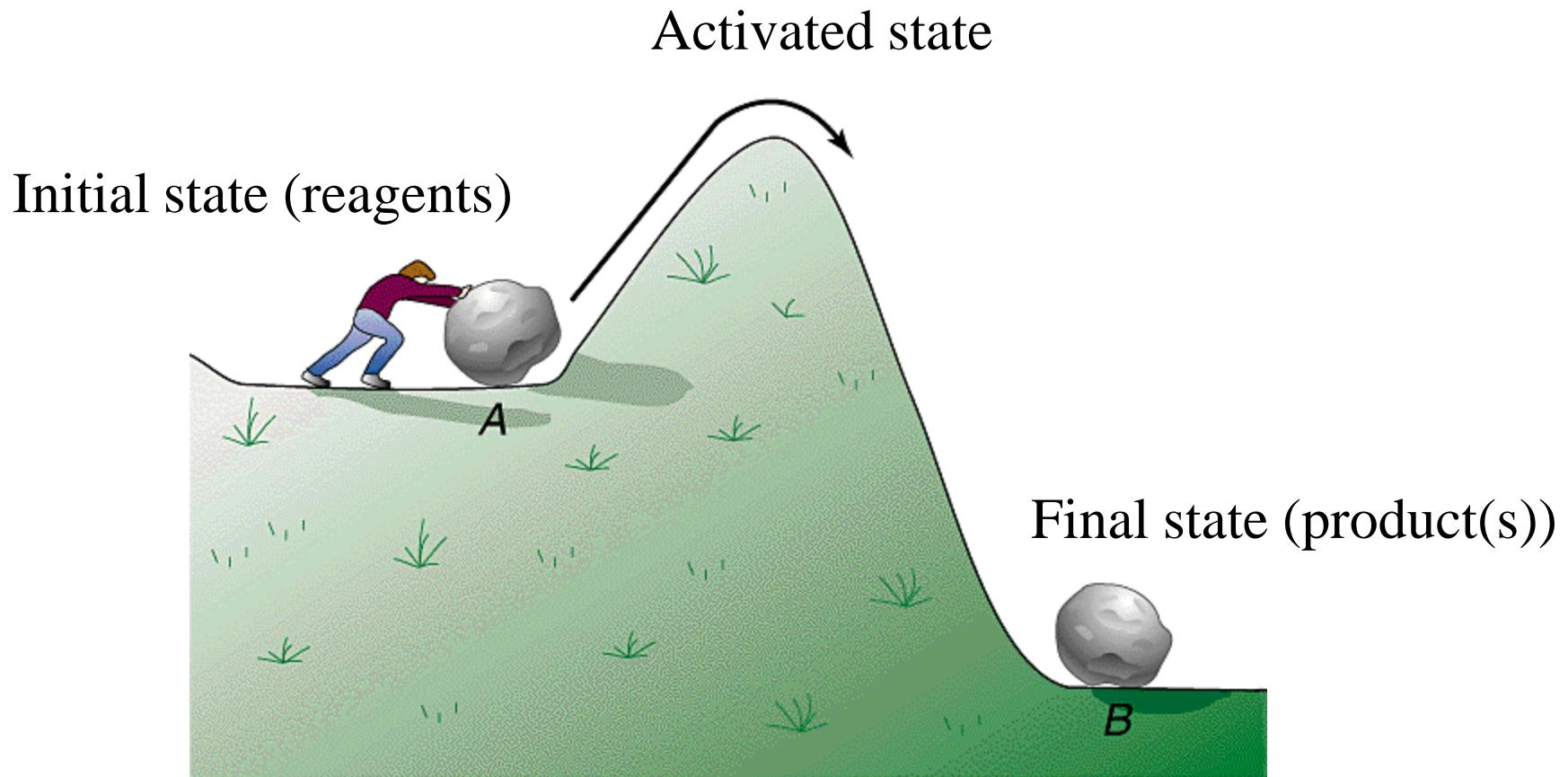


$$\beta > \alpha$$

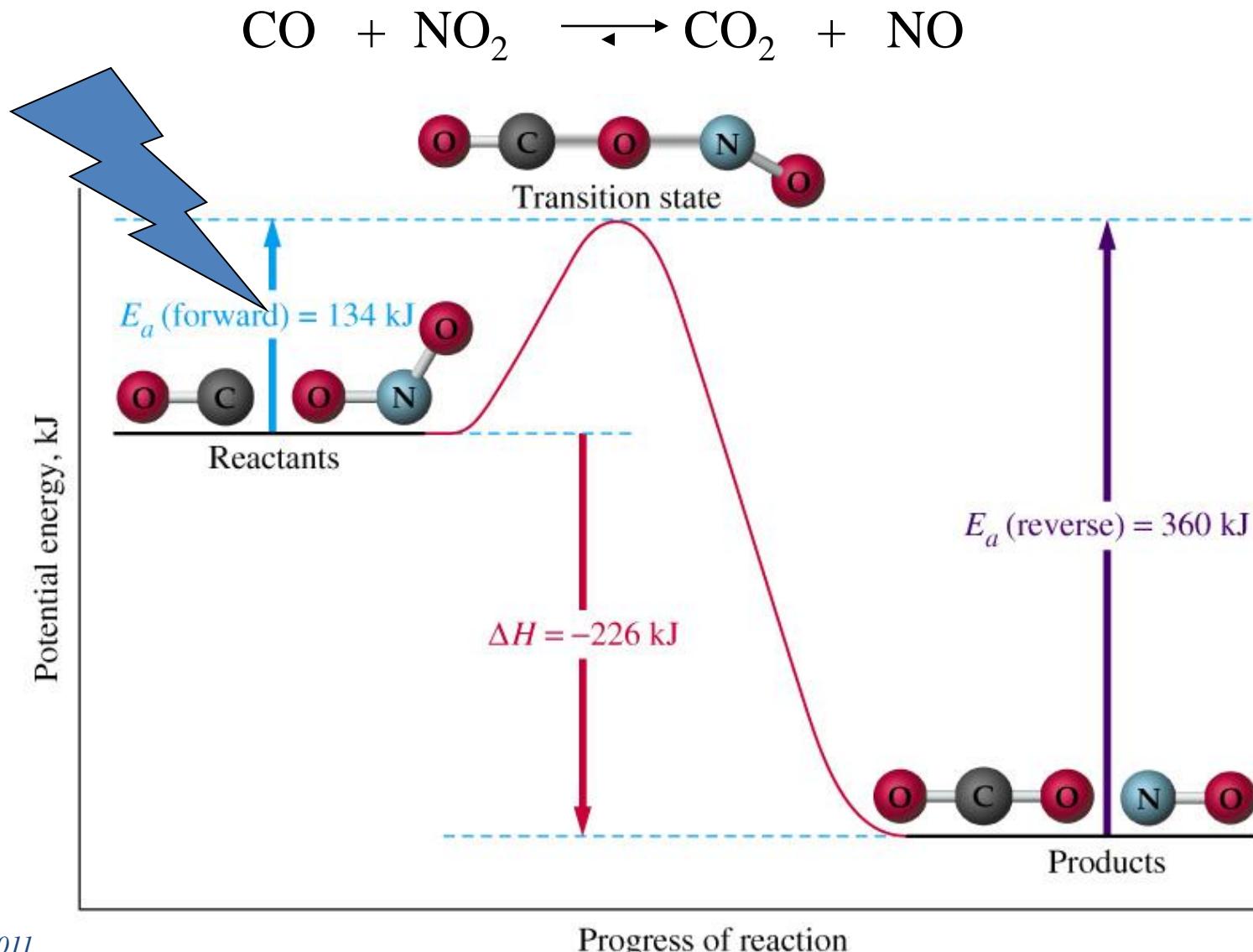
$$E_k = \frac{1}{2} m V^2 > E_a$$



*reacted*



$E_k$  necessary to generate “useful collisions”  $\geq E_a$



# Kinetics

Provides info on:

- 1) Reaction mechanism
- 2) Reaction time course (time needed to reach equilibrium)

How do we make a kinetic measurement?

What do we measure?

In gaseous phase → pp and volumes,  $f(\text{time})$

In liquid phase (solution) → concentrations,  $f(\text{time})$

$$\underbrace{n^{\circ} \text{moles} \times V^{-1} \times \text{time}^{-1}}_{[\text{conc}] \times \text{time}^{-1}} \rightarrow \text{Rate -Velocity!!}$$

## Thermodynamic parameters

$$\Delta G = \Delta H - T \Delta S$$

$$\Delta G = - 57 \text{ Kcal/Mol}$$

$$\Delta H = - 68 \text{ Kcal/mol}$$

$$T = 298 \text{ K}$$

$$\Delta S = - 0.039 \text{ Kcal/mol}$$

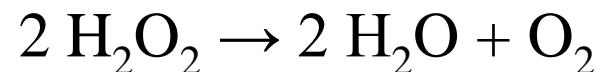
do they give any info  
on rate...!?

No !

can we predict a rate  
based on  $\Delta G$ ?

No !

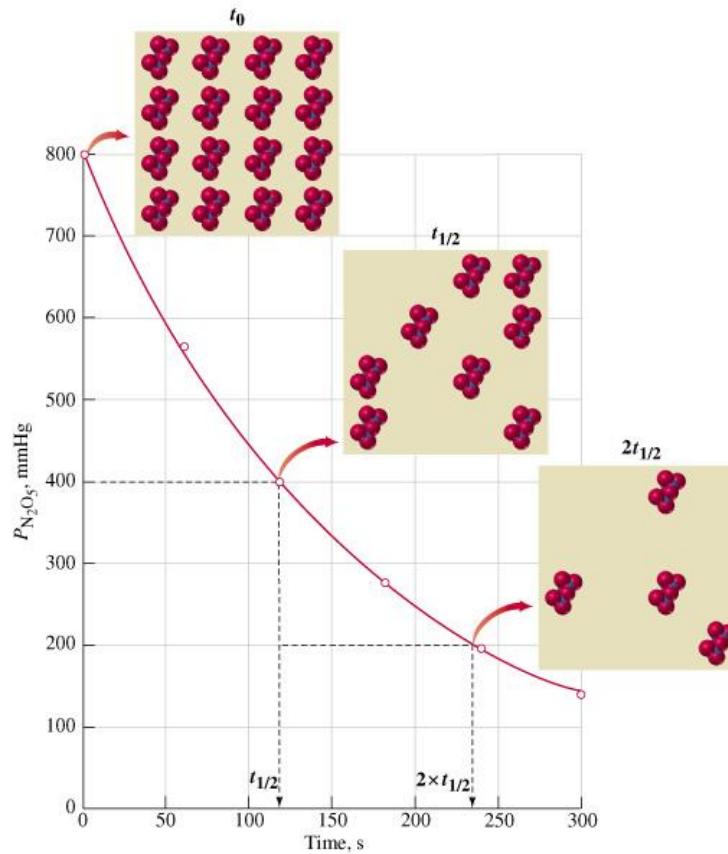
Es.



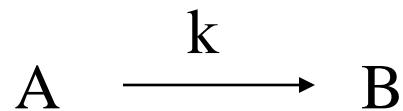
To measure kinetics  
we need to know:

- reagents degradation  $f(t)$
- products formation  $f(t)$
- thus, rate at given time  $t$

# Example

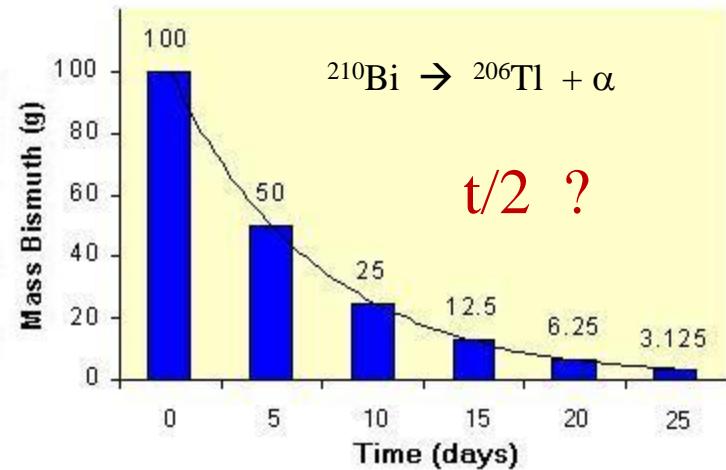
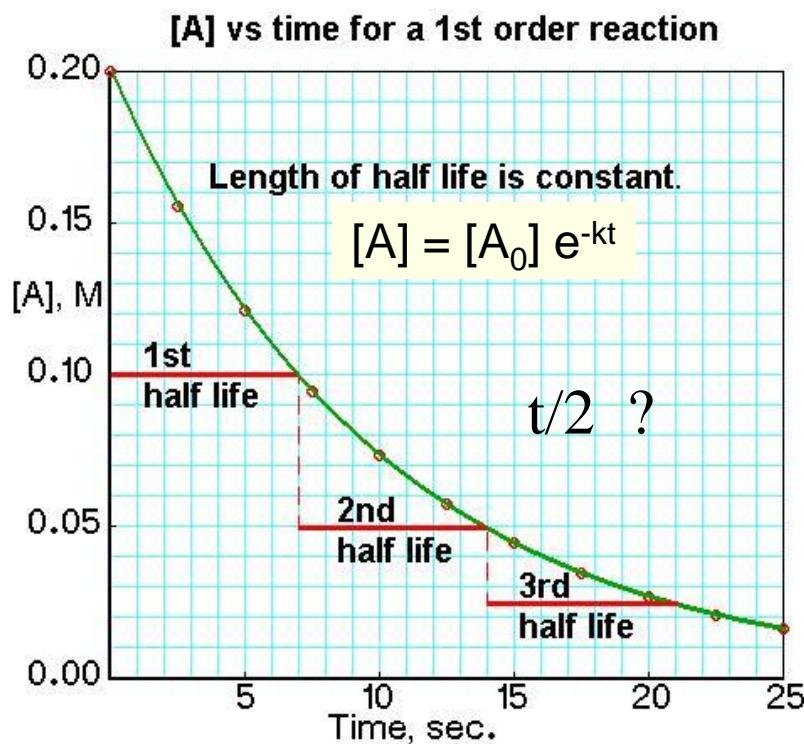


$$A = A_0 e^{-kt}$$

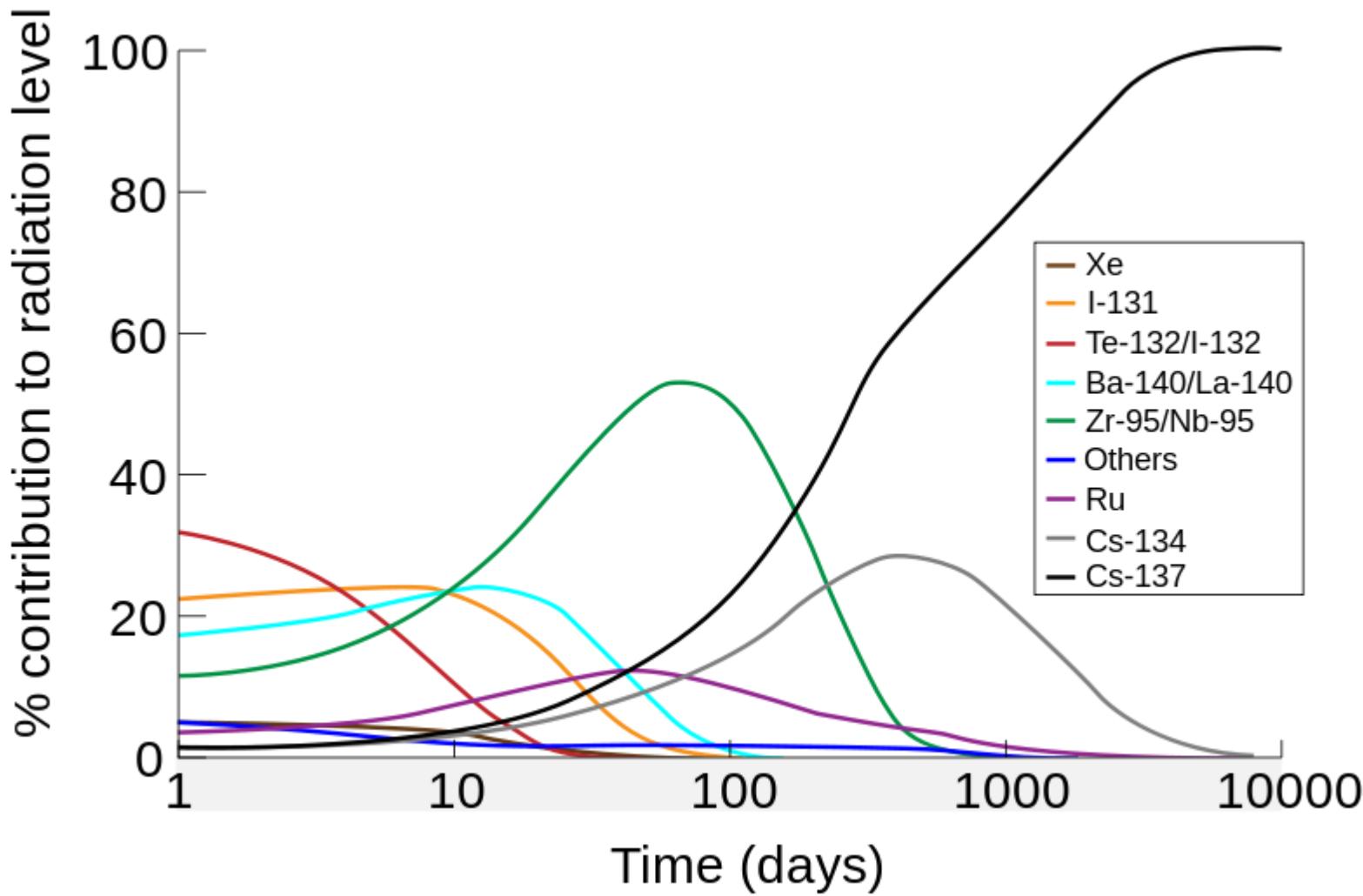


Iodine-131  $t/2 = 8$  days  
 Iodine-125  $t/2 = 59$  days

$$V = k [A]^1$$



$t/2$	% residuo
1	50
2	25
3	12.5
4	6.25
5	3.125



Zr = zirconium

Nb = niobium

$$[A] = [A_o] e^{-kt}$$

for  $t = t/2$

$$A = A_o/2$$

$$\ln A / \ln A_o = -kt$$

$$\ln A_o - \ln 2 - \ln A_o = -kt/2$$

~~$$\ln A_o - \ln 2 - \ln A_o = -kt/2$$~~

$$\ln 2 = k \times t/2$$

$$k = \ln 2 / t/2 = 0.693 / t/2$$

$$t/2 = \text{constant}$$

$$t/2 = 0.693 / k$$

## **Parameters affecting the rate of a reaction :**

- 1) Reagents concentration**
- 2) Temperature**
- 3) Catalysts/enzymes**
- 4) Physico-chemical properties of reagents & products**

## Velocity & concentration

It is intuitive 2 atoms/molecules needs to meet to react !

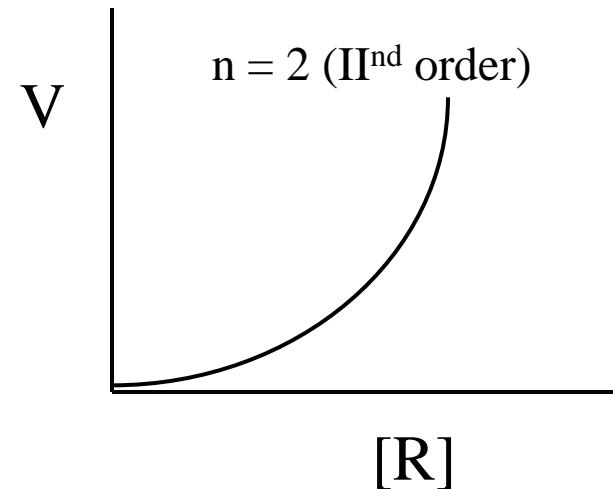
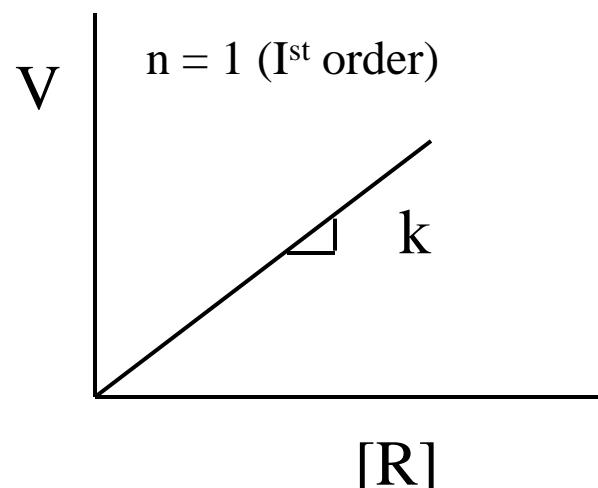
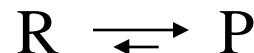
Consequently the reaction rate

$$V \uparrow, f [R]$$

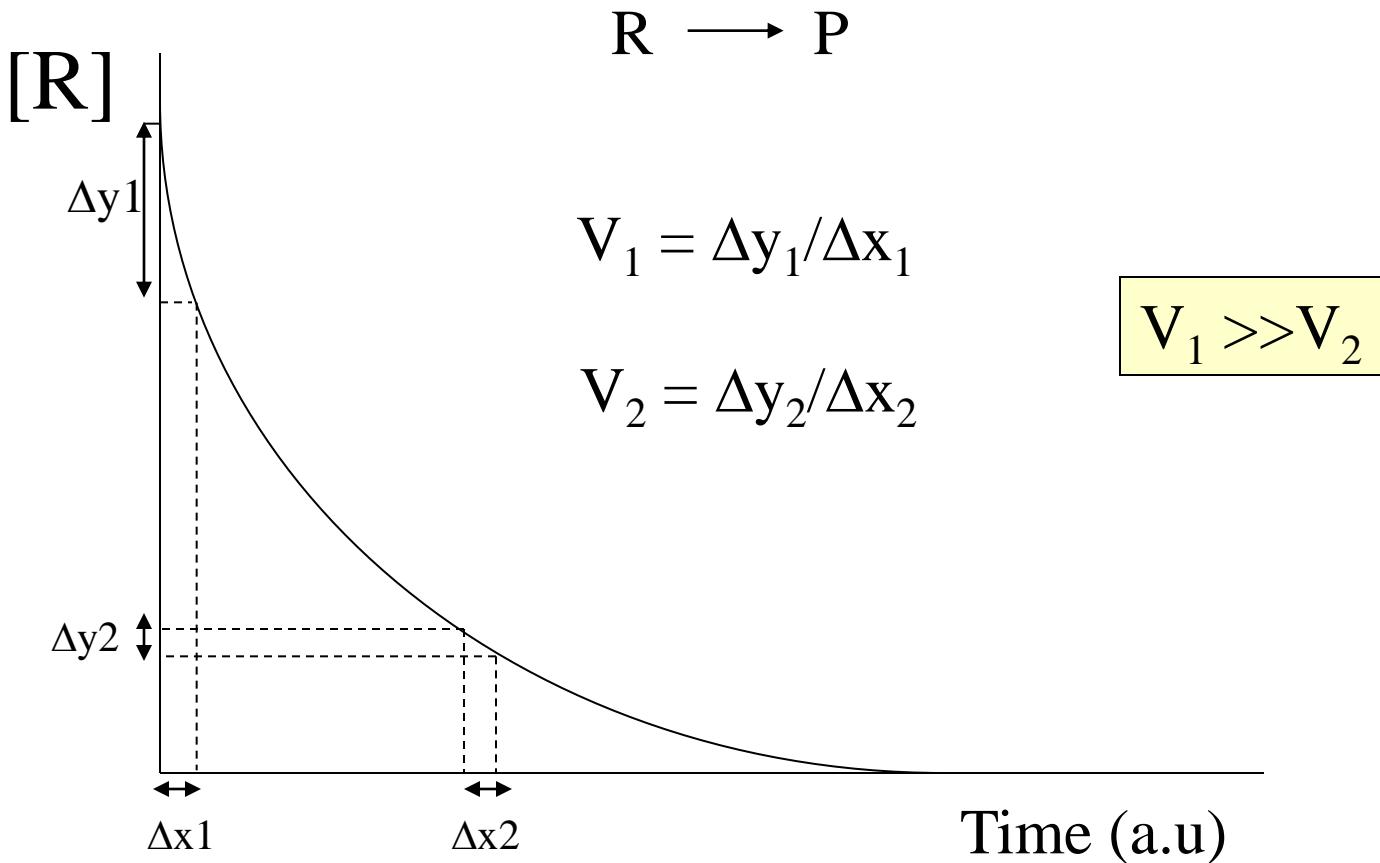
### Kinetic equation

$$V = k [R]^n$$

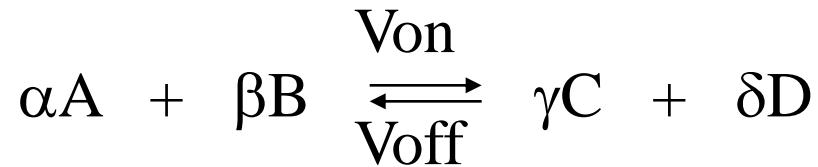
( $n$  = reaction order)



If the rate depends upon the reagents concentration  
Then V has to decrease as a function of time!



## The kinetic of a reaction

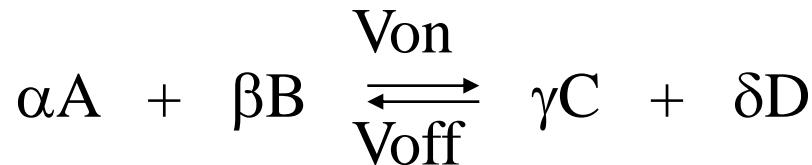


$$V_{\text{on}} = k [A]^n * [B]^m \quad (n, m = \text{on-reaction orders, partial})$$
$$(n + m = \text{on-reaction order, global})$$

$$V_{\text{off}} = k [C]^{n'} * [D]^{m'} \quad (n', m' = \text{off-reaction orders, partial})$$
$$(n' + m' = \text{off-reaction orders, global})$$

**Reaction orders & stoichiometric coefficients**  
**Do not make confusion !!! They are different parameters**  
**Any coincidence is just fortuitous!!**

## **K<sub>eq</sub>** and the reaction rates



$$V_{\text{on}} = k_{\text{on}} [A] [B]$$

$$V_{\text{off}} = k_{\text{off}} [C] [D]$$

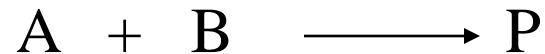
At equilibrium

$$V_{\text{on}} = V_{\text{off}}$$

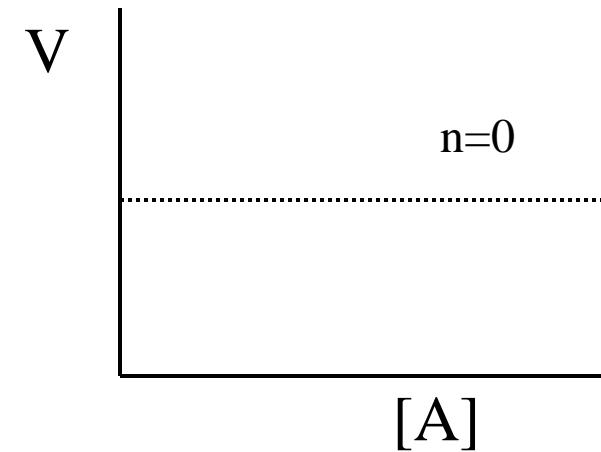
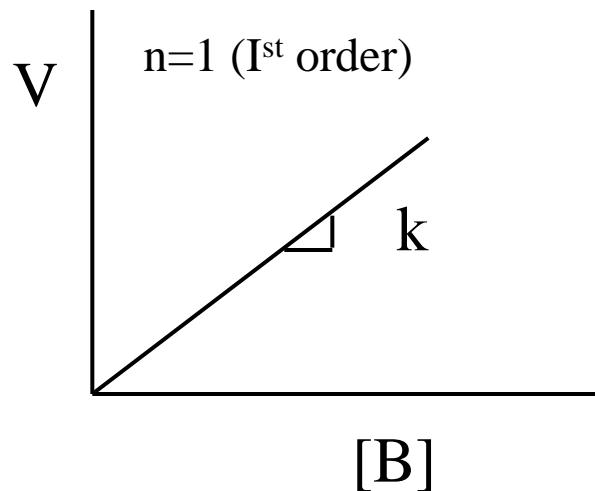
$$k_{\text{on}} [A] [B] = k_{\text{off}} [C] [D]$$

$$k_{\text{on}}/k_{\text{off}} = [C][D]/[A][B] = K_{\text{eq}}$$

# This is interesting!!



$$V = k [A]^0 [B]^n \quad (n = 1, \text{ most commonly!})$$



# Enzymatic catalysis

## Michaelis-Menten model (1913)

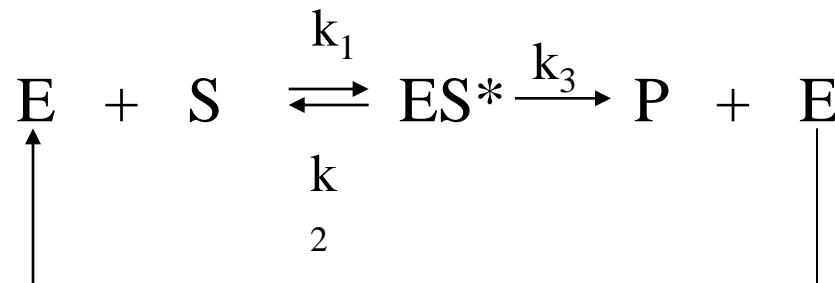


$$V = k [A]^0 [B]^1$$

$$V = k [S]^0 [E]^1 \text{ (at steady state)}$$

---

Model :

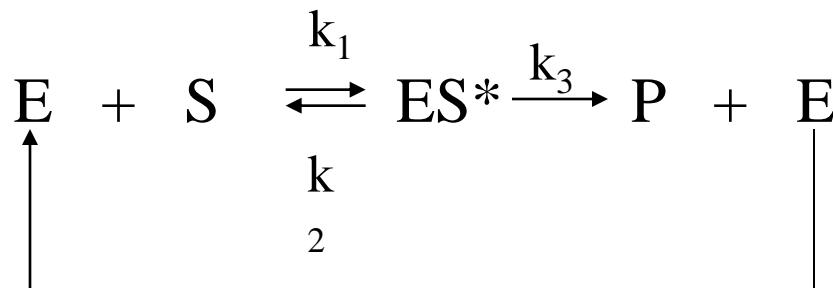


## Michaelis Menten constant $K_M$



$$V = k [S]^0 [E]^1$$

$$\begin{aligned} V_1 &= k_1 [E][S] \\ V_2 &= k_2 [ES] \\ V_3 &= k_3 [ES] \end{aligned}$$



when  $t = t_{\text{steady state (st)}}$

$$V_1 = V_2 + V_3$$

$$k_1 [E][S] = (k_2 [ES] + k_3 [ES])$$

$$k_1 [E][S] = (k_2 + k_3) [ES]$$

$$\frac{(k_2 + k_3)}{k_1} = \frac{[E][S]}{[ES]} = K_M$$

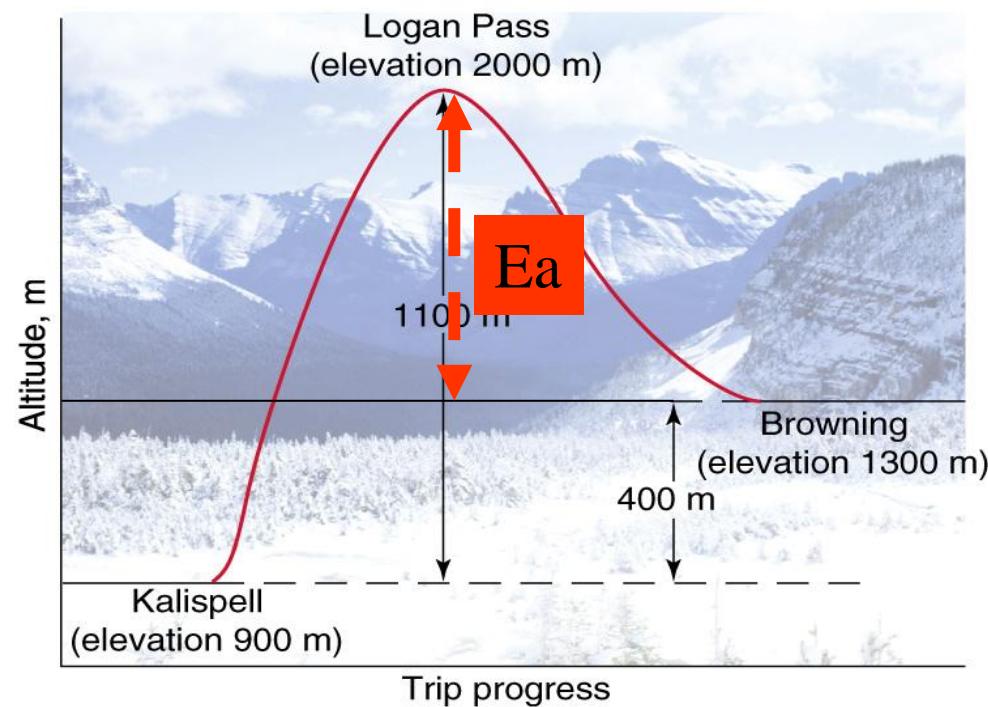
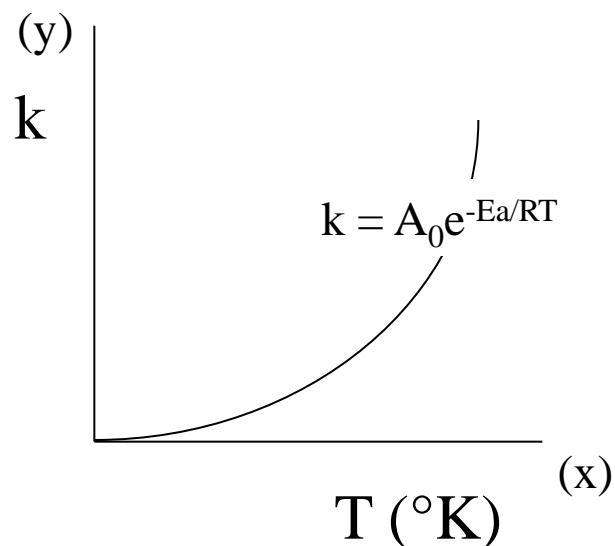
# The rate of a reaction and T (*Arrhenius*)

*Useful collision*  $\approx$  Ea      se T  $\uparrow$  E<sub>K</sub>  $\uparrow$  & V  $\uparrow$

## *Useful collisions*↑ with V↑

$V \propto$  fraction ( $f$ ) of molecules with  $E_K \geq Ea$   
 $f \propto (T); f \propto (1/Ea)$

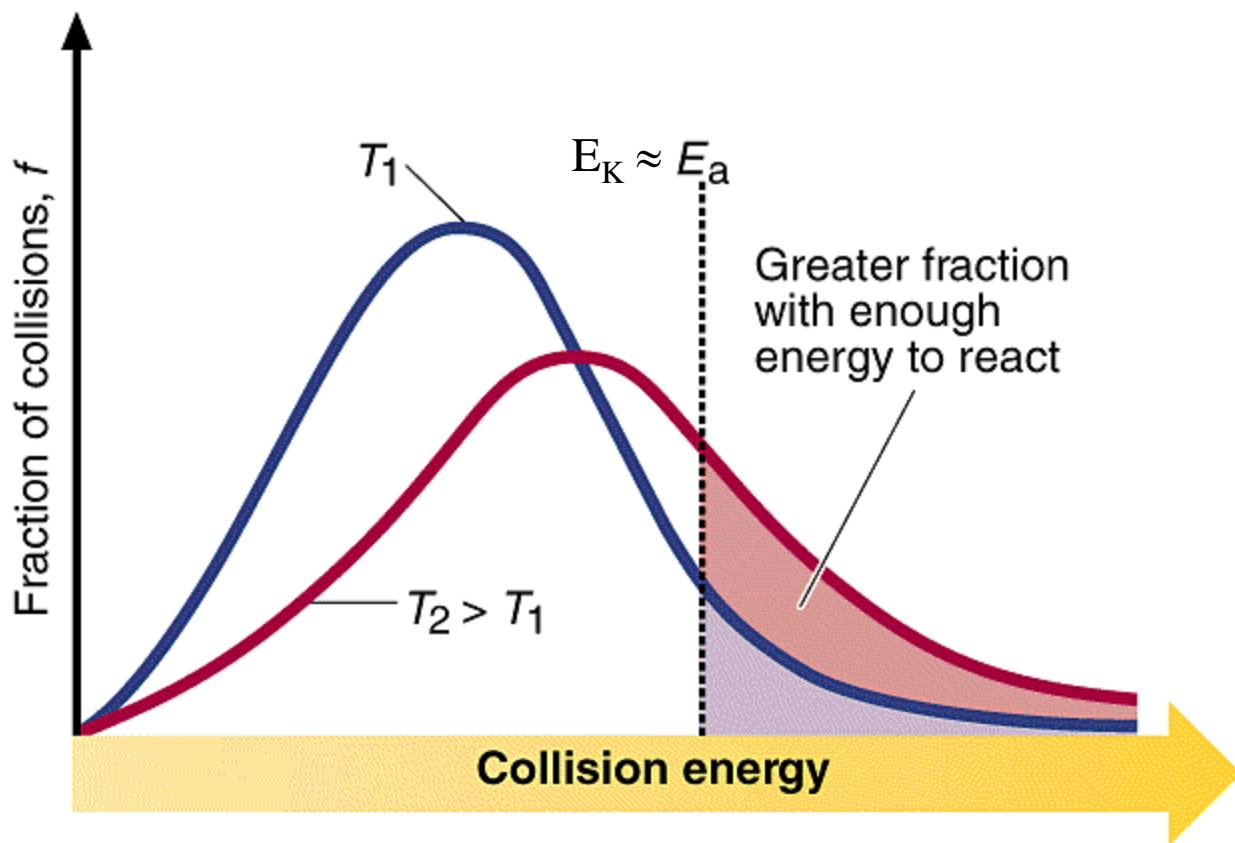
$$k, f \propto e^{-E_a/RT}$$



$$\lim_{x \rightarrow -\infty} e^x = 0$$

if  $T \rightarrow 0$ ,  $e^{-\infty} = 0 \rightarrow V = 0$

if  $T \rightarrow \infty$ ,  $e^{-0} = 1 \rightarrow V = V_{\max}$



*“the energy that must be overcome in order for a chemical reaction to occur (Ea)”*

S. Arrhenius (1859-1927)

