Acids and bases part 2

$$pH = - log_{10}[H_3O^+]$$

$$pOH = -\log_{10}[OH^{-}]$$

a 25 °
$$C$$
 $K_W = [H_3O^+] \times [OH^-] = 1.0 \times 10^{-14} M^2$

pH of a solution of a strong acid

$$HA (aq) + H_2O (I) \rightarrow A^- (aq) + H_3O^+ (aq)$$

- in water $[H_3O^+]_w = [OH^-]_w = 1.0 \times 10^{-7} M$.
- the strong acid HA is added, at a concentration = c_A
- since it is strong $[H_3O^+]_A = c_A$

•
$$[H_3O^+]_{total} = [H_3O^+]_w + [H_3O^+]_A = [H_3O^+]_w + c_A$$
 and $[OH^-]_{total} = [OH^-]_w$

• Q =
$$[H_3O^+]_{total}$$
 $[OH^-]_{total}$ = $([H_3O^+]_w + c_A)$ $[OH^-]_w > K_W$

•
$$K_W = ([H_3O^+]_w + c_A - x) ([OH^-]_w - x)$$

•
$$x^2 - ([H_3O^+]_w + [OH^-]_w + c_A) x + c_A[OH^-]_w = 0$$

$$x = \frac{[H_3O^+]_w + [OH^-]_w + c_A - \sqrt{c_A^2 + 4K_W}}{2}$$

$$[H_3O^+] = [H_3O^+]_w + c_A - x$$
 e $[OH^-] = K_W / [H_3O^+]$

Equation 1

pH of a solution of a strong acid - approximation

$$HA (aq) + H_2O (I) \rightarrow A^- (aq) + H_3O^+ (aq)$$

- in pure water $[H_3O^+]_w = [OH^-]_w = 1.0 \times 10^{-7} M$.
- the strong acid HA is added, at a concentration = c_A
- since it is strong $[H_3O^+]_A = c_A$

When the concentration of C_A is much larger than $[H_3O^+]_w$ from water self-protolysis:

$$pH = -\log_{10} c_A \qquad [H_3O^+]_{total} \approx c_A$$

pH of a solution of a strong base

$$B(aq) + H_2O(I) \rightarrow BH^+(aq) + OH^-(aq)$$

- in pure water $[OH^{-}]_{w} = 1.0 \times 10^{-7} M$.
- the strong base B is added, at a concentration = c_B
- since it is strong $[OH^-]_B = c_B$

$$pH = 14 - log_{10} c_B$$

$$[OH^-]_{total} \approx c_B$$

Range for the approximation $[H_3O^+]_{total} \approx c_A$ (or $[OH^-]_{total} \approx c_B$)

c _A (M)	$[H_3O^+](M)$ (eq. 1)	pH (eq. 1)	$-\log_{10}[c_A]$
10^{-8}	1.05×10^{-7}	6.97	8.00
10^{-7}	1.62×10^{-7}	6.79	7.00
10^{-6}	1.01x10 ⁻⁶	5.99	6.00
10^{-5}	10^{-5}	5.00	5.00
10^{-4}	10 ⁻⁴	4.00	4.00
10^{-3}	10^{-3}	3.00	3.00
10^{-2}	10^{-2}	2.00	2.00
10^{-1}	10^{-1}	1.00	1.00
1	1	0.00	0.00

$$c_A \ge 10^{-5} M$$

and

$$c_B \ge 10^{-5} M$$

pH of a solution of a weak acid

A weak acid is partially dissociated in water

$$HA (aq) + H_2O (I) \rightleftharpoons A^- (aq) + H_3O^+ (aq)$$

We have for species in solution: HA, A^- , H_3O^+ e OH^- .

$$\begin{split} K_A &= \frac{[A^-] \cdot [H_3 O^+]}{[HA]} \quad \text{Law of mass action for the acid} \\ K_W &= [H_3 O^+] \cdot [OH^-] \quad \text{Law of mass action for water} \\ c_A &= [HA] + [A^-] \quad \text{Law of mass conservation for the acid} \\ [H_3 O^+] &= [A^-] + [OH^-] \quad \text{Law of mass conservation for water} \end{split}$$

As in the previous case, the presence of the acid decreases water self-protolysis

$$HA (aq) + H_2O (1) \rightleftharpoons A^- (aq) + H_3O^+ (aq)$$

Approximations

if c_A is not too small and the acid is not too weak $(K_A > 10^{-14})$:

$$[H_3O^+]_{tot} \approx [H_3O^+]_{acid}$$
 then: $[H_3O^+]_{acid} = [A^-]$

Since the acid is weak, $\alpha \ll 1$ then: $c_A \approx [HA]$

if we substitute and we solve for $[H_3O^+]$

$$K_A = \frac{[H_3O^+] \cdot [A^-]}{[HA]}$$
 $[H_3O^+] [A^-] = K_A [HA]$

Using the approximations:

$$[H_3O^+]^2 = K_A c_A$$

$$[H_3O^+] = \sqrt{K_AC_A}$$

If $[H_3O^+] \ll c_A$, it is negligible with respect to c_A :

$$K_A = \frac{[H_3 O^+]^2}{c_A - A} \approx \frac{[H_3 O^+]^2}{c_A}$$

$$[H_3O^+] = \sqrt{K_A c_A}$$

$$c_A \approx [HA] \alpha \ll 1$$

And for a weak base:

$$[OH^-] = \sqrt{K_B c_B}$$

$$c_B \approx [B] \alpha << 1$$

Range of application for these approximations

Calculated pH for acetic acid 25 ° $C(K_A = 1.8 \cdot 10^{-5} M)$

[acid] (M)	pH (eq. 1)	pH (eq. 2)	pH (eq. 3)
10^{-7}	6.793	7.002	5.872
10^{-6}	6.018	6.022	5.372
10^{-5}	5.145	5.145	4.872
10^{-4}	4.464	4.463	4.372
10^{-3}	3.902	3.901	3.872
10^{-2}	3.382	3.381	3.372
10^{-1}	2.875	2.875	2.872
10^{-0}	2.373	2.373	2.372

$$c_A \ge 10^{-4} M$$

And for bases

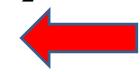
$$c_B \ge 10^{-4} M$$

eq.1
$$[H_3O^+]^3 + K_A[H_3O^+]^2 - (K_Ac_A + K_W) \cdot [H_3O^+] - K_AK_W = 0$$

eq.2
$$[H_3O^+] = \frac{-K_A + \sqrt{K_A^2 + 4K_Ac_A}}{2}$$

eq.3 $[H_3O^+] = \sqrt{K_Ac_A}$ Used to solve problems

eq. 3
$$[H_3O^+] = \sqrt{K_A c_A}$$



The strength of an acid or base increases as K_A o K_B increase

In chemistry and biochemistry we use a logarithmic scale to compare acids and bases.

$$\text{HA (aq)} + \text{H}_2\text{O (l)} \rightleftharpoons \text{A}^- (\text{aq}) + \text{H}_3\text{O}^+ (\text{aq}) \quad \text{K}_{\text{A}} = \frac{[\text{H}_3\text{O}^+] \cdot [\text{A}^-]}{[\text{HA}]}$$
 $p\text{K}_{\text{A}} = -\log_{10}\text{K}_{\text{A}}$

$$pK_A = -log_{10} K_A$$

$$B (aq) + H_2O (l) \rightleftharpoons BH^+ (aq) + OH^- (aq)$$
 $K_B = \frac{[OH^-] \cdot [BH^+]}{[B]}$ $pK_B = -log_{10} K_B$

$$pK_B = -log_{10} K_B$$

examples

$$NH_3 (aq) + H_2O (1) \rightleftharpoons NH_4^+ (aq) + OH^- (aq)$$

$$K_B = \frac{[OH^-] \cdot [NH_4^+]}{[NH_3]} = 1.8 \cdot 10^{-5} M \text{ a } 25 \text{ °C} \rightarrow pK_B = -\log_{10}(1.8 \cdot 10^{-5}) = 4.74$$

$$H_2CO_3 (aq) + H_2O (l) \rightleftharpoons HCO_3^-(aq) + H_3O^+(aq)$$

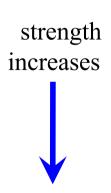
$$K_A = \frac{[H_3O^+] \cdot [HCO_3^-]}{[H_2CO_3]} = 4.2 \cdot 10^{-7} M \text{ a } 25 \text{ °C} \rightarrow pK_A = -\log_{10}(4.2 \cdot 10^{-7}) = 6.38$$

pK_A o pK_B decrease as the strength of an acid or a base increase

acid	formula	$K_{A}(M)$	рK
propanoic	CH ₃ CH ₂ COOH	1.3x10 ⁻⁵	4.89
acetic	CH ₃ COOH	1.8x10 ⁻⁵	4.74
methanoic	НСООН	1.8x10 ⁻⁴	3.74



base	formula	$K_{A}(M)$	pK
aniline	C ₆ H ₅ NH ₂	4.0x10 ⁻¹⁰	9.40
ammonia	NH ₃	1.8x10 ⁻⁵	4.74
methylammine	CH ₂ NH ₂	5.0x10 ⁻⁴	3.30



Acids and bases part 3

Relationship between the ionization constants of an acid and its conjugate base

HCN (aq) +
$$H_2O(1) \rightleftharpoons CN^-(aq) + H_3O^+(aq)$$

Conjugate couple

The product between K_A of an acid and K_B of its conjugate base is K_W :

$$K_A K_B = K_W$$

$$pK_A + pK_B = 14$$

$$HA (aq) + H_2O (1) \rightleftharpoons A^{-} (aq) + H_3O^{+} (aq)$$

$$K_A = \frac{[H_3 O^+] \cdot [A^-]}{[HA]}$$

$$A^{-}$$
 (aq) + H_2O (I) \rightleftharpoons HA (aq) + OH^{-} (aq)

$$K_B = \frac{[OH^-] \cdot [AH]}{[A^-]}$$

$$K_A \cdot K_B = \frac{[H_3 O^+] \cdot [A^-]}{[HA]} \bullet \frac{[OH^-] \cdot [AH]}{[A^-]} = [H_3 O^+] \cdot [OH^-] = K_W$$

Therefore K_B can be calculated: K_W/K_A

Interactions between the ionization constants of an acid and its conjugate base with H_2O at 25 $^\circ$ C

$$HCN (aq) + H_2O (l) \rightleftharpoons CN^-(aq) + H_3O^+(aq)$$
 $K_A = 4.0x10^{-5} M$ $CN^-(aq) + H_2O (l) \rightleftharpoons HCN (aq) + OH^-(aq)$ $K_B = 2.5x10^{-10} M$

$$2 \text{ H}_2\text{O} (1) \rightleftharpoons \text{H}_3\text{O}^+(\text{aq}) + \text{OH}^-(\text{aq}) \qquad \text{K}_W = \text{K}_A\text{K}_B = 1.0 \times 10^{-14} \text{ M}^2$$

$$K_{A} \cdot K_{B} = \frac{[H_{3}O^{+}] \cdot [CN^{-}]}{[HCN]} \cdot \frac{[HCN] \cdot [OH^{-}]}{[CN^{-}]} = [H_{3}O^{+}] \cdot [OH^{-}] = K_{W}$$

$$K_A K_B = K_W$$

$$pK_A + pK_B = pK_W$$

Therefore K_B can be calculated: K_W/K_A

pK of some acids and of their conjugate bases at 25 ° C: $14 = pK_A + pK_B$

Name of acid	acido	pK_A	base	pK_{B}	Name of base
hydronium	H_3O^+	0	H_2O	14	water
phosphoric	H ₃ PO ₄	2.12	$\mathrm{H_2PO_4}^-$	11.88	Dihydrogen phosphate
fluoridire	HF	3.14	F-	10.86	fluoride
acetic	CH₃COOH	4.74	CH ₃ COO-	9.25	acetate
carbonic	H ₂ CO ₃	6.38	HCO ₃ ⁻	7.62	Hydrogen carbonate
sulphidric	H_2S	7	HS ⁻	7	Hydrogen sulphide
Dihydrogen phosphate	$\mathrm{H_{2}PO_{4}^{-}}$	7.21	HPO ₄ ²⁻	6.79	Hydrogen phosphate
ammonium	NH ₄ ⁺	9.25	NH ₃	4.74	ammonia
cianidric	HCN	9.4	CN-	4.6	cianide
Hydrogen carbonate	HCO ₃ ⁻	10.32	CO ₃ ²⁻	3.68	carbonate
Hydrogen phosphate	HPO ₄ ²⁻	12.44	PO ₄ ³⁻	1.56	phosphate
water	H_2O	14	OH-	0	hydroxide

forza della base crescente

Types of acid-base reactions

We studied the reaction between acids and bases (strong and weak) with amphiprotic water has been studied. Acids and bases can react in water to form a salt.

$$acid + base \approx salt + H_2O$$

type	example
strong acid + strong base	$HC1 + NaOH \rightarrow NaC1 + H_2O$
strong acid + weak base	$HC1 + NH_3 \rightleftharpoons NH_4C1 + H_2O$
weak acid + strong base	CH ₃ COOH + NaOH ⇌ CH ₃ COONa + H ₂ O
weak acid + weak base	$CH_3COOH + NH_3 \rightleftharpoons CH_3COONH_4 + H_2O$

Reaction between strong acid and strong base: neutralization

Strong acids and bases are 100 % ionized in solution:

HC1 (aq) + H₂O
$$\longrightarrow$$
 H₃O⁺ (aq) + Cl⁻ (aq)
NaOH (aq) \longrightarrow Na⁺ (aq) + OH⁻ (aq)

The net equation between HCl (strong acid) and NaOH (strong base) is:

$$H_{3}O^{+} (aq) + Cl^{-} (aq) + Na^{+} (aq) + OH^{-} (aq) \rightleftharpoons 2 H_{2}O (l) + Na^{+} (aq) + Cl^{-} (aq)$$

$$H_{3}O^{+} (aq) + OH^{-} (aq) \rightleftharpoons 2 H_{2}O (l)$$

$$K = \frac{1}{[H_{3}O^{+}] \cdot [OH^{-}]} = \frac{1}{K_{W}} = 1.0 \cdot 10^{14} M^{-2}$$

The net ionic equation for the reaction of a strong acid with a strong base is always the union of a hydronium ion with a hydroxide ion to give water. Since $K = 1 / K_W$, reagents are fully consumed to $K = 1 / K_W$, reagents are fully consumed to yield products. If an equal amount of moles of NaOH and HCl, are mixed, the result is a neutral NaCl solution (pH = 7.0 at 25 $^{\circ}$ C)

Chemistry of acids and bases 3

- Salt hydrolysis
- Buffer solutions
- Acid-base titrations

Hydrolytic equilibria

The aqueous solution of a salt obtained from an acid and a strong base contains the free ionic species that form the salt.

Base and acid (strong)	Salt solution	pН
$NaOH + HCl \longrightarrow NaCl + H_2O$	$NaCl(s) \rightarrow Na^{+}(aq) + Cl^{-}(aq)$	7
$NaOH + HNO_3 \longrightarrow NaNO_3 + H_2O$	$NaNO_3(s) \rightarrow Na^+(aq) + NaNO_3^-(aq)$	7
$KOH + HClO_4 \longrightarrow KClO_4 + H_2O$	$KClO_4(s) \rightarrow K^+(aq) + ClO_4^-(aq)$	7
$KOH + HBr \longrightarrow KBr + H_2O$	$KBr(s) \rightarrow K^{+}(aq) + Br^{-}(aq)$	7
$Ca(OH)_2 + 2 HC1 \longrightarrow CaCl_2 + H_2O$	$CaCl_2(s) \rightarrow Ca^{2+}(aq) + 2 Cl^-(aq)$	7

In these solutions there is no proton exchange because both cation (conjugated acid of the strong base) and anion (conjugated base of the strong acid) do not tend to release or subtract protons from water. The solution is therefore neutral.

We call hydrolysis those proton exchange reactions (acid-base) that are established in the aqueous solutions of salts formed by:

- weak acids and strong bases (which contain moderately strong conjugated bases and very weak conjugated acids): basic hydrolysis, pH > 7
- weak bases and strong acids (which contain moderately strong conjugated acids and very weak conjugated bases): acid hydrolysis, pH > 7
- acids and bases both weak (which contain moderately strong conjugated acids and bases): basic, acid or neutral hydrolysis

As a result of these exchanges of protons with the aqueous amphiprotic solvent there is a variation in the concentration of $[H_3O^+]$ and $[OH^-]$ (pH)

$$NH_4Cl(s) \rightarrow NH_4^+(aq) + Cl^-(aq)$$

$$NH_4^+$$
 (aq) + H_2O (l) $\rightleftharpoons NH_3$ (aq) + H_3O^+ (aq)

Salt formed by weak acids and strong bases: basic hydrolysis

The dissociation of the salt CA is followed by the protonation equilibrium of the anion A^- , which is a moderately strong Brønsted base.

$$CA (aq) \rightarrow C^{+} (aq) + A^{-} (aq)$$

 $A^{-} (aq) + H_{2}O (l) \rightleftharpoons HA (aq) + OH^{-} (aq)$

$$CH_3COONa (aq) \rightarrow Na^+ (aq) + CH_3COO^- (aq)$$

 $CH_3COO^- (aq) + H_2O (l) \rightleftharpoons CH_3COOH (aq) + OH^- (aq)$

$$KCN (aq) \rightarrow K^{+} (aq) + CN^{-} (aq)$$

 $CN^{-} (aq) + H_{2}O (l) \rightleftharpoons HCN (aq) + OH^{-} (aq)$

$$KNO_2 (aq) \rightarrow K^+ (aq) + NO_2^- (aq)$$

 $NO_2^- (aq) + H_2O (l) \rightleftharpoons HNO_2 (aq) + OH^- (aq)$

Due to the hydrolytic equilibrium, the solution is enriched with OH-ions.

The equilibrium constant of this equilibrium is called hydrolysis constant K_i :

$$A^{-}(aq) + H_{2}O(1) \rightleftharpoons HA(aq) + OH^{-}(aq)$$

$$K_{i} = \frac{[HA] \cdot [OH^{-}]}{[A^{-}]}$$

 K_i is directly related to K_A of the weak acid that is formed:

$$K_{i} = \frac{[HA] \cdot [OH^{-}]}{[A^{-}]} = \frac{[HA] \cdot [OH^{-}]}{[A^{-}]} \cdot \frac{[H_{3}O^{+}]}{[H_{3}O^{+}]} = \frac{K_{W}}{K_{A}}$$

$$K_{i} = \frac{K_{W}}{K_{A}}$$

$$[OH^{-}] = \sqrt{K_{i}c_{S}} = \sqrt{\frac{K_{W}}{K_{A}}c_{S}}$$

The weaker the acid and the higher the salt concentration, the more basic is the resulting solution.

Alkaline hydrolisis pH determination formula

$$K_{i} = \frac{[HA] \cdot [OH^{-}]}{[A^{-}]} = \frac{[HA] \cdot [OH^{-}]}{[A^{-}]} \cdot \frac{[H_{3}O^{+}]}{[H_{3}O^{+}]} = \frac{K_{W}}{K_{A}}$$

$$K_{i} = \frac{K_{W}}{K_{A}}$$

$$K_{i} = \frac{K_{W}}{K_{A}}$$

The OH- arising from water selfprotolysis are negligible: [OH-]=[HA] And if we consider that A^{-} is a weak base: $[A^{-}]=c_{s}$

Rearranging Ki

$$[OH^-]^2$$
=Ki c_s

$$[OH^-] = \sqrt{K_i c_S} = \sqrt{\frac{K_W}{K_A} c_S}$$



Salt formed by weak base and strong acid: acid hydrolysis

The dissociation of the salt BHA is followed by the deprotonation equilibrium of the cation BH, which is a moderately strong Brønsted acid.

BHA (aq)
$$\rightarrow$$
 BH⁺ (aq) + A⁻ (aq)
BH⁺ (aq) + H₂O (l) \rightleftharpoons B (aq) + H₃O⁺ (aq)

$$NH_4Cl (s) \rightarrow NH_4^+ (aq) + Cl^- (aq)$$

 $NH_4^+ (aq) + H_2O (l) \rightleftharpoons NH_3 (aq) + H_3O^+ (aq)$

$$C_6H_5NH_3Cl(s) \rightarrow C_6H_5NH_3^+(aq) + Cl^-(aq)$$

 $C_6H_5NH_3^+(aq) + H_2O(l) \rightleftharpoons C_6H_5NH_2(aq) + H_3O^+(aq)$

Due to the hydrolytic equilibrium, the solution is enriched with H_3O^+ ions.

The complete dissociation of BHA salt is accompanied by the deprotonation equilibrium of the BH+ cation, which is a moderately strong Brønsted acid.

Acid hydrolisis pH determination formula

$$K_{i} = \frac{[B] \cdot [H_{3}O^{+}]}{[BH^{+}]} = \frac{[B] \cdot [H_{3}O^{+}]}{[BH^{+}]} \cdot \frac{[OH^{-}]}{[OH^{-}]} = \frac{K_{W}}{K_{B}}$$

$$K_{i} = \frac{K_{W}}{K_{B}}$$

The H₃O⁺ arising from water self-

protolysis are negligible: $[H_3O^+]=[HA]$

And if we consider that

BH⁺ is a weak acid: $[BH^+]=c_s$

Rearranging Ki

$$[H_3O^+]^2$$
=Ki c_s

$$[H_3O^+] = \sqrt{K_i c_S} = \sqrt{\frac{K_W}{K_B} c_S}$$



The hydrolysis constant K_i:

$$BH^{+}(aq) + H_{2}O(1) \rightleftharpoons B(aq) + H_{3}O^{+}(aq)$$

 K_i is related to K_B of the weak base that is formed:

$$K_{i} = \frac{[B] \cdot [H_{3}O^{+}]}{[BH^{+}]} = \frac{[B] \cdot [H_{3}O^{+}]}{[BH^{+}]} \cdot \frac{[OH^{-}]}{[OH^{-}]} = \frac{K_{W}}{K_{B}}$$

$$K_{i} = \frac{K_{W}}{K_{B}}$$
 $[H_{3}O^{+}] = \sqrt{K_{i}c_{S}} = \sqrt{\frac{K_{W}}{K_{B}}c_{S}}$

The weaker the base and the higher the salt concentration, the more acidic is the resulting solution.

Salt formed from a weak acid and base: hydrolysis

The full dissociation of the salt BHA is accompanied by the dissociation of BH^+ and by protonation of A^-

BHA (aq)
$$\to$$
 BH⁺ (aq) + A⁻ (aq)
BH⁺ (aq) + H₂O (l) \rightleftharpoons B (aq) + H₃O⁺ (aq)
A⁻ (aq) + H₂O (l) \rightleftharpoons HA (aq) + OH⁻ (aq)
H₃O⁺ (aq) + OH⁻ (aq) \rightleftharpoons 2 H₂O (l)
BH⁺ (aq) + A⁻ (aq) \rightleftharpoons B (aq) + HA (aq)

As usual we neglect hydrogen and hydroxide ions coming from water dissociation if the salt concentration is not too small.

$$BH^{+}(aq) + A^{-}(aq) \rightleftharpoons B(aq) + HA(aq)$$

$$K_{i} = \frac{K_{W}}{K_{A}^{HA} \cdot K_{B}^{B}}$$

$$K_{i} = \frac{K_{W}}{K_{A}^{HA} \cdot K_{B}^{B}}$$

$$[H_3O^+] = \sqrt{\frac{K_A^{HA}}{K_B^B} \cdot K_W}$$

$$K_{A}^{HA} = K_{B}^{B} \rightarrow pH = 7$$
if: $K_{A}^{HA} > K_{B}^{B} \rightarrow pH < 7$

$$K_{A}^{HA} < K_{B}^{B} \rightarrow pH > 7$$

Exercise 13. Calculate the pH of a 0.2 M of Na Acetate solution $(K_A = 1.8 \cdot 10^{-5} \text{ M a } 25 ^{\circ} \text{ C})$

Exercise 13. Calculate the pH of a 0.2 M of Na Acetate solution $(K_A = 1.8 \cdot 10^{-5} \text{ M a } 25^{\circ} \text{ C})$

$$CH_3COONa (aq) \rightarrow Na^+ (aq) + CH_3COO^- (aq)$$

$$CH_3COO^-(aq) + H_2O(1) \rightleftharpoons CH_3COOH(aq) + OH^-(aq)$$

We will have an alkaline hydrolisis

Exercise 13. Calculate the pH of a 0.2 M of Na Acetate solution $(K_A = 1.8 \cdot 10^{-5} \text{ M a } 25^{\circ} \text{ C})$

$$CH_3COONa (aq) \rightarrow Na^+ (aq) + CH_3COO^- (aq)$$

$$CH_3COO^-(aq) + H_2O(1) \rightleftharpoons CH_3COOH(aq) + OH^-(aq)$$

We will have an alkaline hydrolisis

$$[OH^{-}] = \sqrt{K_{i} \cdot c_{S}} = \sqrt{\frac{K_{W}}{K_{A}} c_{S}} = \sqrt{\frac{1 \cdot 10^{-14}}{1.8 \cdot 10^{-5}}} \cdot 0.2 = 1.05 \cdot 10^{-5} \text{ M}$$

 $pOH = 4.98 \implies pH = 14 - 4.98 = 9.02$

Exercise 14. Calculate the pH of 0.1 M ammonium chloride solution ($K_B = 1.8 \cdot 10^{-5}$ M a 25 ° C)

Exercise 14. Calculate the pH of 0.1 M ammonium chloride solution ($K_B = 1.8 \cdot 10^{-5}$ M a 25 ° C)

$$NH_4Cl(s) \rightarrow NH_4^+(aq) + Cl^-(aq)$$

$$NH_4^+$$
 (aq) + H_2O (l) $\rightleftharpoons NH_3$ (aq) + H_3O^+ (aq)

We have an acid hydrolysis

Exercise 14. Calculate the pH of 0.1 M ammonium chloride solution ($K_B = 1.8 \cdot 10^{-5}$ M a 25 ° C)

$$NH_4Cl(s) \rightarrow NH_4^+(aq) + Cl^-(aq)$$

$$NH_4^+$$
 (aq) + H_2O (l) $\rightleftharpoons NH_3$ (aq) + H_3O^+ (aq)

We have an acid hydrolysis

$$[H_3O^+] = \sqrt{K_i \cdot c_S} = \sqrt{\frac{K_W}{K_B} \cdot c_S} = \sqrt{\frac{1 \cdot 10^{-14}}{1.8 \cdot 10^{-5}} \cdot 0.1} = 7.45 \cdot 10^{-6} \text{ M}$$

$$pH = 5.12$$

Exercise 15. Calculate the pH of a 0.05 M ammonium fluoride solution (ammonia $K_B = 1.8 \cdot 10^{-5}$ M; HF $K_A = 7.2 \cdot 10^{-4}$ M at 25 ° C)

Exercise 15. Calculate the pH of a 0.05 M ammonium fluoride solution (ammonia $K_B = 1.8 \cdot 10^{-5}$ M; HF $K_A = 7.2 \cdot 10^{-4}$ M at 25 ° C)

$$NH_{3}F (aq) \rightarrow NH_{4}^{+} (aq) + F^{-} (aq)$$
 $NH_{4}^{+} (aq) + H_{2}O (1) \rightleftharpoons NH_{3} (aq) + H_{3}O^{+} (aq)$
 $F^{-} (aq) + H_{2}O (1) \rightleftharpoons HF (aq) + OH^{-} (aq)$
 $H_{3}O^{+} (aq) + OH^{-} (aq) \rightleftharpoons 2 H_{2}O (1)$
 $NH_{4}^{+} (aq) + F^{-} (aq) \rightleftharpoons NH_{3} (aq) + HF (aq)$

Exercise 15. Calculate the pH of a 0.05 M ammonium fluoride solution (ammonia $K_B = 1.8 \cdot 10^{-5}$ M; HF $K_A = 7.2 \cdot 10^{-4}$ M at 25 ° C)

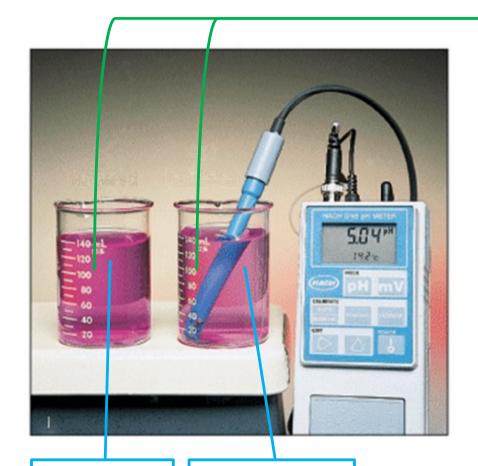
$$NH_{3}F (aq) \rightarrow NH_{4}^{+} (aq) + F^{-} (aq)$$
 $NH_{4}^{+} (aq) + H_{2}O (1) \rightleftharpoons NH_{3} (aq) + H_{3}O^{+} (aq)$
 $F^{-} (aq) + H_{2}O (1) \rightleftharpoons HF (aq) + OH^{-} (aq)$
 $H_{3}O^{+} (aq) + OH^{-} (aq) \rightleftharpoons 2 H_{2}O (1)$
 $NH_{4}^{+} (aq) + F^{-} (aq) \rightleftharpoons NH_{3} (aq) + HF (aq)$

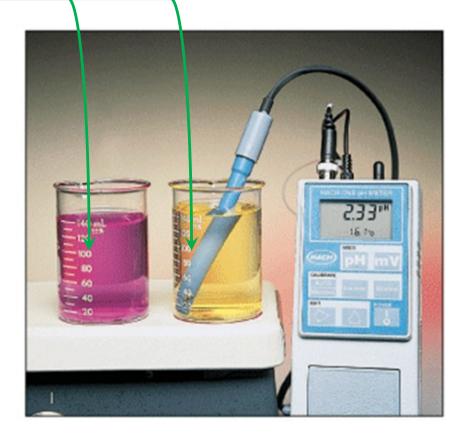
$$[H_3O^+] = \sqrt{\frac{K_A^{HF}}{K_B^{NH_3}} \cdot K_W} = \sqrt{\frac{7.2 \Box 10^4}{1.8 \Box 10^5} \cdot 1.0 \cdot 10^{-14}} = 6.32 \cdot 10^{-7} \text{ M}$$

$$pH = 6.20$$

Controlling pH: Buffer solutions

+ HCI to both solutions



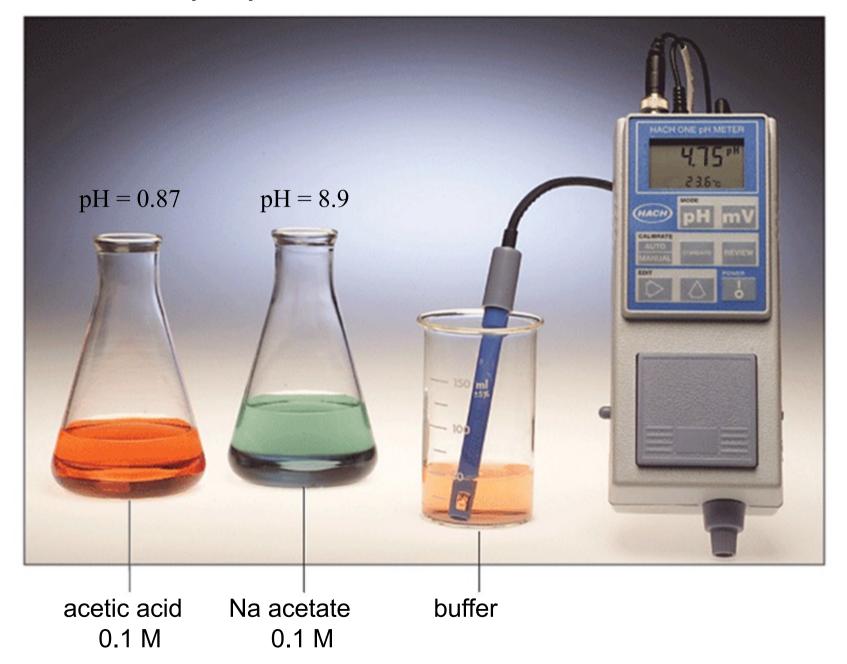


Buffered solution pH 5.04

Not buffred solution pH 5.04

After the addition of HCl, the pH of the buffered solution does not change (or changes slightly), while the non-buffered solution drops to pH 2.33. The buffered solution hampers pH variations.

How do we prepare a buffer solution?



How do we prepare a buffer solution?

A buffer solution is an aqueous solution in which the pH does not vary appreciably upon small additions of strong acids or bases.

To make a buffer solution we have to satisfy two conditions:

- we need the simultaneous presence of two species: an acid capable of reacting with OH^- ions and a base capable reacting with H_3O^+ ion.
- •The acid and the base must not react with each other.

A buffer solution is usually prepared from approximately equal amounts of a conjugated acid-base pair:

- a weak acid and its conjugate base (e.g. acetic acid and acetate ion)
- a weak base and its conjugate acid (e.g. ammonia and ammonium ion)

How does a buffer solution work?

In the acetic acid/acetate buffer, acetic acid (weak acid) is required to react and consume the added hydroxide ions:

$$CH_3COOH$$
 (aq) + OH^- (I) $\rightleftarrows CH_3COO^-$ (aq) + H_2O (aq)

$$K = \frac{[CH_3COO^-]}{[CH_3COOH] \cdot [OH^-]} = \frac{K_A}{K_W} = \frac{1.8 \cdot 10^{-5}}{1.0 \cdot 10^{-14}} = 1.8 \cdot 10^9 \text{ M}^{-1}$$

The equilibrium constant for the reaction is very large because the OH^- ion is a much stronger basis than acetate ($CH3COO^{-)}$). This means that all OH^- ions, coming from an external source, are completely consumed.

Similarly, each hydronium ion added to the solution will react with the acetate ion present in the buffer.

$$CH_3COO^-(aq) + H_3O^+(1) \rightleftharpoons CH_3COOH(aq) + H_2O(aq)$$

$$K = \frac{[CH_3COOH]}{[CH_3COO^-] \cdot [H_3O^+]} = \frac{1}{K_A} = \frac{1}{1.8 \cdot 10^{-5}} = 5.6 \cdot 10^4 \text{ M}^{-1}$$

The equilibrium constant for this reaction is very large, since the H_3O^+ ion is a much stronger acid than acetic acid (CH_3COOH).

Common buffers in laboratory practice

Weak acid	Conjugate base	$K_A(M)$	Buffering range pH
Acetic acid CH ₃ COOH	acetate CH ₃ COO ⁻	$1.8 \cdot 10^{-5}$	3.7–5.8
dhydrogen phosphate H ₂ PO ₄ ⁻	hydrogen phosphate HPO ₄ ²⁻	$6.2 \cdot 10^{-8}$	6.2-8.2
hydrogen carbonate HCO ₃ ⁻	carbonate CO ₃ ²⁻	$4.8 \cdot 10^{-11}$	9.3–11.3
hydrogen phosphate HPO ₄ ²⁻	phosphate PO ₄ ³⁻	$3.6 \cdot 10^{-13}$	11.3–13.3

Buffer system in the blood

- bicarbonate
- hemoglobin
- phosphate

The Henderson-Hasselbalch equation

$$pH = pK_A + \log_{10} \frac{\text{[coniugate base]}}{\text{[acid]}}$$



L.J. Henderson (1878–1942)

The pH of a buffer solution is controlled by two factors:

- the strength of the acid (indicated by K_A o pK_A)
- the relative amounts of the acid and of its conjugate base

The pH of a buffer solution is mainly determined by the value of pK_A and the fine pH control is achieved by modifying the relative amounts of conjugate base and acid.

$$if \frac{[\text{conjugate base}]}{[\text{acid}]} > 1 \rightarrow pH > pK_A$$

$$if \frac{[\text{conjugate base}]}{[\text{acid}]} = 1 \rightarrow pH = pK_A$$

$$if \frac{[\text{conjugate base}]}{[\text{acid}]} < 1 \rightarrow pH < pK_A$$

The Henderson-Hasselbalch Equation

In a buffer solution containing a weak acid HA and its conjugate base A⁻:

HA (aq) + H₂O (l)
$$\rightleftharpoons$$
 A⁻ (aq) + H₃O⁺ (aq) $K_A = \frac{[A^-] \cdot [H_3 O^+]}{[HA]}$

$$[H_3 O^+] = K_A \cdot \frac{[HA]}{[A^-]} = K_A \cdot \frac{[acid]}{[conjugate base]}$$

Let's use the co-logarithmic expression:

$$-\log_{10}[H_3O^+] = -\log_{10} K_A - \log_{10} \frac{\text{[acid]}}{\text{[conjugate base]}}$$
$$= -\log_{10} K_A + \log_{10} \frac{\text{[conjugate base]}}{\text{[acid]}}$$

$$pH = pK_A + \log_{10} \frac{\text{[conjugate base]}}{\text{[acid]}}$$

Preparing a buffer solution

We have two main conditions to satisfy:

• Control of pH: it has to be efficient at the desired pH. Use Henderson-Hasselbalch equation.

$$pH = pK_A + \log_{10} \frac{\text{[conjugate base]}}{\text{[acid]}}$$

First of all, on has to choose a a weak acid that has a K_A or pK_A close to the desired $[H_3O^+]$ or pH. The precise pH value is achieved adjusting the [conjugate base]/[acid] value.

• buffering power: the buffer solution has to compensate the amounts of acid or alkali added. E.g. in an acetate buffer we must have enough aceti acid to compensate for the acid which we foresee to be introduced. A buffer solution is not effective, once the acid or conjuate base from the buffer is consumed.

Buffering power β

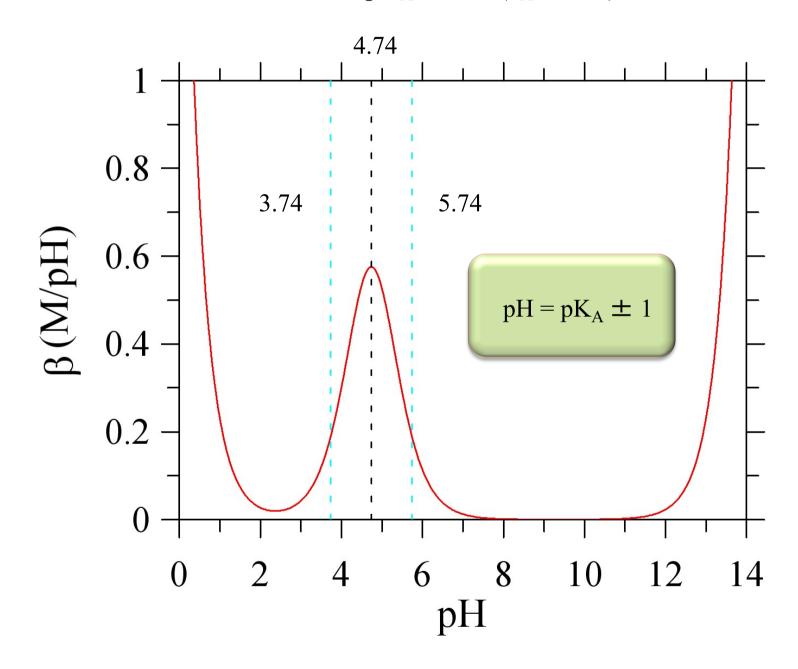
A buffer is at maximum efficacy pH is close to pK_A , i.e. when:

The buffering power β is defined as the amount of base that leads to an increase of pH of 1.

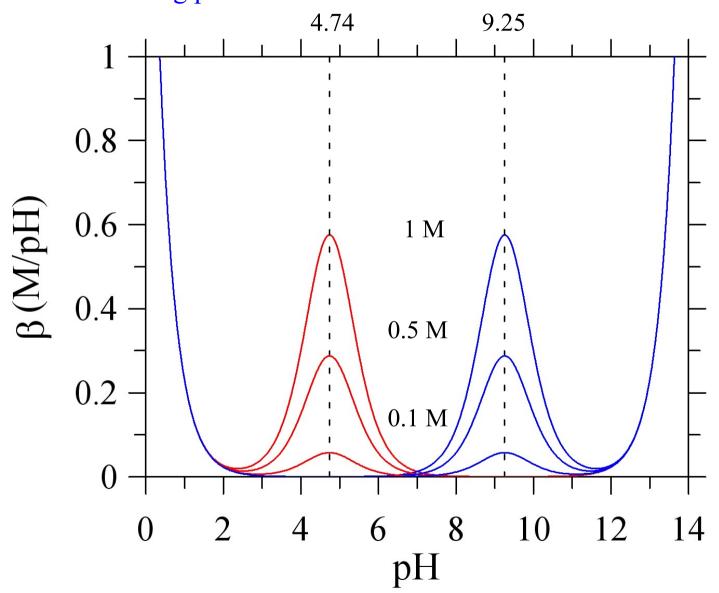
$$\beta = \frac{dc_B}{dpH} = -\frac{dc_A}{dpH}$$

A buffer is efficient if $pH = pK_A \pm 1$

The acetic acid /acetate buffer pK_A = 4.74 (c_A = 1 M)



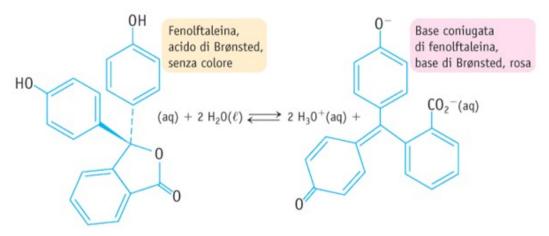
Acetate buffer $pK_A = 4.74$ and ammonia buffer $pK_B = 9.25$ Buffering power decreases with buffer concentration



pH indicators

pH indicators

A pH indicator is a weak acid or a weak base in which protonated and deprotonated forms have different colours.







It is added in small quantities to a solution (to affect the least the pH) and it has different colours, depending on the pH of the solution.

If the indicator is a weak acid, we indicate as Hind (colour red) the protonated form and as con Ind⁻ (blue colour).

The indicator is in equilibrium in water:

HInd
$$(aq) + H_2O(1) \rightleftharpoons Ind^-(aq) + H_3O^+(aq)$$

$$[Ind^-] \cdot [H_3O^+] \qquad K_{\Delta} \qquad [Ind^-]$$

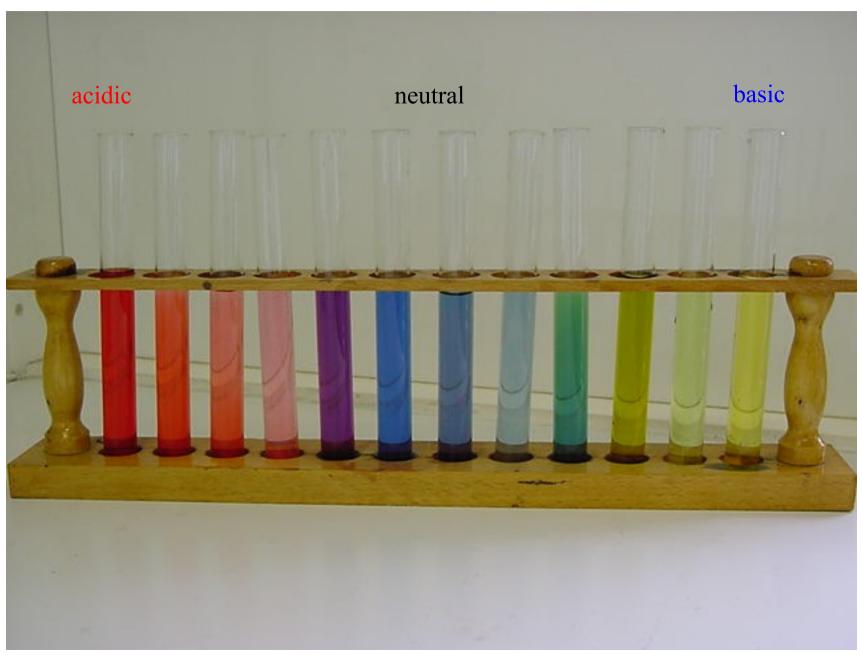
$$K_{A} = \frac{[Ind^{-}] \cdot [H_{3}O^{+}]}{[HInd]} \quad \frac{K_{A}}{[H_{3}O^{+}]} = \frac{[Ind^{-}]}{[HInd]}$$

The ratio [Ind⁻] / [HInd] determines the colour of the solution. We can have three limit cases:

$$[H_3O^+] > K_A \rightarrow [HInd] > [Ind^-]$$
 red solution
 $[H_3O^+] = K_A \rightarrow [HInd] = [Ind^-]$ purple solution
 $[H_3O^+] < K_A \rightarrow [HInd] < [Ind^-]$ blue solution

Each acidic indicator will be characterized by a K_A : in solution it will have the colour of the protonated form HInd if $pH < pK_A$. If $pH > pK_A$ the it will have the colour of the deprotonated species Ind⁻.

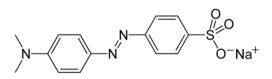
Anthocyanins from red cabbage

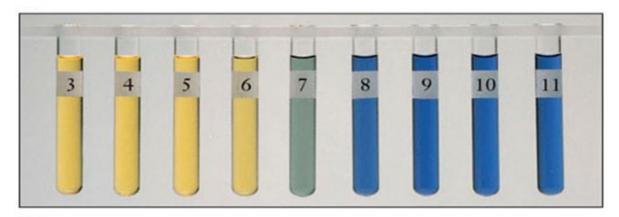


Colour change for some indicators:

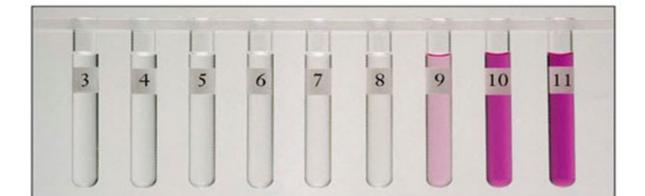


Methyl orange



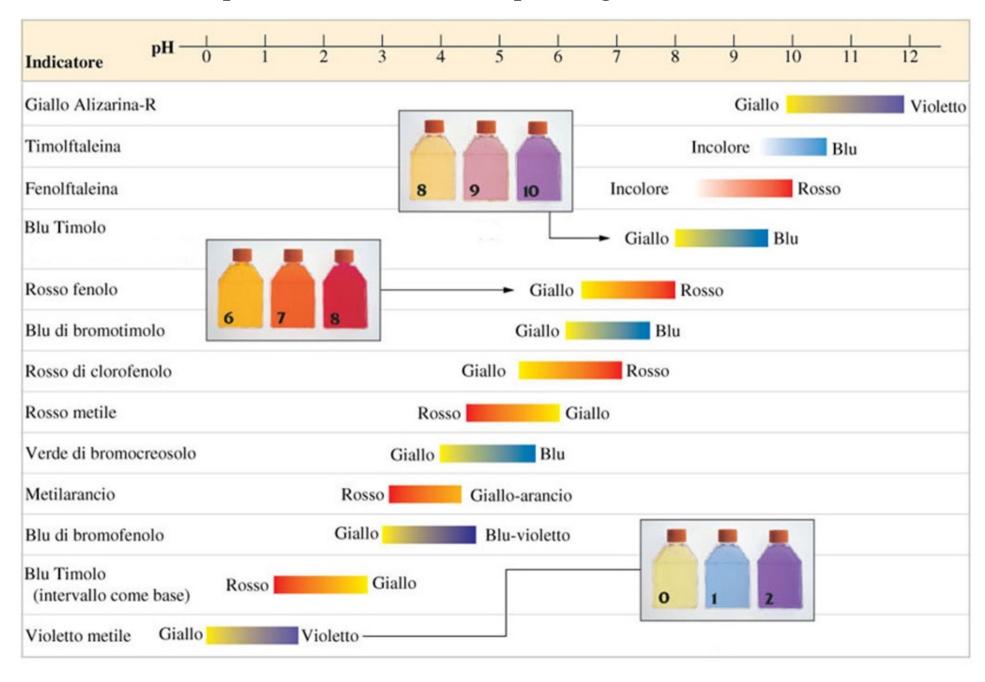


Bromothymol blue



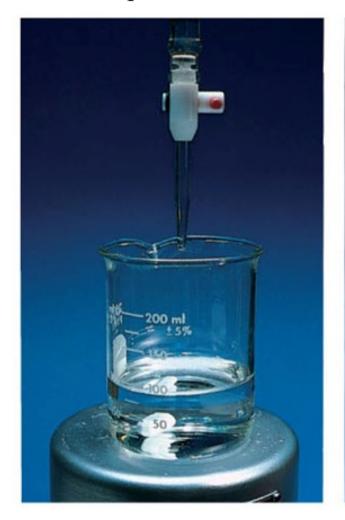
Phenolphtalein

Some pH indicators and their pH range



Acid-base titration with phenolphtalein

In an acidic solution, phenolphthalein is colourless and it remains so as long as the colour-transition point is achieved. When the pH reaches 9 the solution starts to turn pink







Acid-base titrations

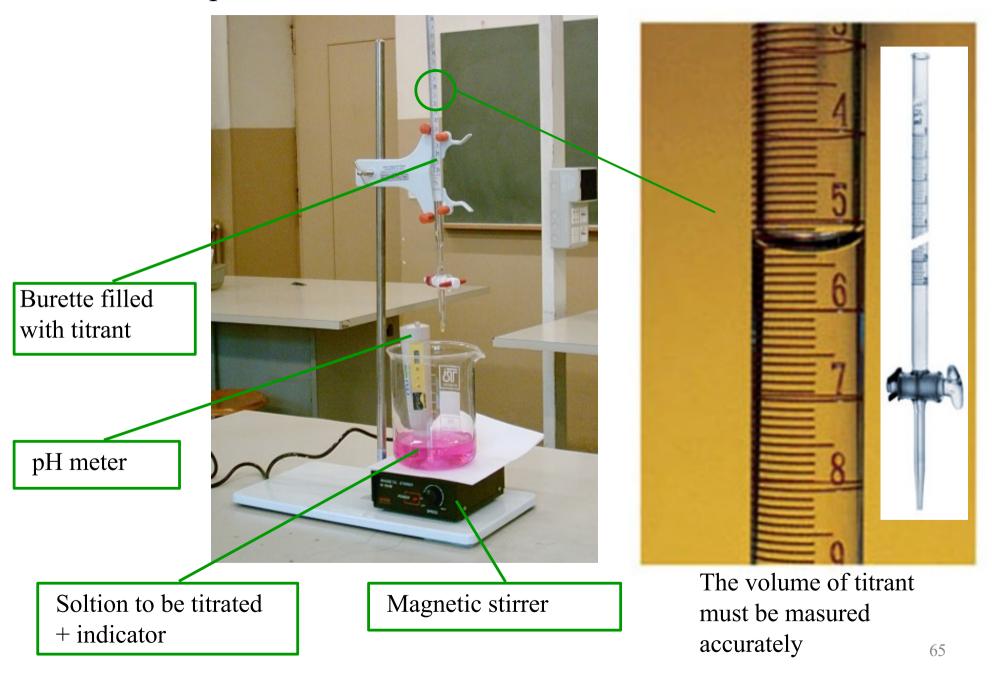
An acid-base titration allows one to determine the quantity of acid (or base) present in a solution by measuring the volume of a solution with a known concentration of base (or acid) necessary to achieve complete neutralization.

The acid solution to be titrated is introduced into a a flask and the base solution of known concentration is placed in a graduated burette above the container and added drop by drop until the acid is completely neutralized. From the volume of base added we can immediately calculate the number of moles of base necessary for neutralization

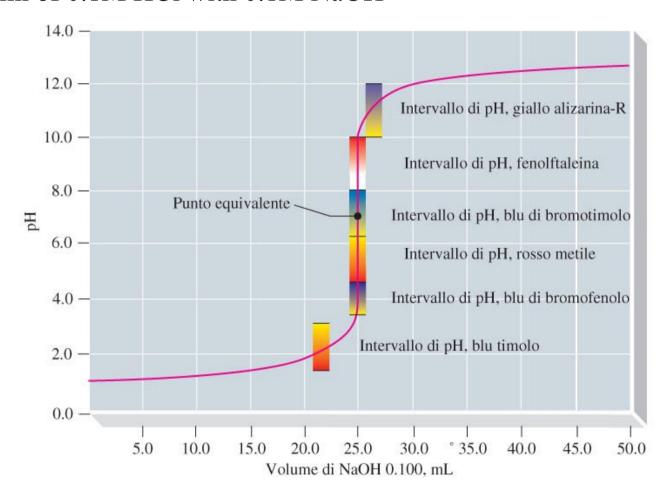
 $n_{\text{Base}} = \text{volume} \cdot \text{concentration}$

This amounts corresponds to the acid present (for a monoprotic acid). To appreciate neutralization one adds an indicator with turning poin at pH ≈ 7

Titration in paractice



An acid-base titration plot is a graph plotting the pH of an acid (or base) solution as a function of the volume of base (acid) added. The figure below shows the titration curve of 25ml of 0.1M HCl with 0.1M NaOH



The equivalence point of a titration is the point that corresponds to the addition of a stoichiometric amount of base (or acid). For an acid-base titration of strong electrolytes the equivalence point will be at pH=7.

66

Titration of a strong acid with a strong base

During titration the pH is calculated taking into account that the number of moles of base added neutralize the same number of moles of acid: the number of remaining moles of acid is divided by the total volume (which has increased compared to the initial value).

Initially we have a stron acid HA at concentration=c_A $pH = -log_{10}c_A$. If one adds the strong base B: $HA (aq) + B (aq) \rightarrow BHA (aq) + H₂O (1)$

$$n_{A} = c_{A} \cdot V_{\text{initial}}$$

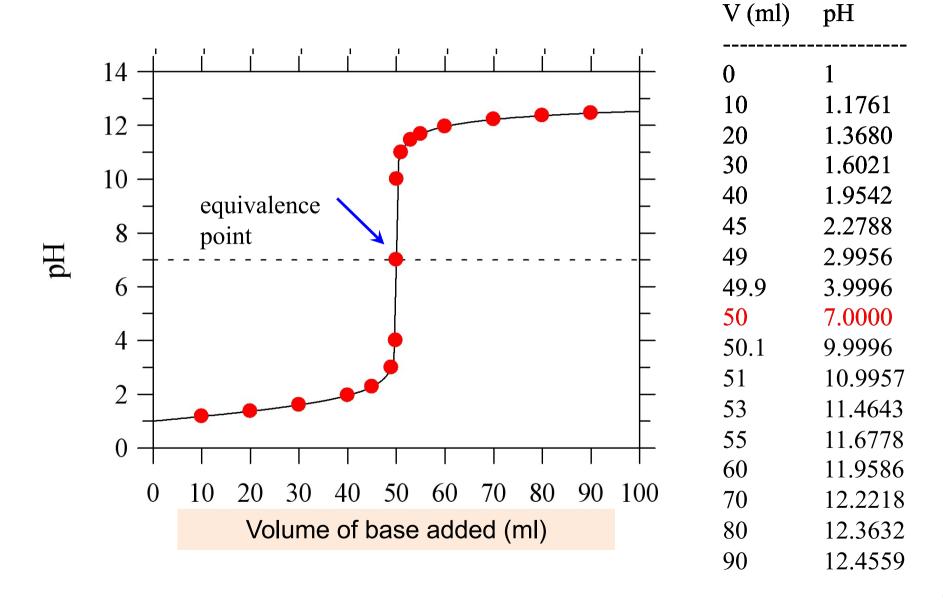
$$n_{B} = c_{B} \cdot V_{\text{added}}$$

- as long asn_A > n_B $[H_3O^+] = \frac{n_A n_B}{V_{\text{iniziala}} + V_{\text{againnto}}} = \frac{c_A \cdot V_{\text{iniziala}} c_B \cdot V_{\text{againnto}}}{V_{\text{iniziala}} + V_{\text{againnto}}}$
- when $n_A = n_B$, the base has completely neutralized the acid and pH = 7 (equivalence point)
- from that point on, adding further amounts of the base will cause: $n_A < n_B$

$$[OH^{-}] = \frac{n_{B} - n_{A}}{V_{iniziale} + V_{aggiunto}} = \frac{c_{B} \cdot V_{aggiunto} - c_{A} \cdot V_{iniziale}}{V_{iniziale} + V_{aggiunto}}$$

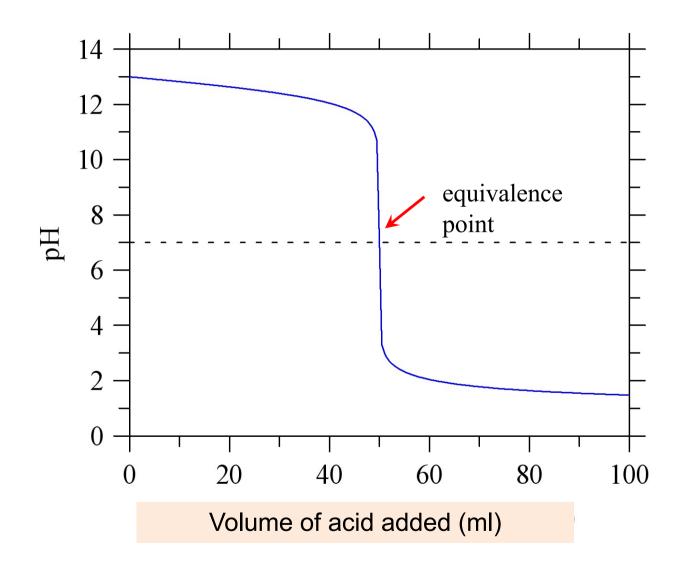
Titration of 50 ml di 0.1 M HCl with 0.1 M NaOH

 $HCl(aq) + NaOH(aq) \rightleftharpoons NaCl(aq) + H_2O(1)$



Titration of 50 ml of 0.1 M NaOH con 0.1 M HCl

NaOH (aq) + HCl (aq) \rightleftharpoons NaCl (aq)+ H₂O (l)



Problem: Calculate the pH of an aqueous soltion obtaine by mixing 40.0 g of NaOH (M = 40.0 g/mol) with 40.0 g of HBr (M = 80.9 g/mol) in a volume of solution of 1700 mL.

$$n_{\text{NAOH}} = \frac{40.0 \text{ g}}{40.0 \text{ g/mol}} = 1.0 \text{ mol}$$
 $n_{\text{NAOH}} = \frac{40.0 \text{ g}}{80.9 \text{ g/mol}} = 0.49 \text{ mol}$

Hydrobromic acid is present in a smaller quantity (0.49 moles), and will react completely to neutralize 0.49 moles of NaOH::

$$NaOH + HBr \rightarrow NaBr + H_2O$$

The number of moles of remaining NaOH will be:

$$n_{NaOH} = 1.0 - 0.49 = 0.51 \text{ mol}$$

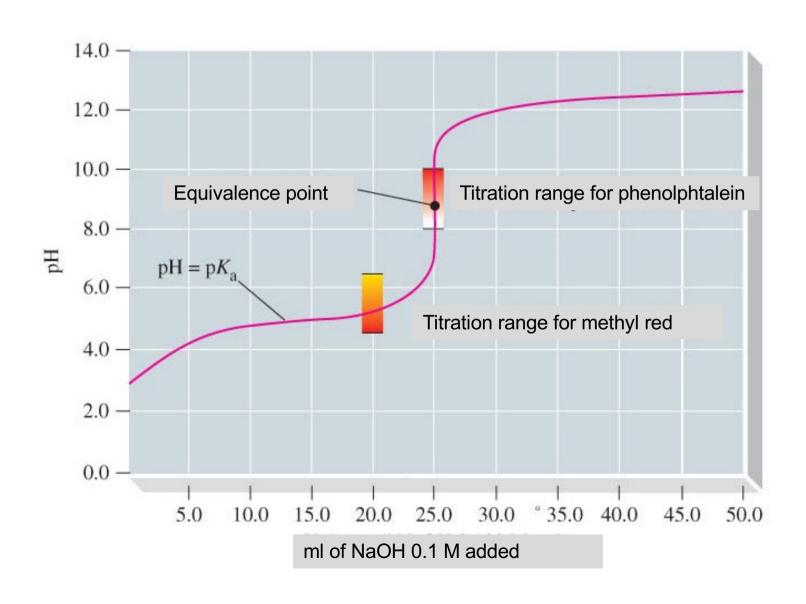
A concentration of:
$$c_{\text{NAOH}} = \frac{0.51 \text{ mol}}{1.7 \text{ L}} = 0.30 \text{ M}$$

We will obtain a 0.30 M solution of NaOH. $[OH^-] = 0.30$ M, with

$$pOH = -log_{10} 0.30 = 0.52$$
 therefore $pH = 14 - 0.52 = 13.5$

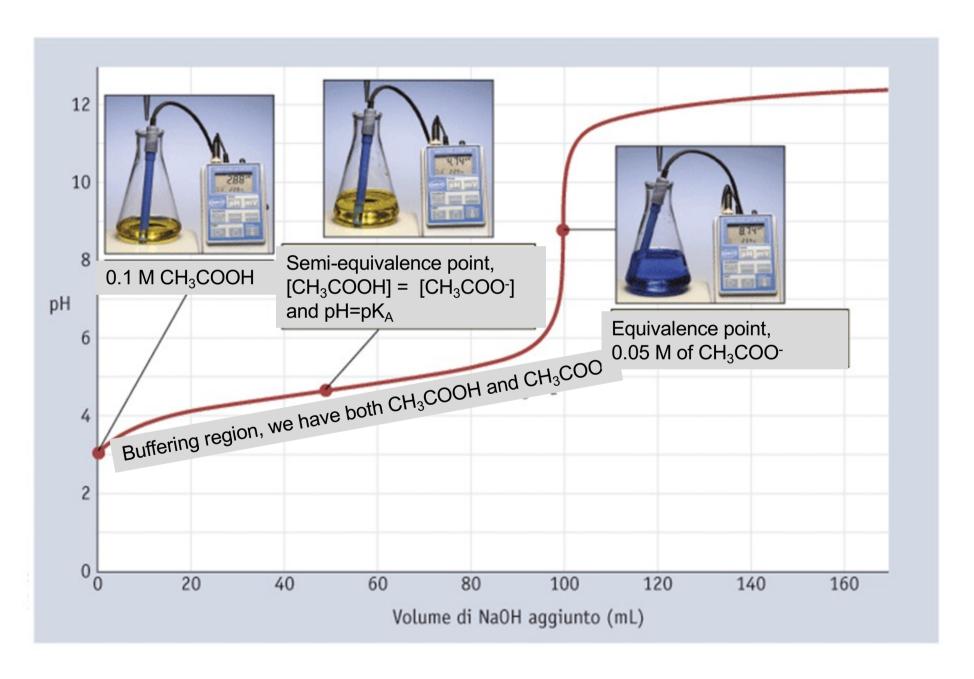
Titration of a weak acid with a strong base

The titration plot has a different shape. We report below the titration plot of 25ml of CH₃COOH 0.1M with NaOH 0.1M

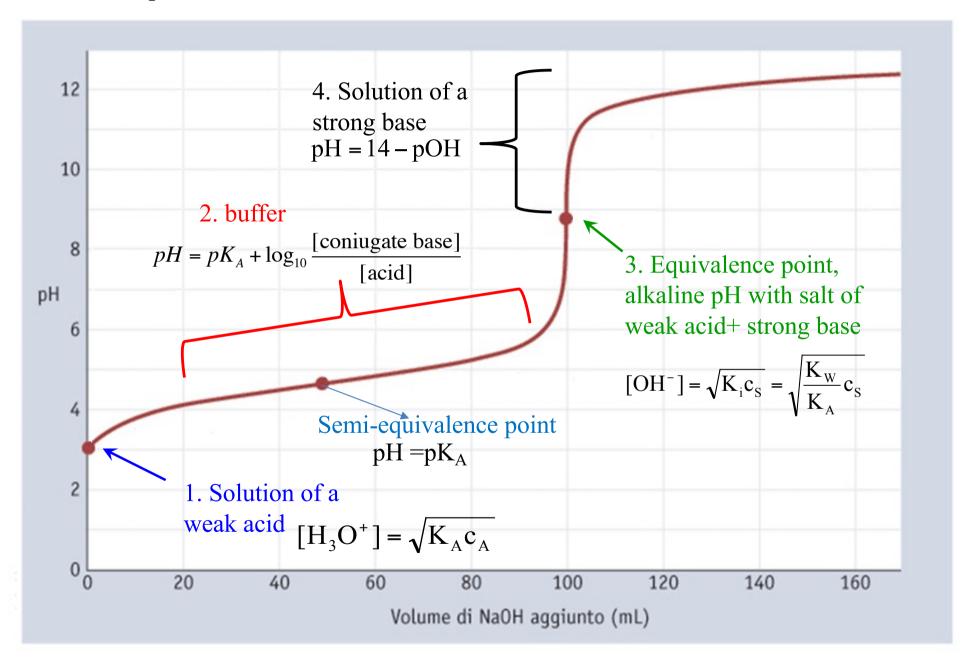


Titration of a weak acid with a strong base

100 ml of acetic acid 0.1 M with NaOH 0.1 M.



The titration curve can be divided in four regions, where we calculate pH with different equations:



Titration of a weak acid ($pK_A = 4$) with a strong base in the presence of an indicator

