



Microcosmo e Macrocosmo

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Lezioni della Cattedra Fermi

*23 Gennaio 2014
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Sapienza Università di Roma*

Friedman's equation

- Einstein's equation, in the case of a homogenous isotropic universe, gives

$$\left(\frac{\dot{a}}{a}\right)^2 = H_o^2 \left[\frac{\Omega_{Ro}}{a^4} + \frac{\Omega_{Mo}}{a^3} + \frac{(1-\Omega_o)}{a^2} + \Omega_{\Lambda} \right]$$

- The solution $a(t)$ tells us how all the distances in the universe evolve with time (i.e. how the universe expands).
- To find the solution, we need to find empirically the mass energy densities ρ_{Ro} , ρ_{Mo} , ρ_{Λ} and from them the parameters Ω_{Ro} , Ω_{Mo} , Ω_{Λ}

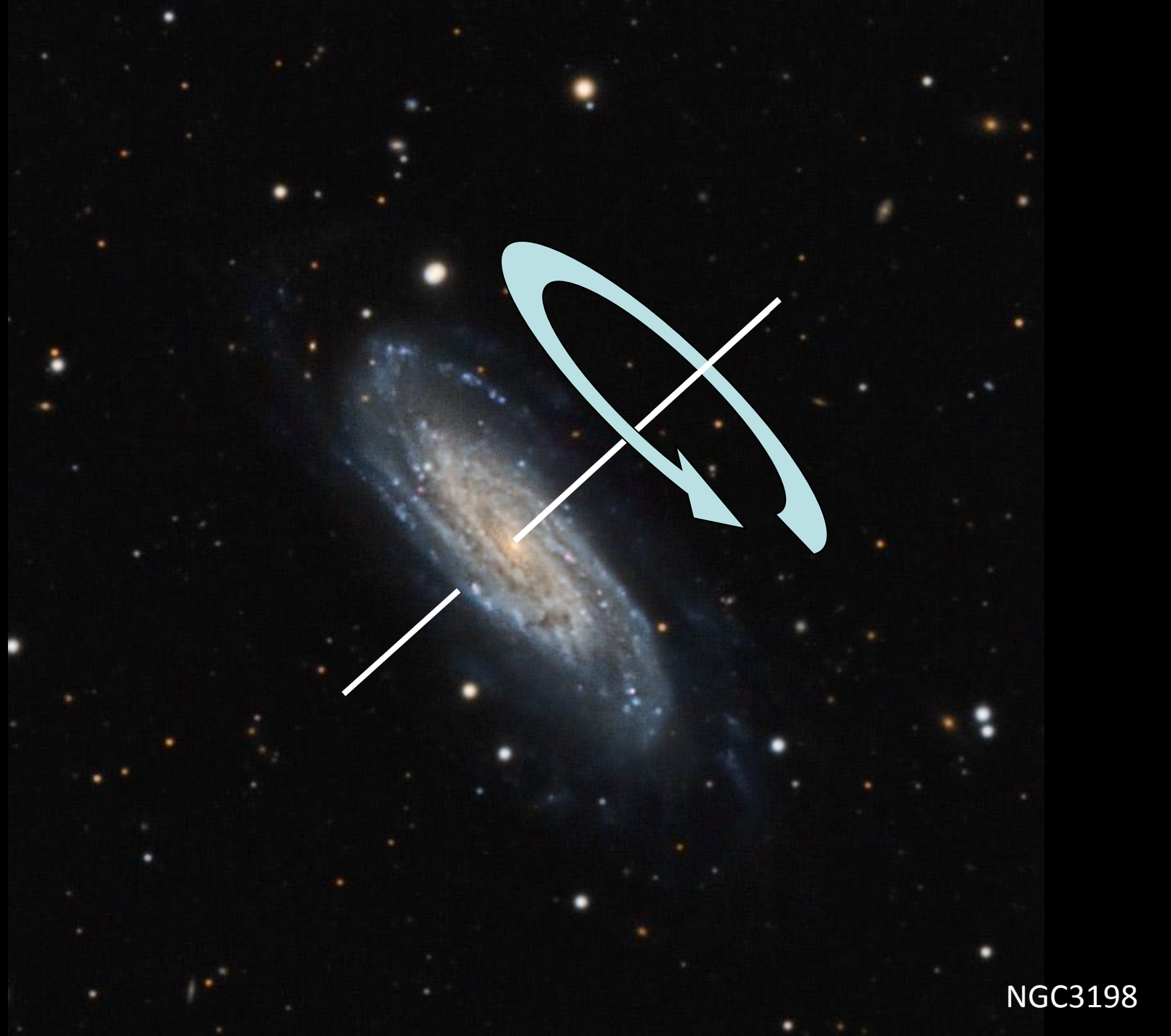
Dark Matter

- Dark matter does not interact electromagnetically.
- We can measure it only through its gravitational interaction, which is much weaker than electromagnetic.
- The dynamics of stars in galaxies and of galaxies in clusters of galaxies cannot be explained without the presence of dark matter
- Additional evidence comes from gravitational lensing and other effects.

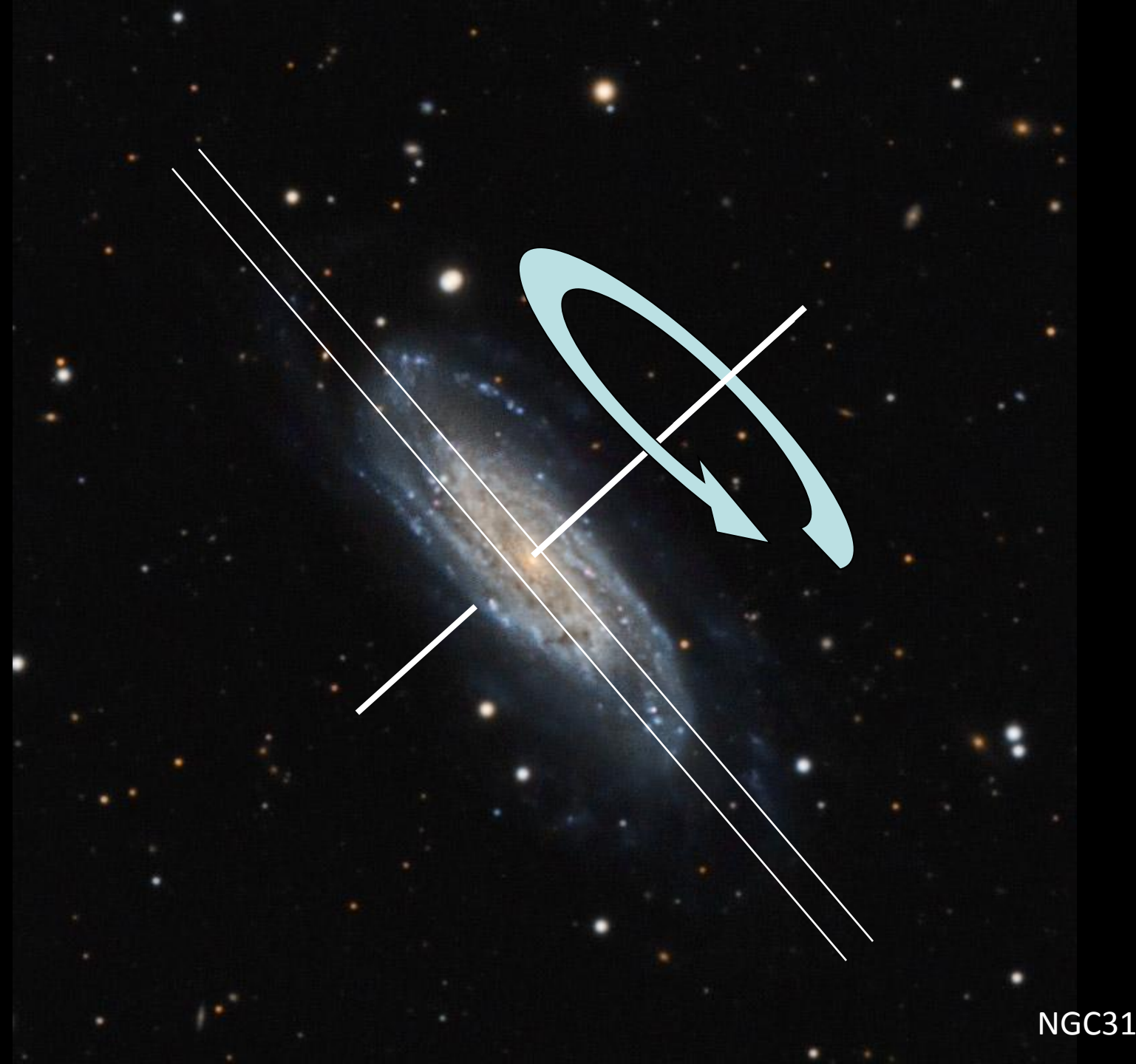
$$\Omega_{DMo} = (0.22 \pm 0.02)$$



NGC3198

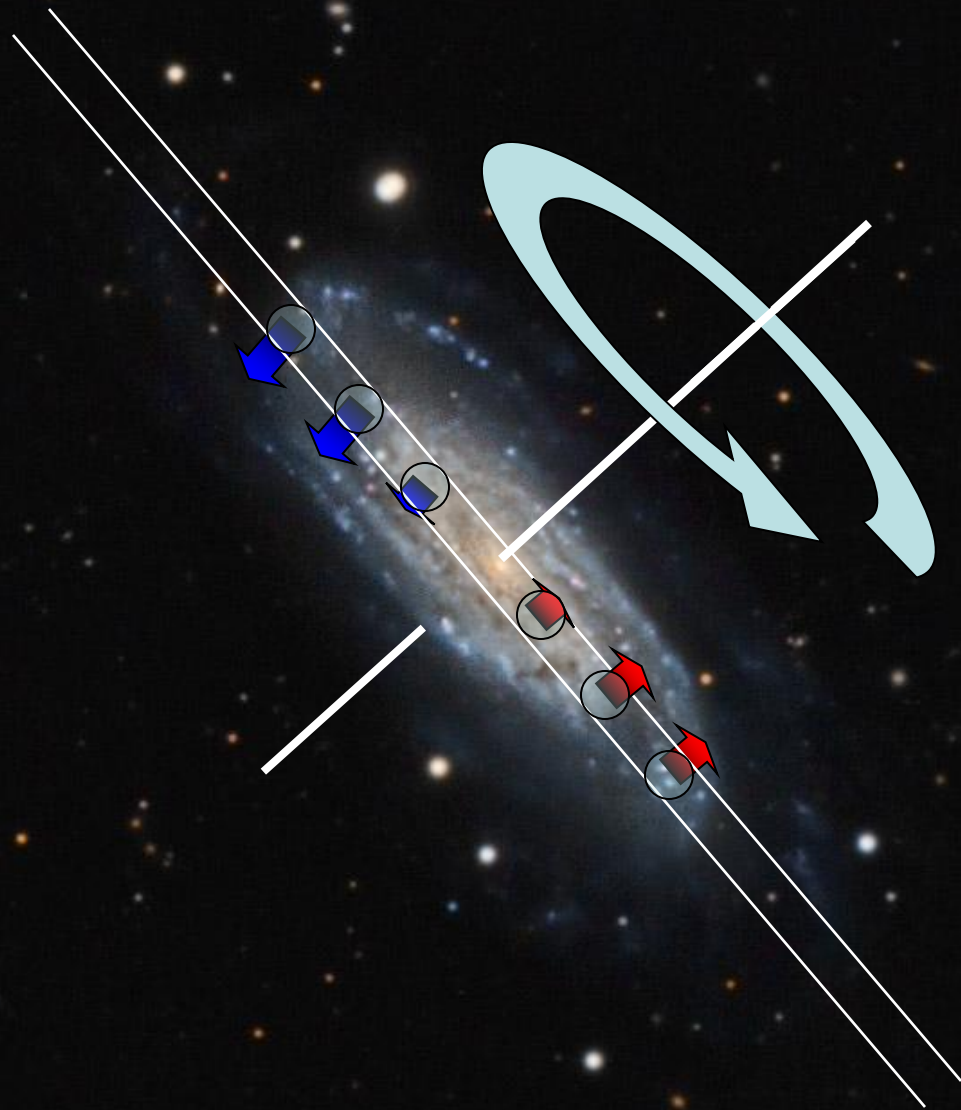


NGC3198

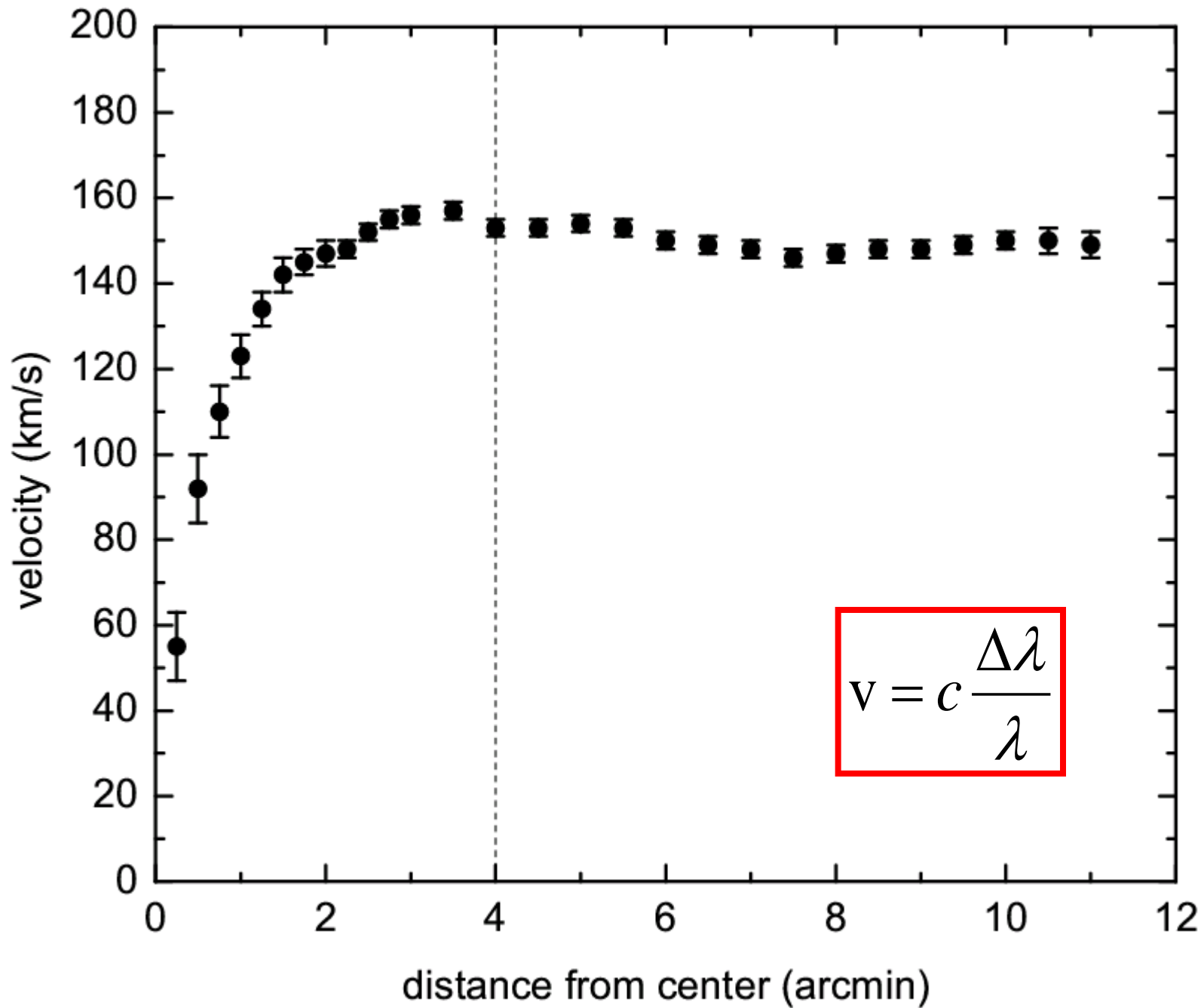


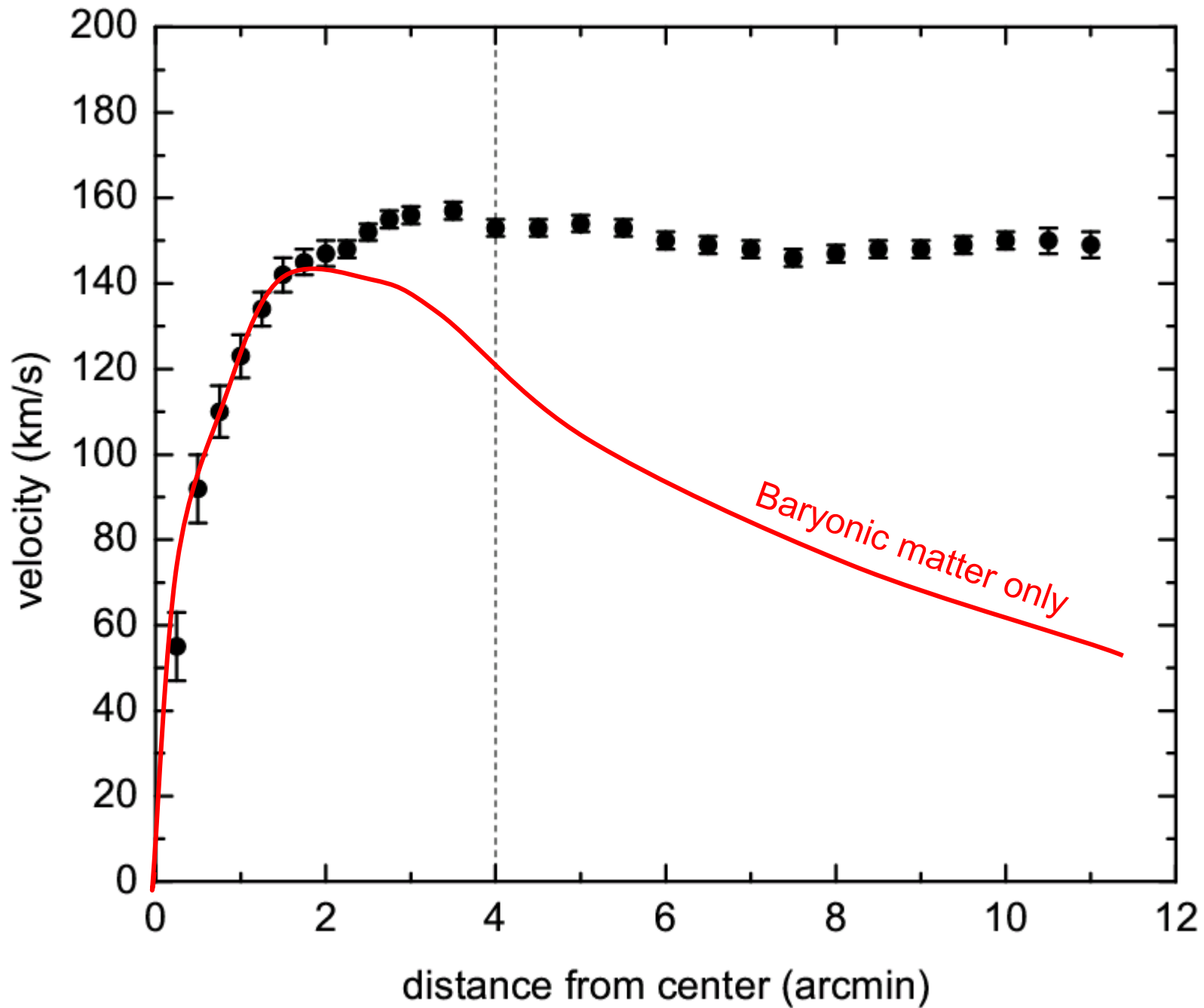
NGC3198

$$\frac{\Delta\lambda}{\lambda} = \frac{v}{c}$$



NGC3198

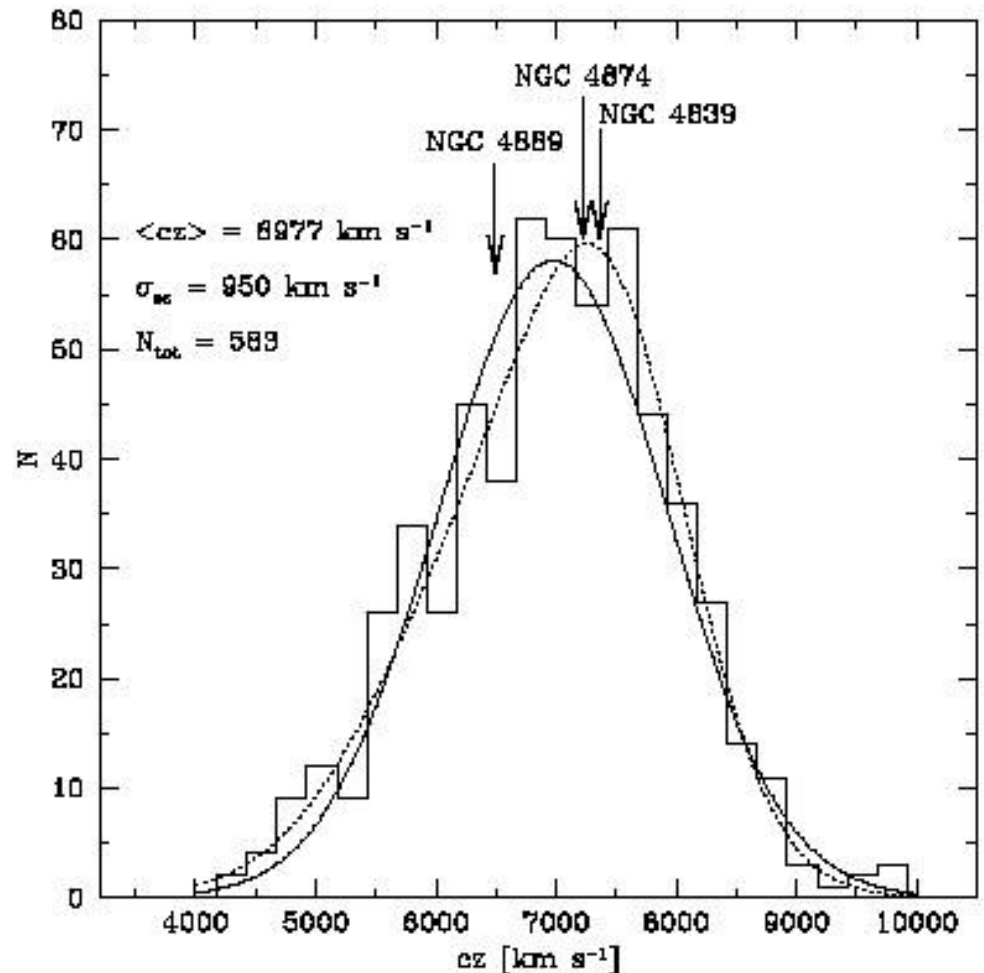


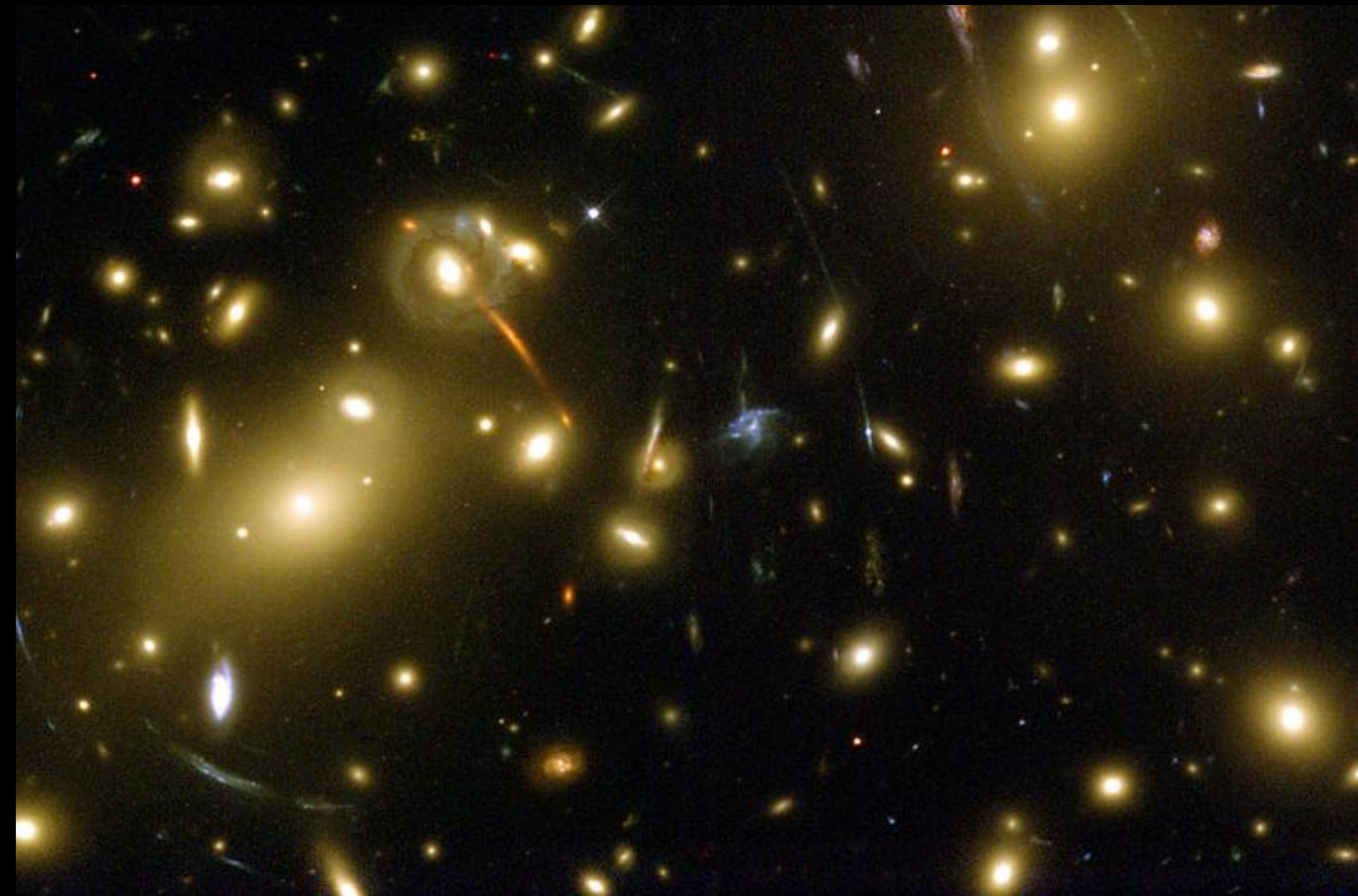




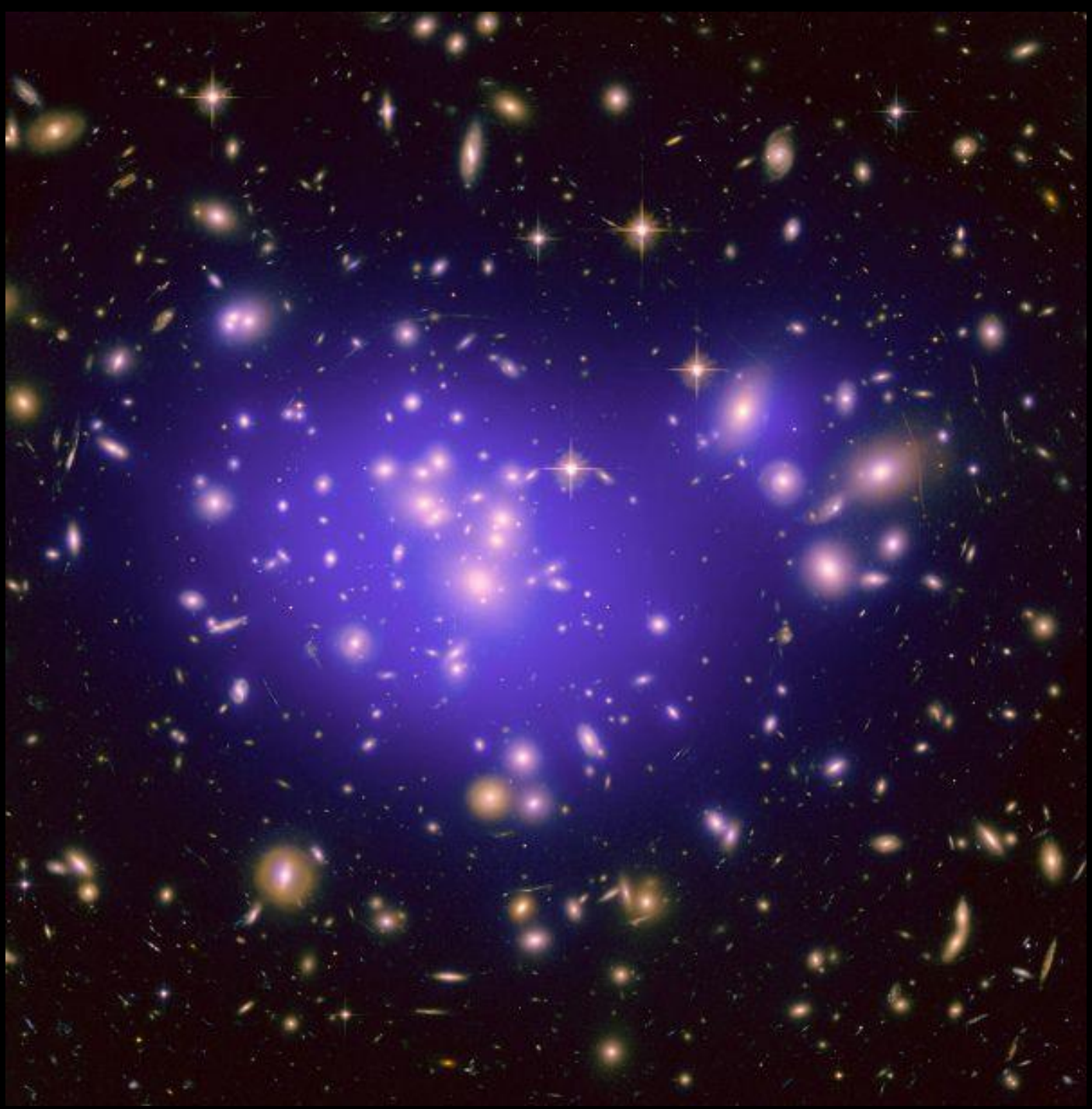
Coma

Figure 4.10— The distribution of radial velocities of all 583 identified Coma cluster galaxies ($4000 < cz < 10000 \text{ km s}^{-1}$). The solid curve is a Gaussian with mean $6977 \pm 53 \text{ km s}^{-1}$ and standard deviation $950 \pm 39 \text{ km s}^{-1}$. The dotted curve is the sum of two Gaussians with $\overline{cz}_1 = 7501 \pm 187 \text{ km s}^{-1}$, $\sigma_1 = 650 \pm 216 \text{ km s}^{-1}$ and $\overline{cz}_2 = 6640 \pm 470 \text{ km s}^{-1}$, $\sigma_2 = 1004 \pm 120 \text{ km s}^{-1}$ and gives a better fit to the observed distribution. The radial velocities of the three dominant galaxies are indicated.





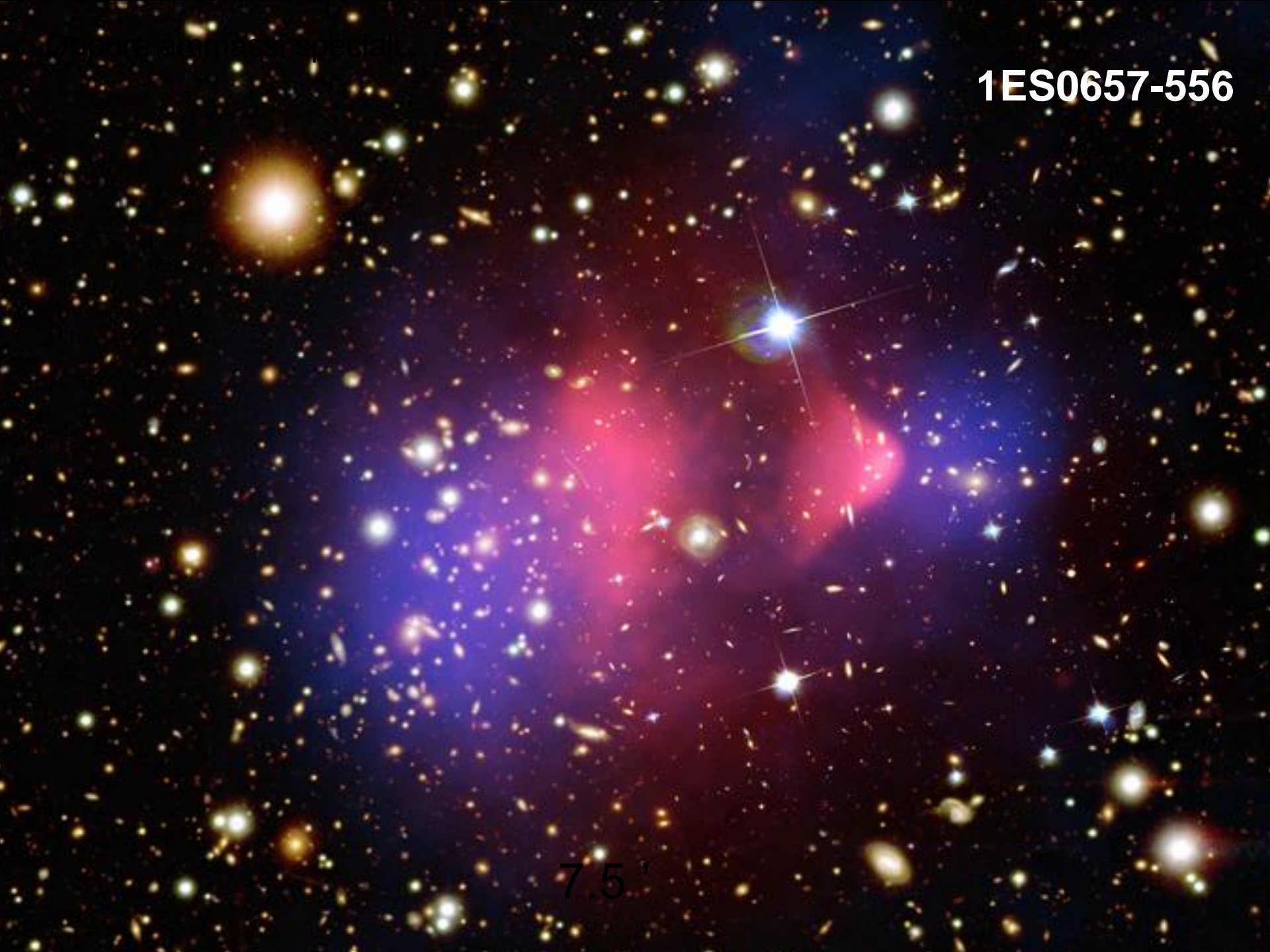
A2218

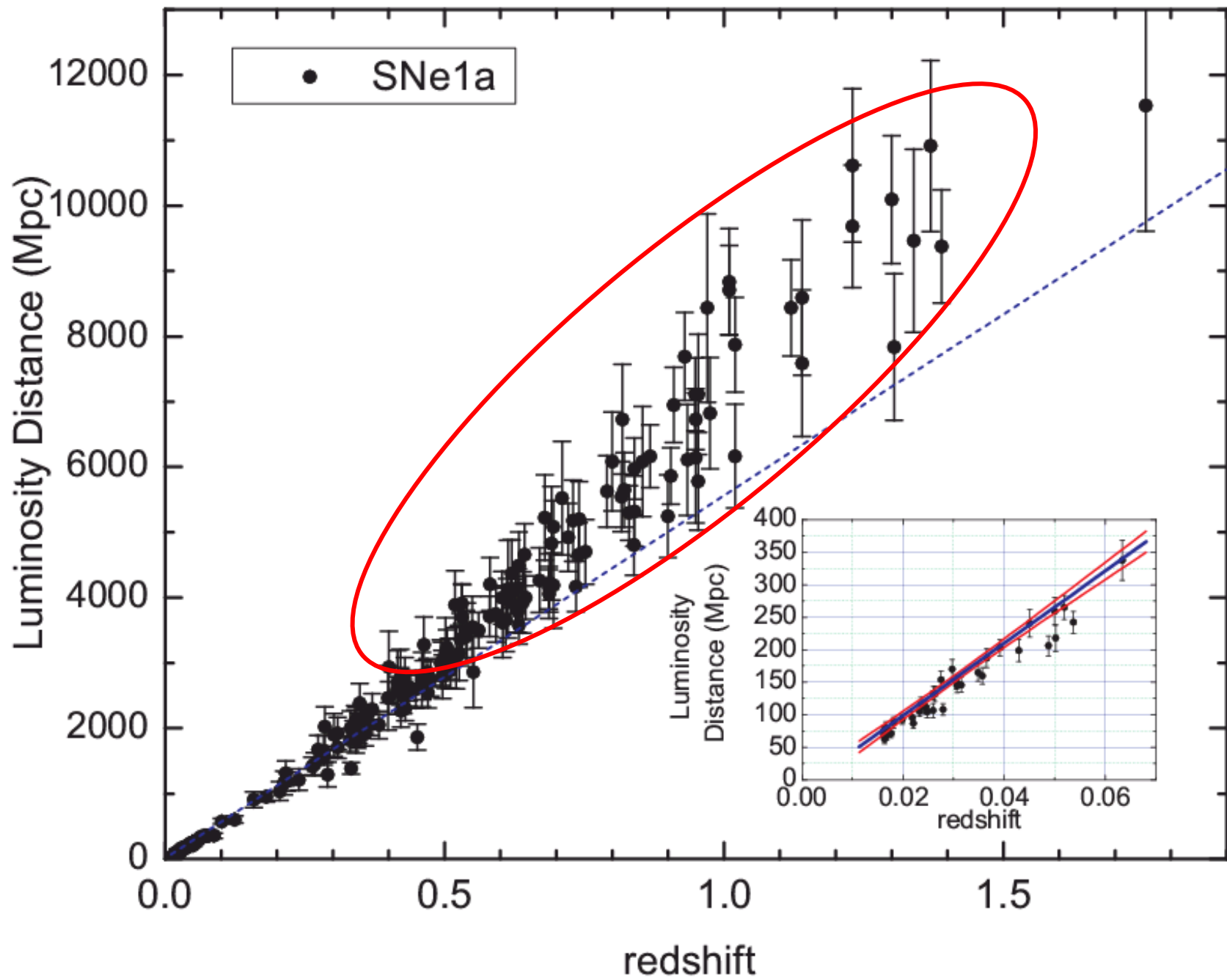


A1689

1ES0657-556

7.5'





Dark Energy

- Systematic weakness of distant (high redshift) SNe1a
- Can be explained by an accelerated expansion of the universe, so that they are more distant for a given redshift.
- From Friedman's equation, the only way is to have $\Omega_{\Lambda} > 0$.

$$\ddot{a} = H_o^2 \left[-\frac{\Omega_{Ro}}{a^3} - \frac{1}{2} \frac{\Omega_{Mo}}{a^2} + \Omega_{\Lambda} a \right]$$

- The best fit is $\Omega_{\Lambda} = (0.73 \pm 0.03)$
- This can be obtained from independent measurements as well (CMB, see below)

Radiation

- Light and electromagnetic waves fill the universe.
- Stellar radiation is not the most important radiation field present in the universe, since it dilutes far from stars.
- The cosmic microwave background is a perfect blackbody with a temperature $T_0=2.725\text{K}$ filling the whole universe, so dominating over stellar and any other radiation at large scales.
- Its density today is negligible: $\Omega_{Ro} < 10^{-4}$
- However, early in the evolution of the universe, it dominated the energy density. In principle, it was light.

$$\left(\frac{\dot{a}}{a}\right)^2 = H_o^2 \left[\frac{\Omega_{Ro}}{a^4} + \frac{\Omega_{Mo}}{a^3} + \frac{(1-\Omega_o)}{a^2} + \Omega_\Lambda \right]$$

Density Parameter

- The total mass-energy density is the sum of all the components analyzed above.

$$\Omega_o = \Omega_{Ro} + \Omega_{Mo} + \Omega_{DMo} + \Omega_{\Lambda} \approx 1$$

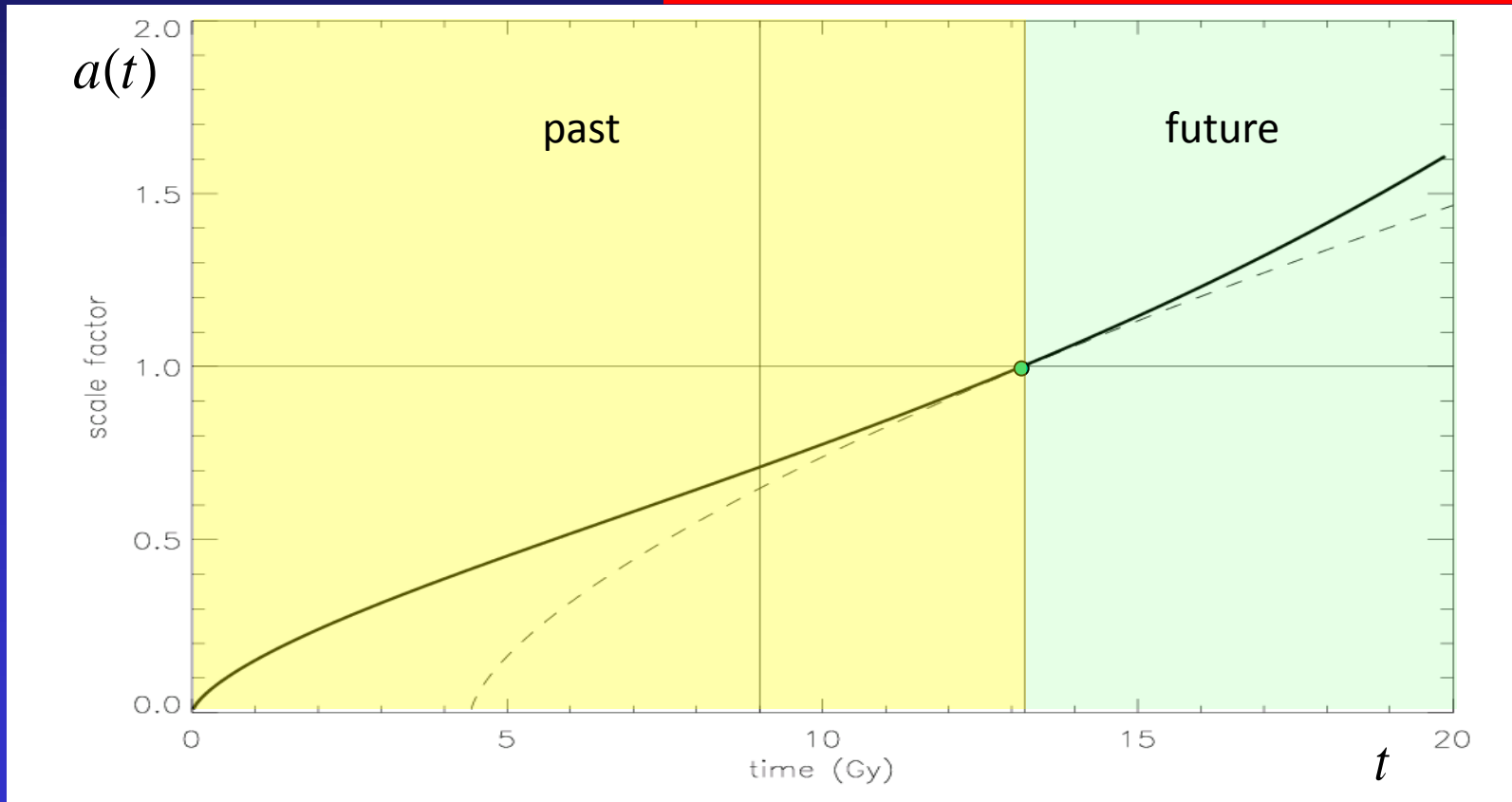
- I.e. the mass-energy density is consistent with the critical density, and there is no curvature of space.
- This result is confirmed and its accuracy is improved by measurements of the causal horizon at redshift 1100, using the cosmic microwave background:

$$\Omega_o = (1.02 \pm 0.02)$$

Friedman's equation

- We know all the parameters, so we can solve the equation:

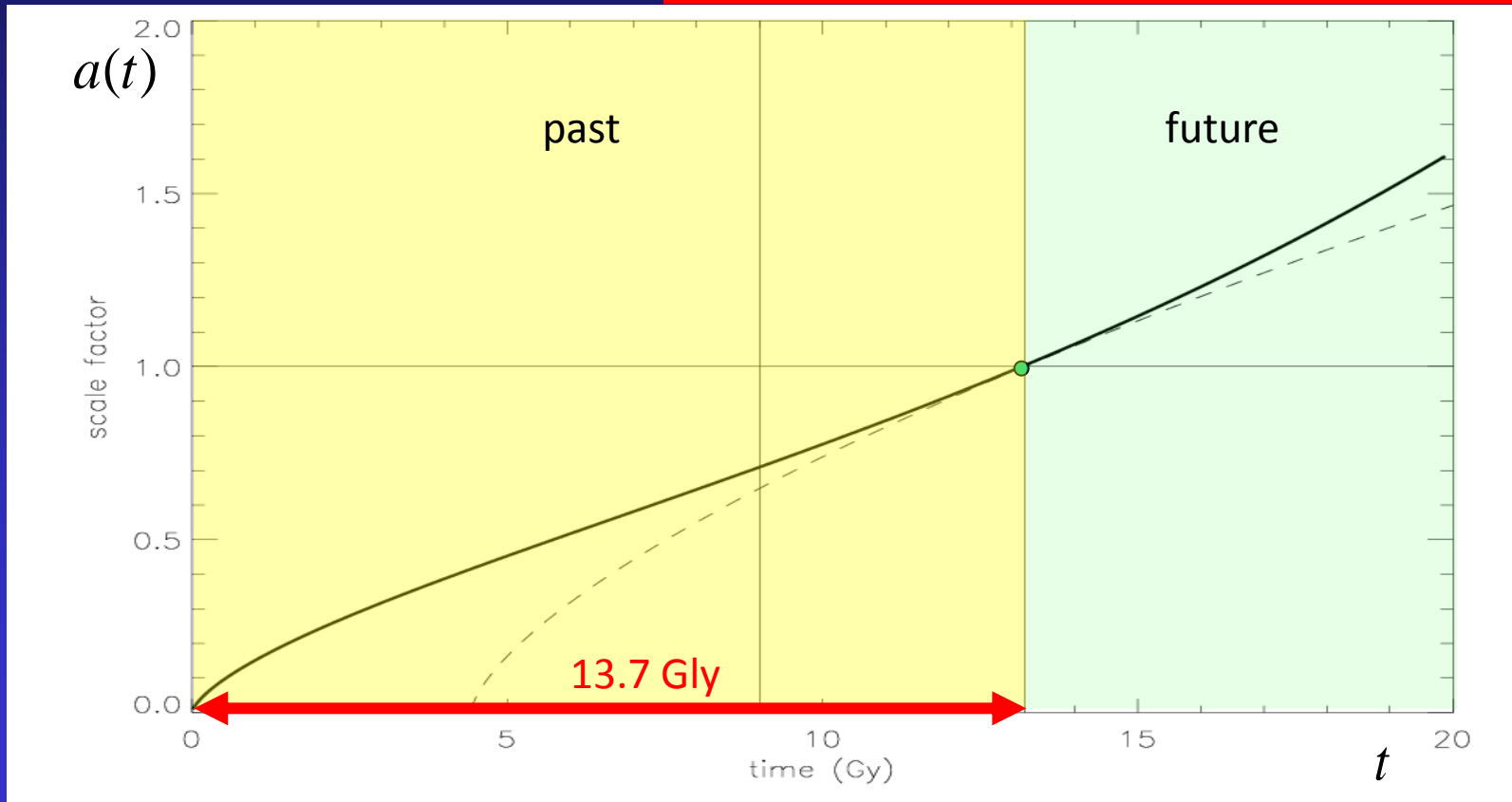
$$\left(\frac{\dot{a}}{a}\right)^2 = H_o^2 \left[\frac{\Omega_{Ro}}{a^4} + \frac{\Omega_{Mo}}{a^3} + \frac{(1-\Omega_o)}{a^2} + \Omega_{\Lambda} \right]$$



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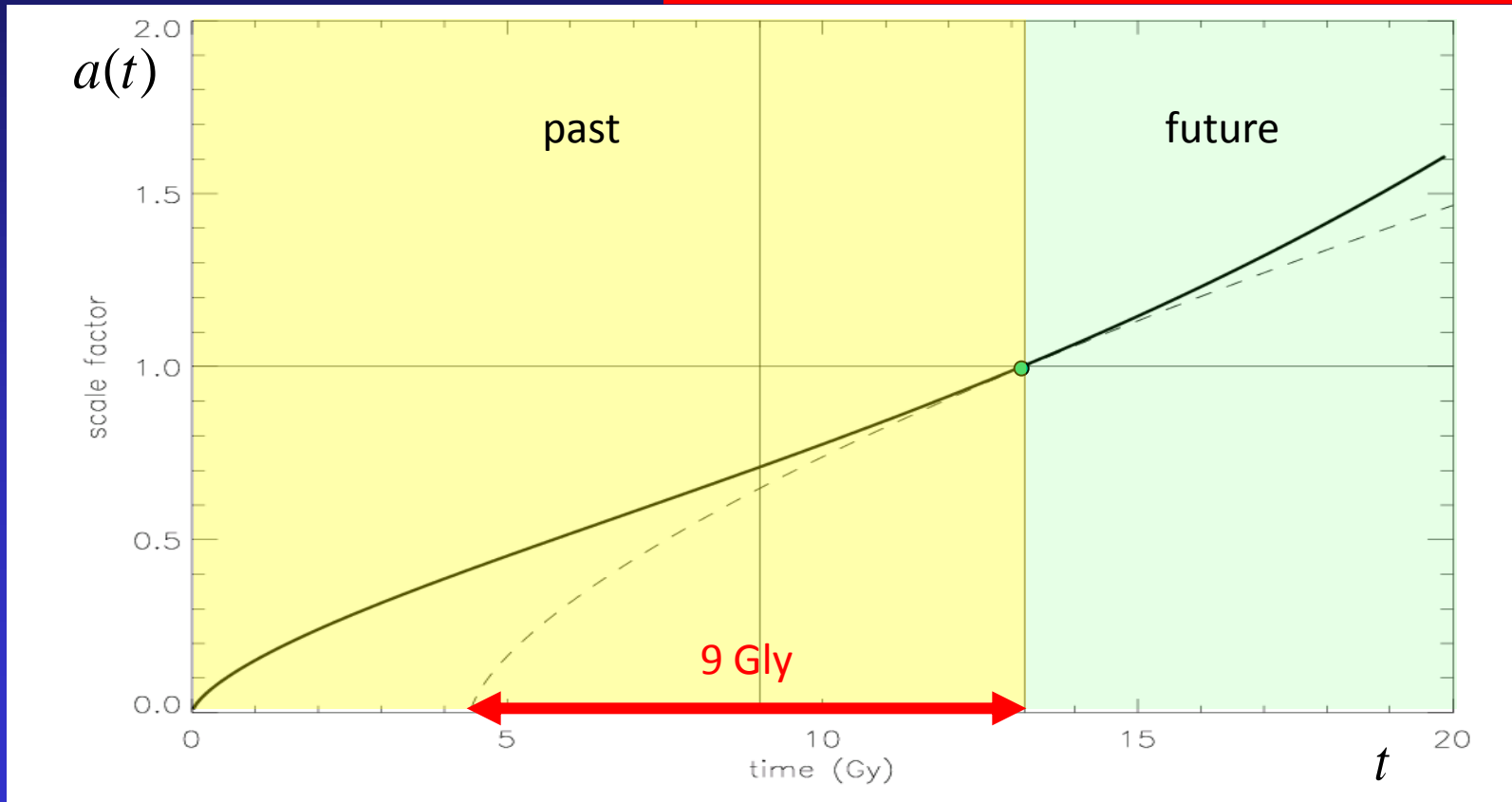
$$\left(\frac{\dot{a}}{a}\right)^2 = H_o^2 \left[\frac{\Omega_{Ro}}{a^4} + \frac{\Omega_{Mo}}{a^3} + \frac{(1-\Omega_o)}{a^2} + \Omega_{\Lambda} \right]$$



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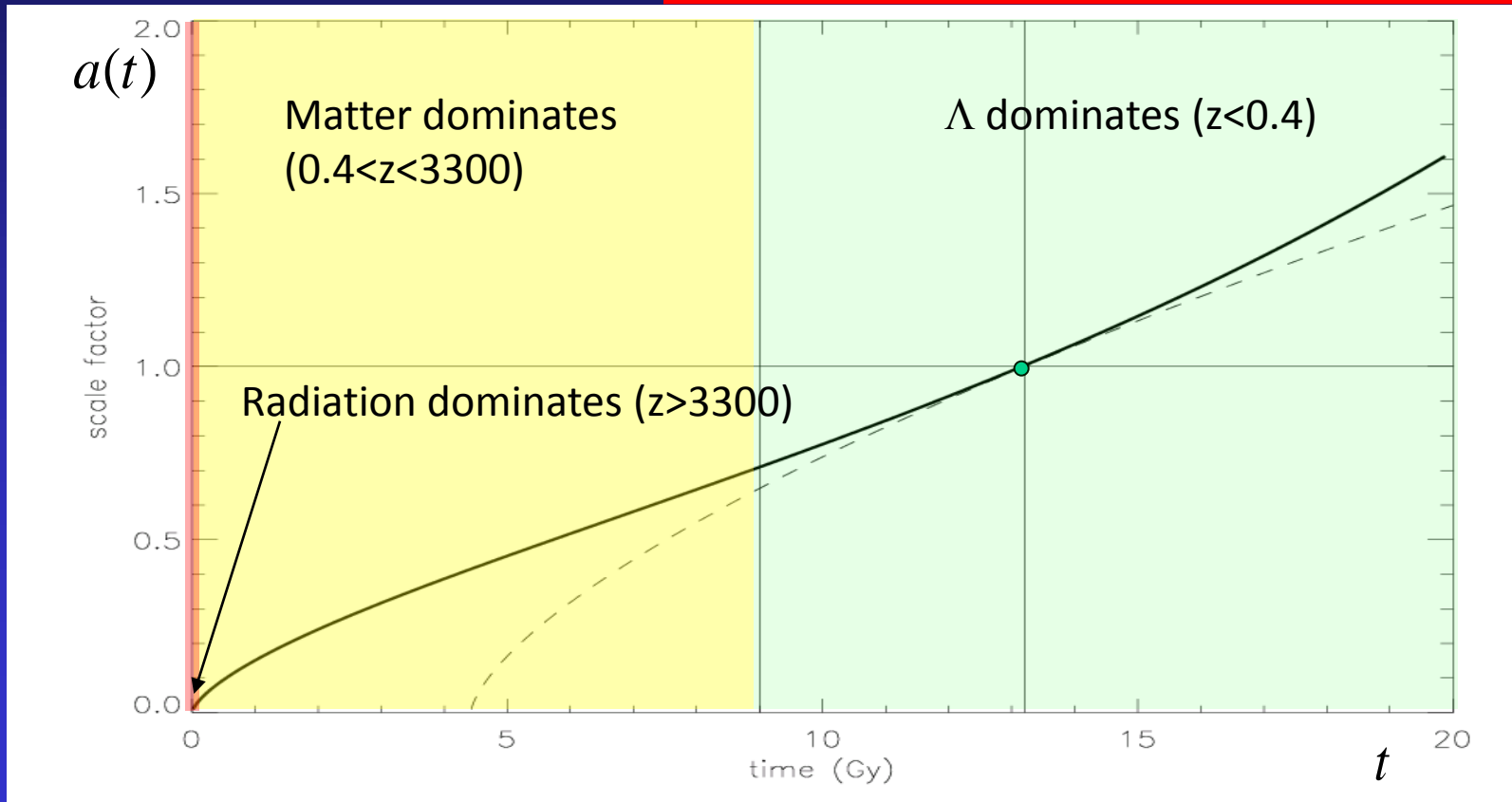


NGC 6397

Friedman's equation

- We know all the parameters, so we can solve the equation:

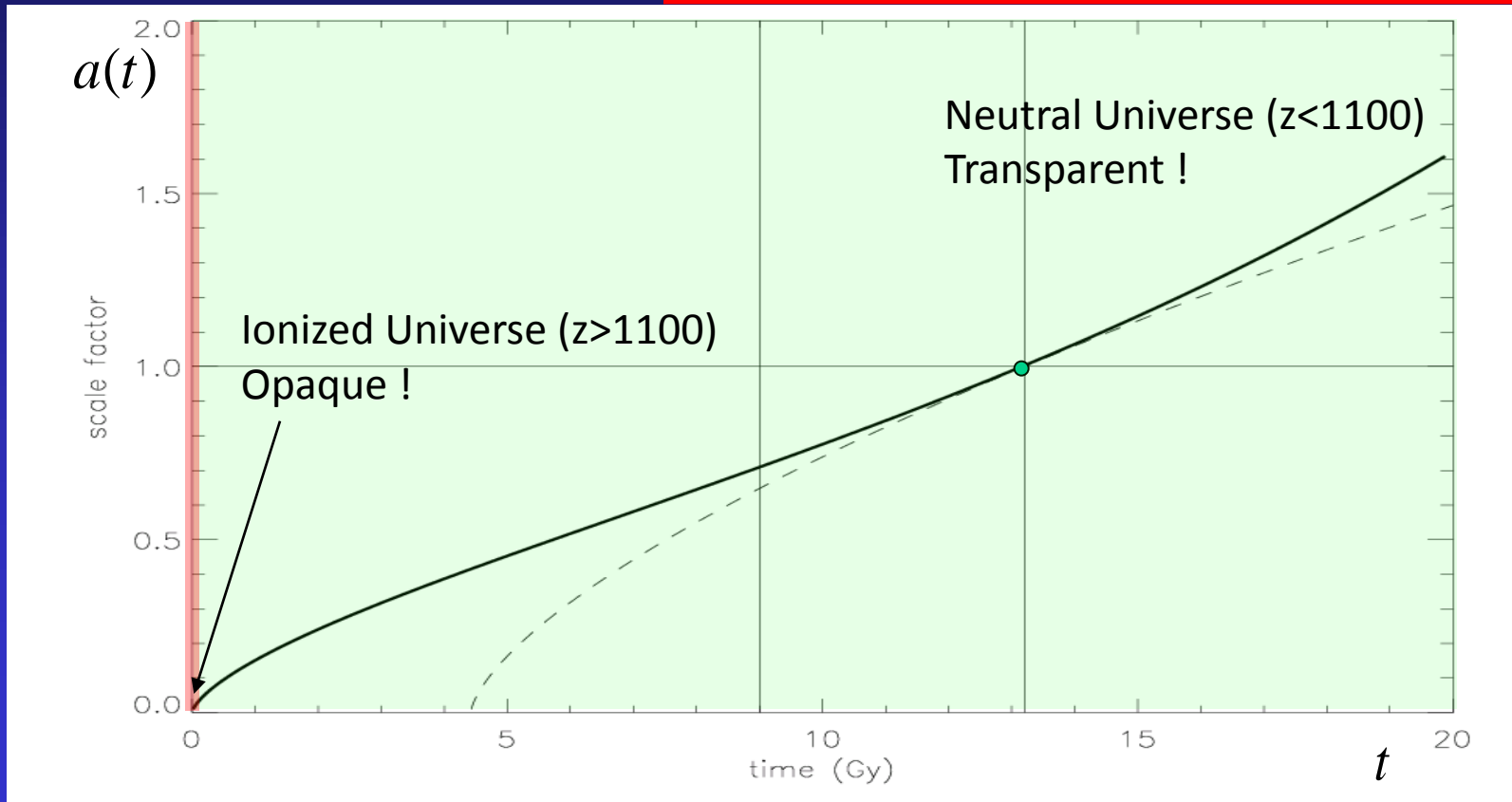
$$\left(\frac{\dot{a}}{a}\right)^2 = H_o^2 \left[\frac{\Omega_{Ro}}{a^4} + \frac{\Omega_{Mo}}{a^3} + \frac{(1-\Omega_o)}{a^2} + \Omega_\Lambda \right]$$

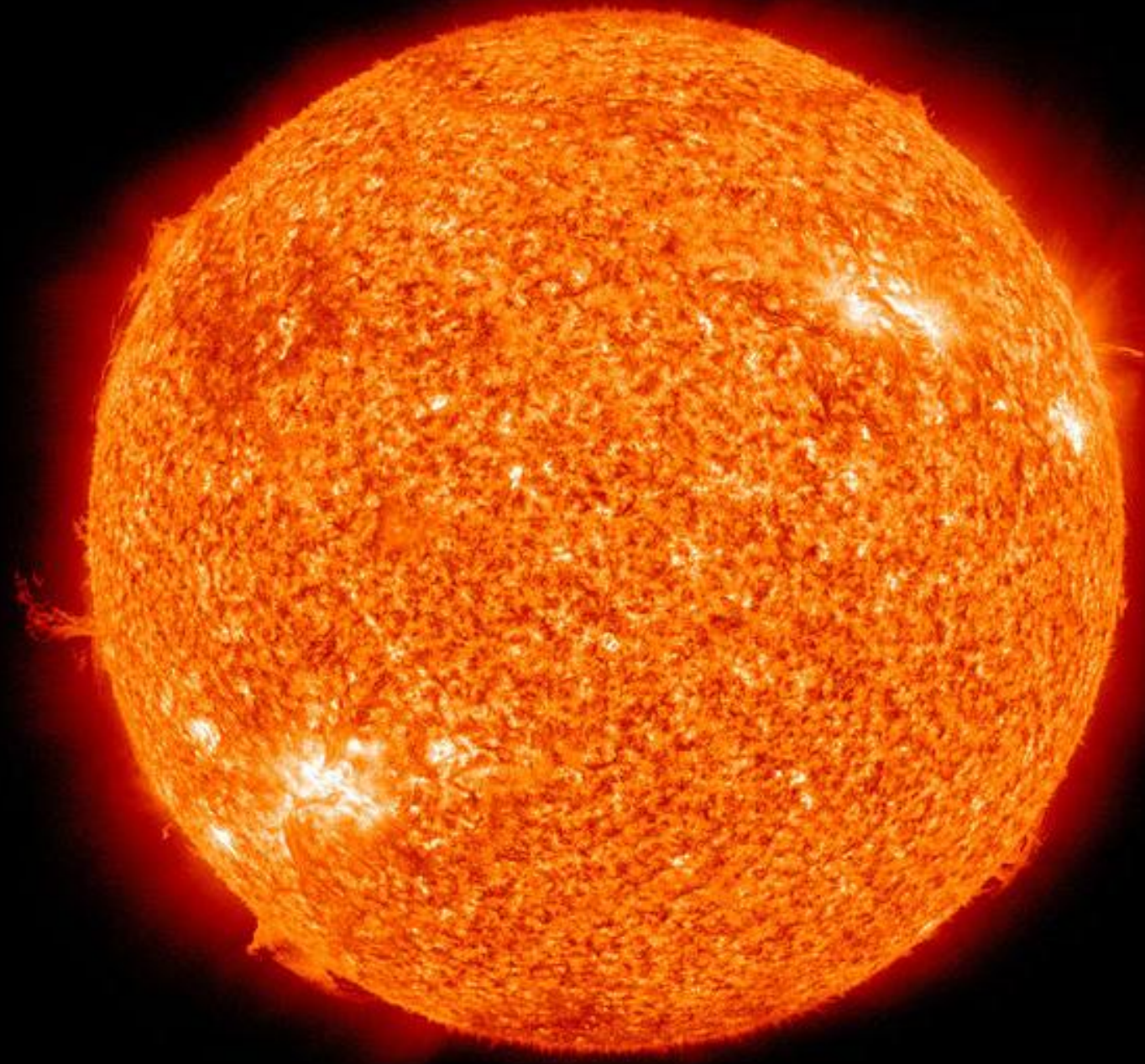


Friedman's equation

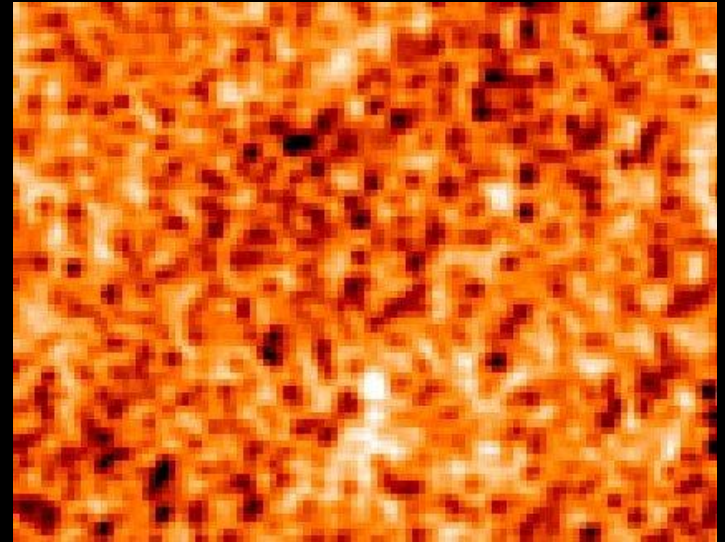
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$$\left(\frac{\dot{a}}{a}\right)^2 = H_o^2 \left[\frac{\Omega_{Ro}}{a^4} + \frac{\Omega_{Mo}}{a^3} + \frac{(1-\Omega_o)}{a^2} + \Omega_{\Lambda} \right]$$





Granulazione solare



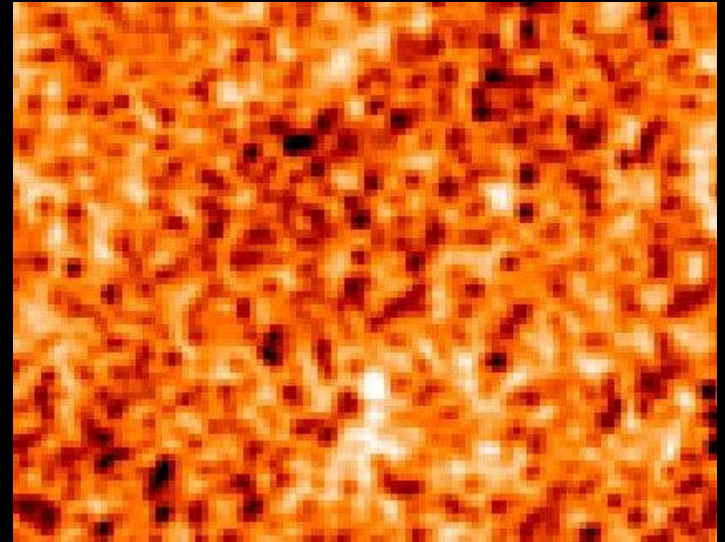
Gas incandescente
sulla superficie del
Sole (5500 K)

8 minuti luce



Qui, ora

Granulazione solare



Gas incandescente
sulla superficie del
Sole (5500 K)

8 minuti luce

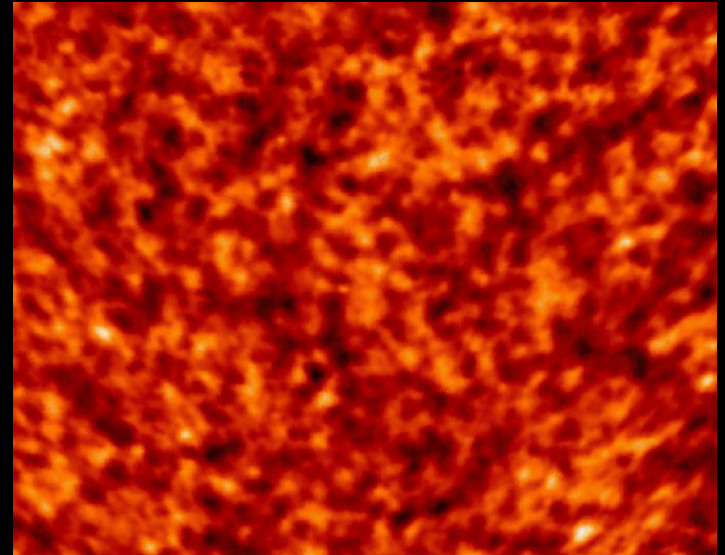
Qui, ora



Gas incandescente
nell' universo
primordiale (l'
universo diventa
trasparente a 3000 K)

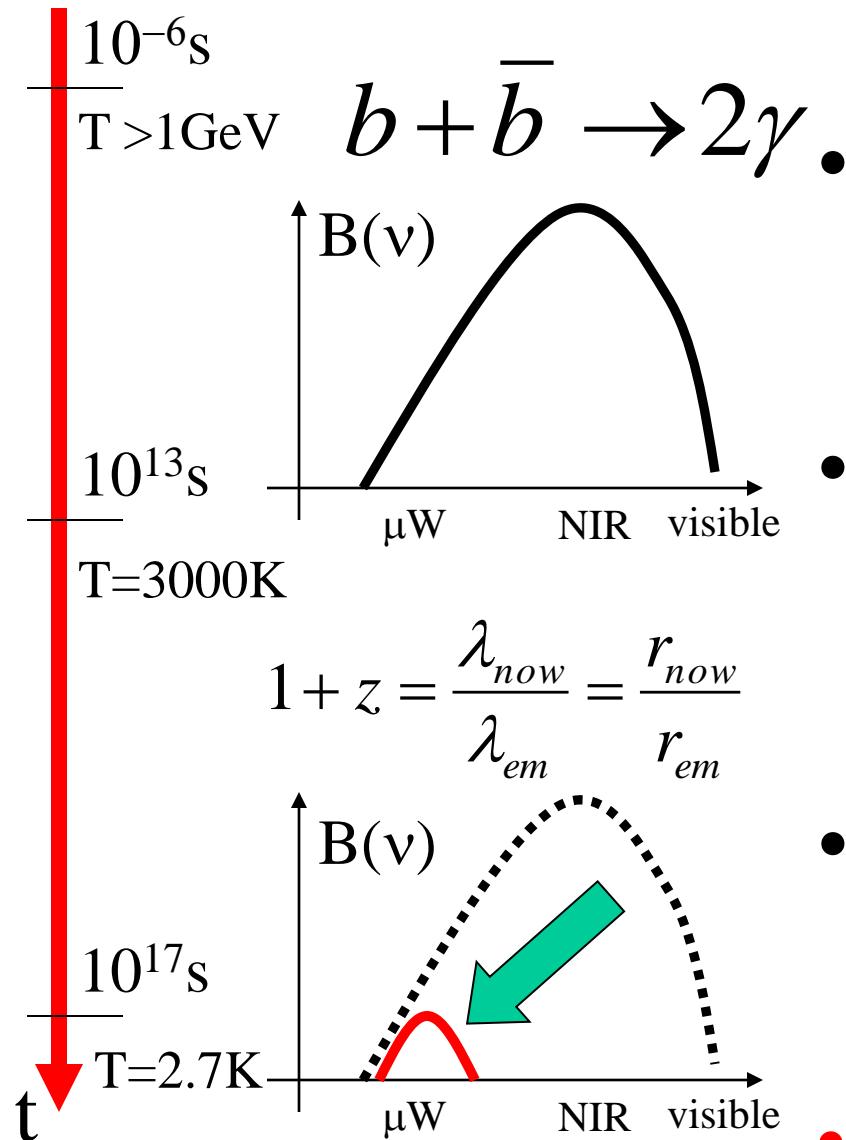
14 miliardi di anni luce

Qui, ora



Mappa di BOOMERanG dell' Universo Primordiale

What is the CMB

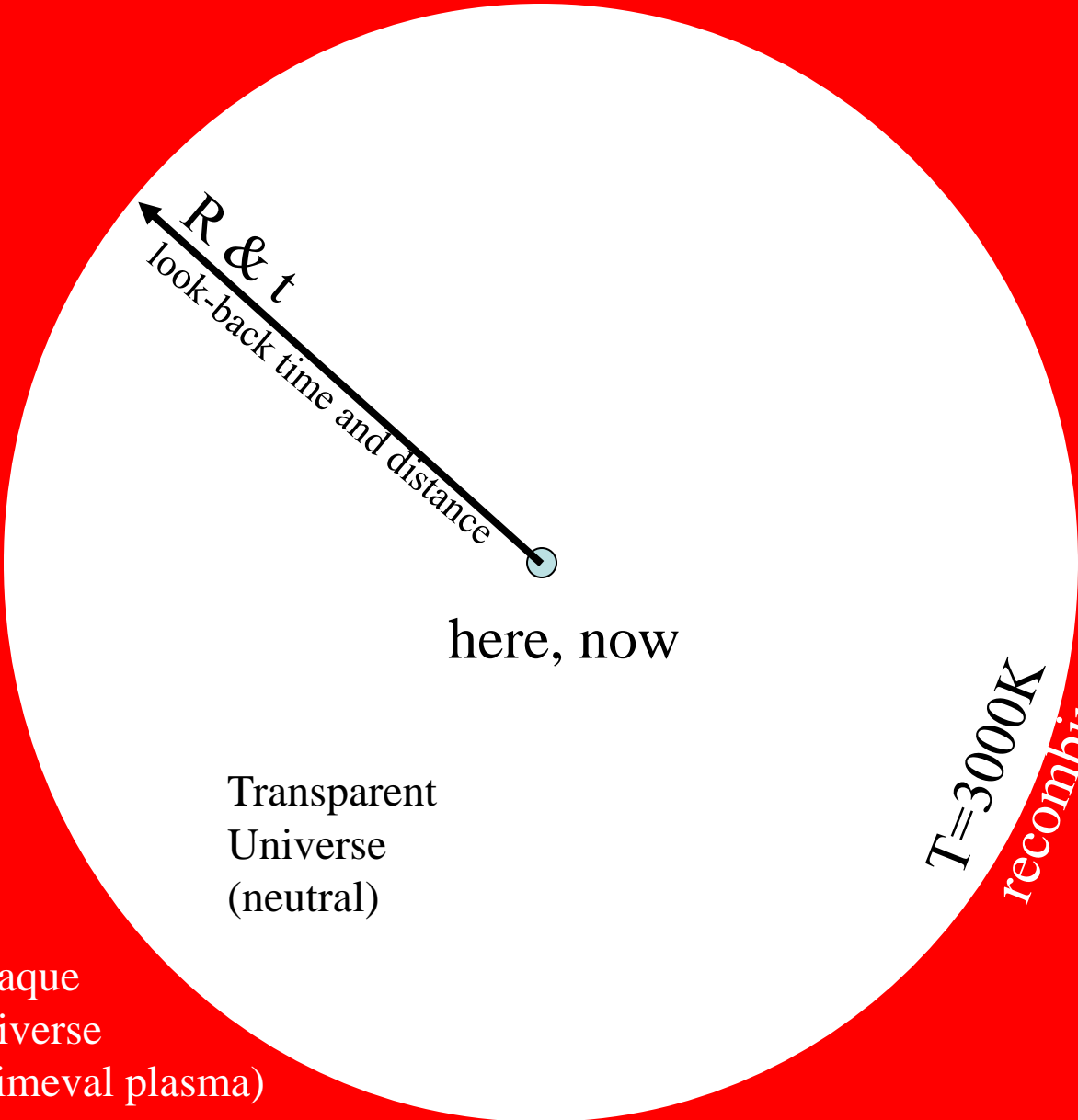


According to modern cosmology:

An abundant background of photons filling the Universe.

- **Generated** in the very early universe, less than $4 \mu\text{s}$ after the Big Bang ($10^9\gamma$ for each baryon)
- **Thermalized** in the primeval fireball (in the first 380000 years after the big bang) by repeated scattering against free electrons
- **Redshifted** to microwave frequencies **and diluted** in the subsequent 14 Gyrs of expansion of the Universe
- **Today: $410\gamma/\text{cm}^3$, $\sim 1 \text{ meV}$**

These photons carry
significant information
on the structure, evolution and
composition of our universe



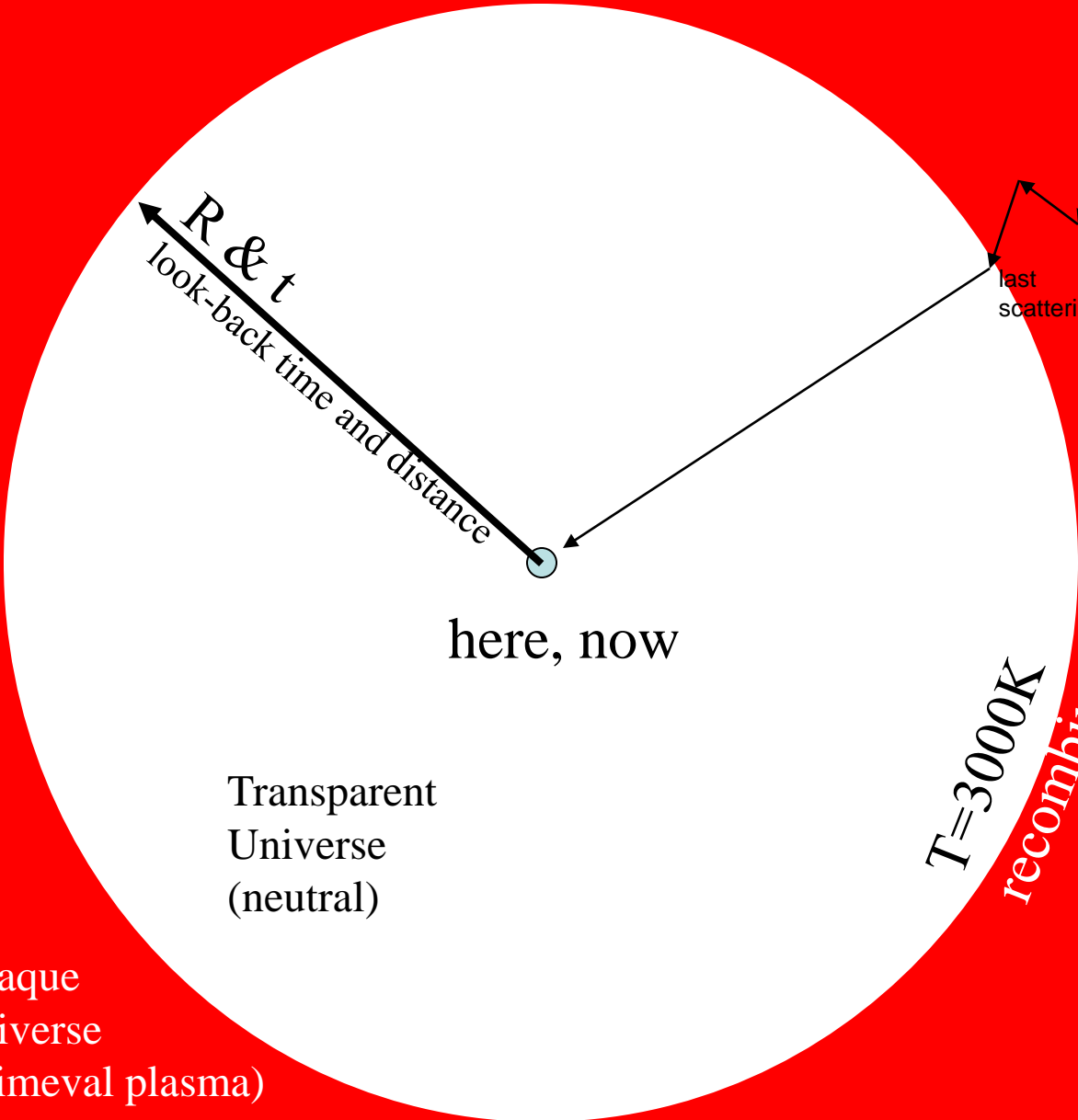
$R \ \& \ t$
look-back time and distance

here, now

Transparent
Universe
(neutral)

$T=3000K$
recombination

Opaque
Universe
(primeval plasma)



$R \ \& \ t$
look-back time and distance

here, now

last scattering

Transparent
Universe
(neutral)

$T=3000K$

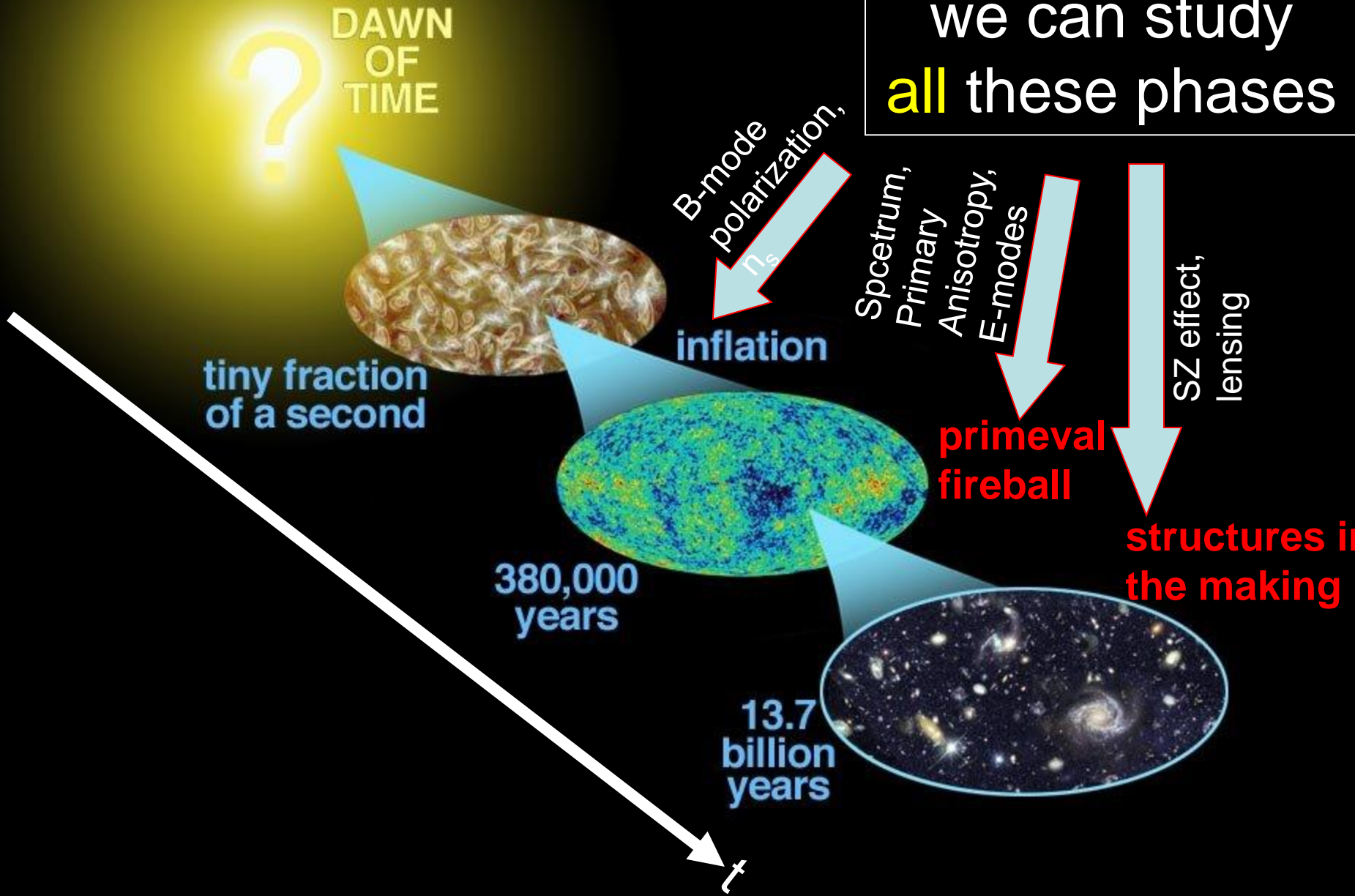
recombination

Opaque
Universe
(primeval plasma)

The spectrum

- CMB photons are produced when matter and radiation are in tight thermal equilibrium (Thomson scattering in the primeval plasma)
- The spectrum of the CMB has to be a **blackbody**.
- The expansion of the universe preserves the shape of a blackbody spectrum, while its temperature decreases as the inverse of the scale factor.
- Measuring a blackbody spectrum of the CMB, we can prove the existence of a primeval fireball phase of the universe.
- To be consistent with the primordial abundance of light elements, a temperature of **a few K** is expected (Gamow)

with CMB data
we can study
all these phases



CMB anisotropy (intrinsic)

- Different physical effects, all related to the *small* density fluctuations $\delta\rho / \rho$ present 380000 yrs after the big bang (recombination) produce CMB Temperature fluctuations:

$$\frac{\delta T}{T} = \frac{1}{3} \frac{\delta\phi}{c^2} + \frac{1}{4} \frac{\delta\rho_\gamma}{\rho_\gamma} - \frac{\vec{v}}{c} \cdot \vec{n}$$

Sachs-Wolfe
(gravitational
redshift)

Photon
density
fluctuations

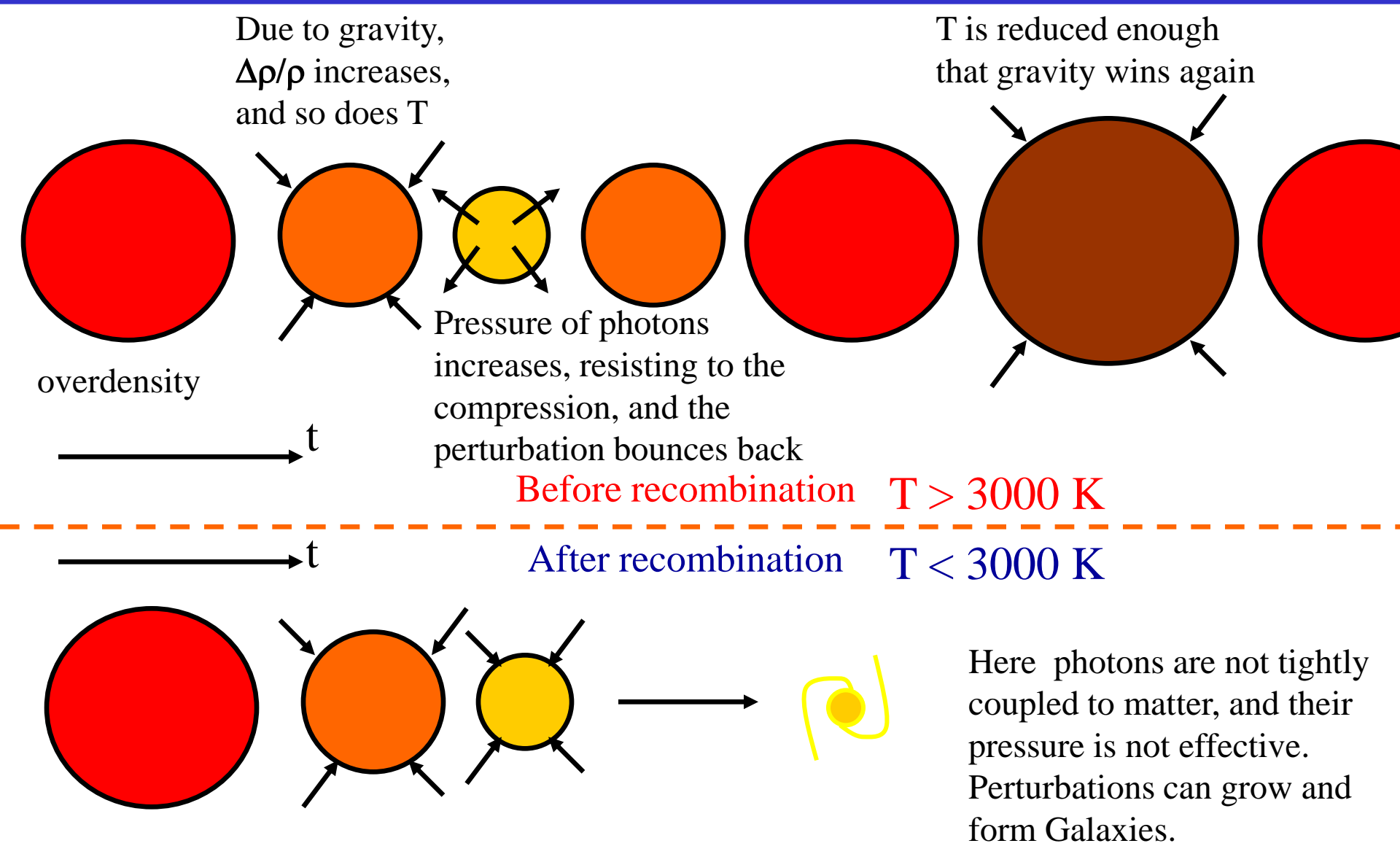
Doppler effect
from velocity
fields

- Scales larger than the horizon are basically frozen in the pre-recombination era. Flat power spectrum of $\delta T/T$ at large scales.
- Scales smaller than the horizon undergo acoustic oscillations during the primeval fireball. Acoustic peaks in the power spectrum of $\delta T/T$ at sub-degree scales.

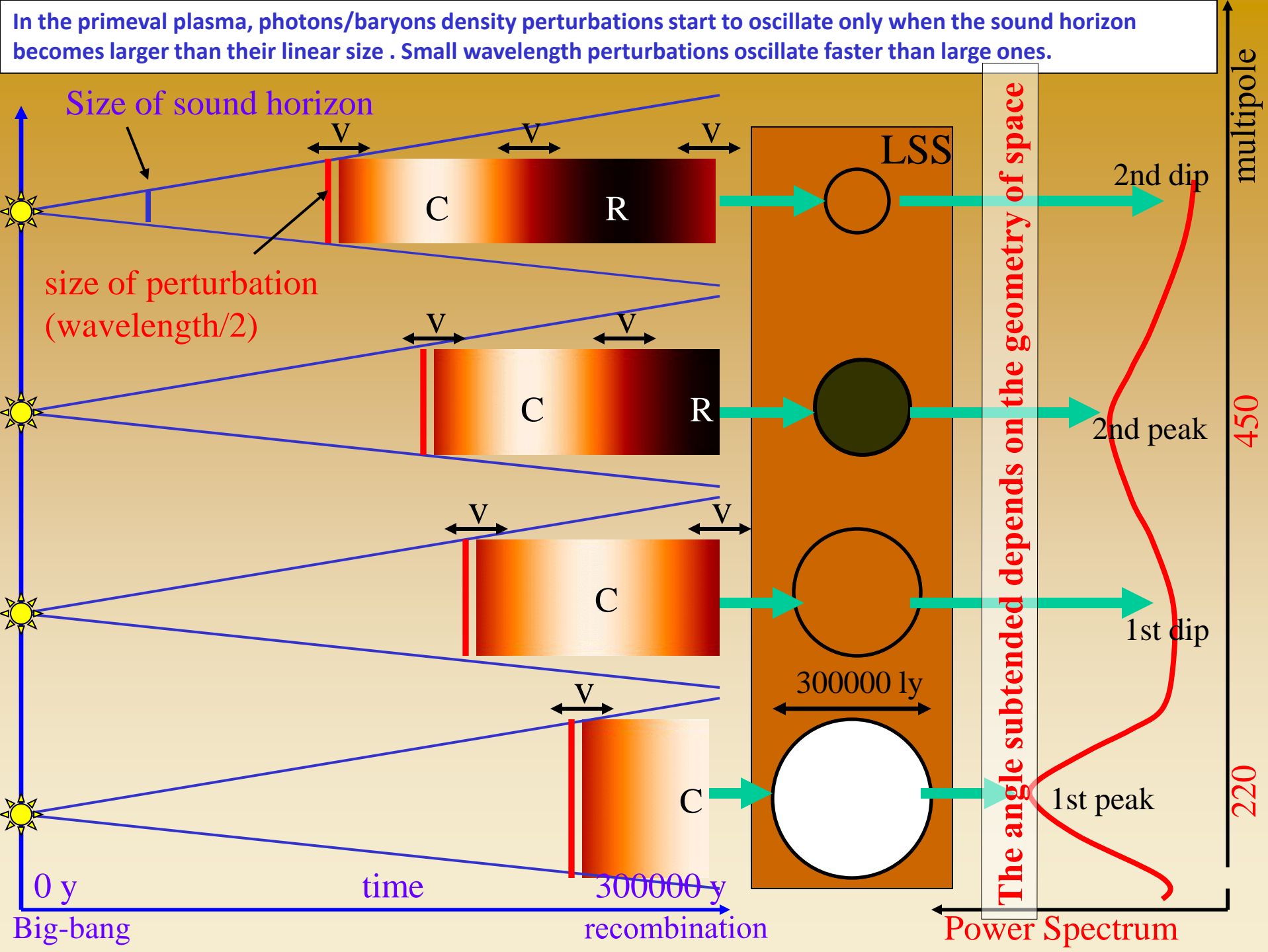
CMB anisotropy (intrinsic)

- The primeval plasma of photons and matter **oscillates** :
- self-gravity vs radiation pressure.
- We can measure the result of these oscillations as a weak anisotropy pattern in the **image** of the CMB.
- Statistical theory: all information encoded in the **angular power spectrum** of the image.

Density perturbations ($\Delta\rho/\rho$) were **oscillating** in the primeval plasma (as a result of the opposite effects of gravity and photon pressure).



After recombination, **density perturbation** can **grow** and create the hierarchy of structures we see in the nearby Universe.



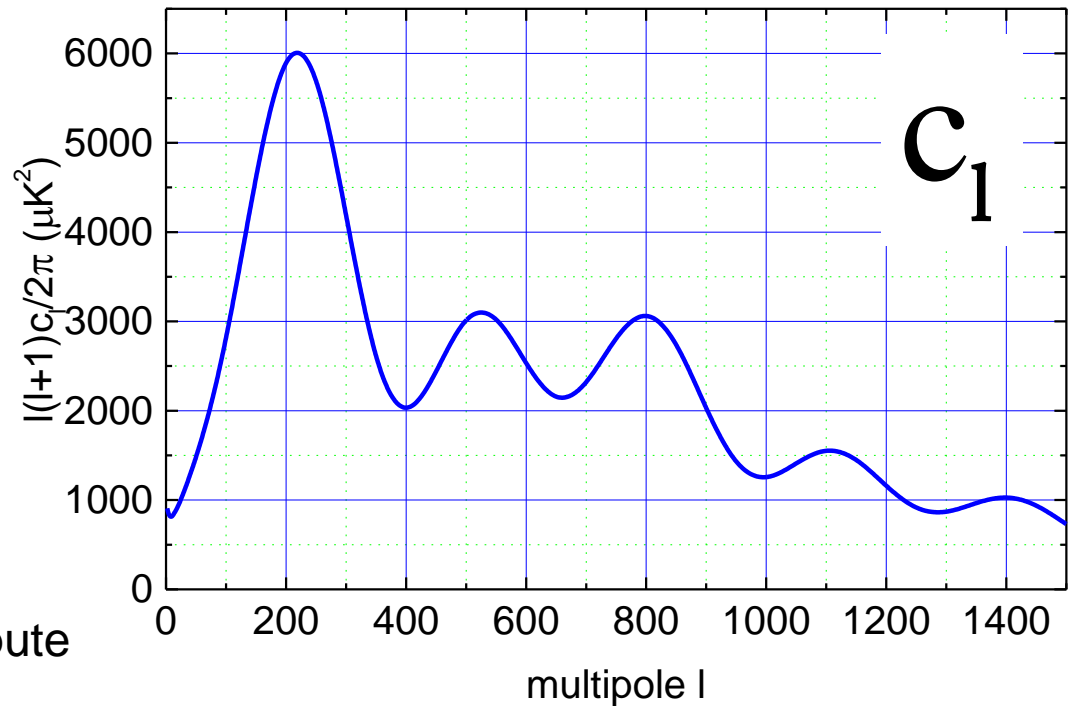
Expected power spectrum:

$$\Delta T(\theta, \varphi) = \sum_{\ell, m} a_{\ell m} Y_{\ell}^m(\theta, \varphi)$$

$$c_{\ell} = \langle a_{\ell m}^2 \rangle$$

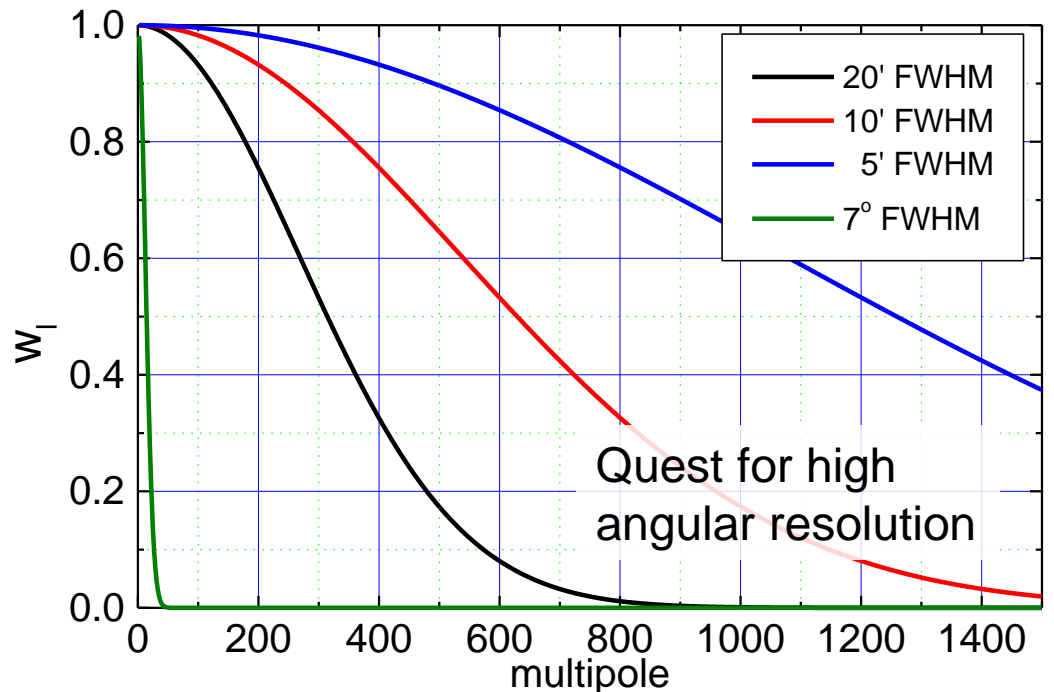
$$\langle \Delta T^2 \rangle = \frac{1}{4\pi} \sum_{\ell} (2\ell + 1) c_{\ell}$$

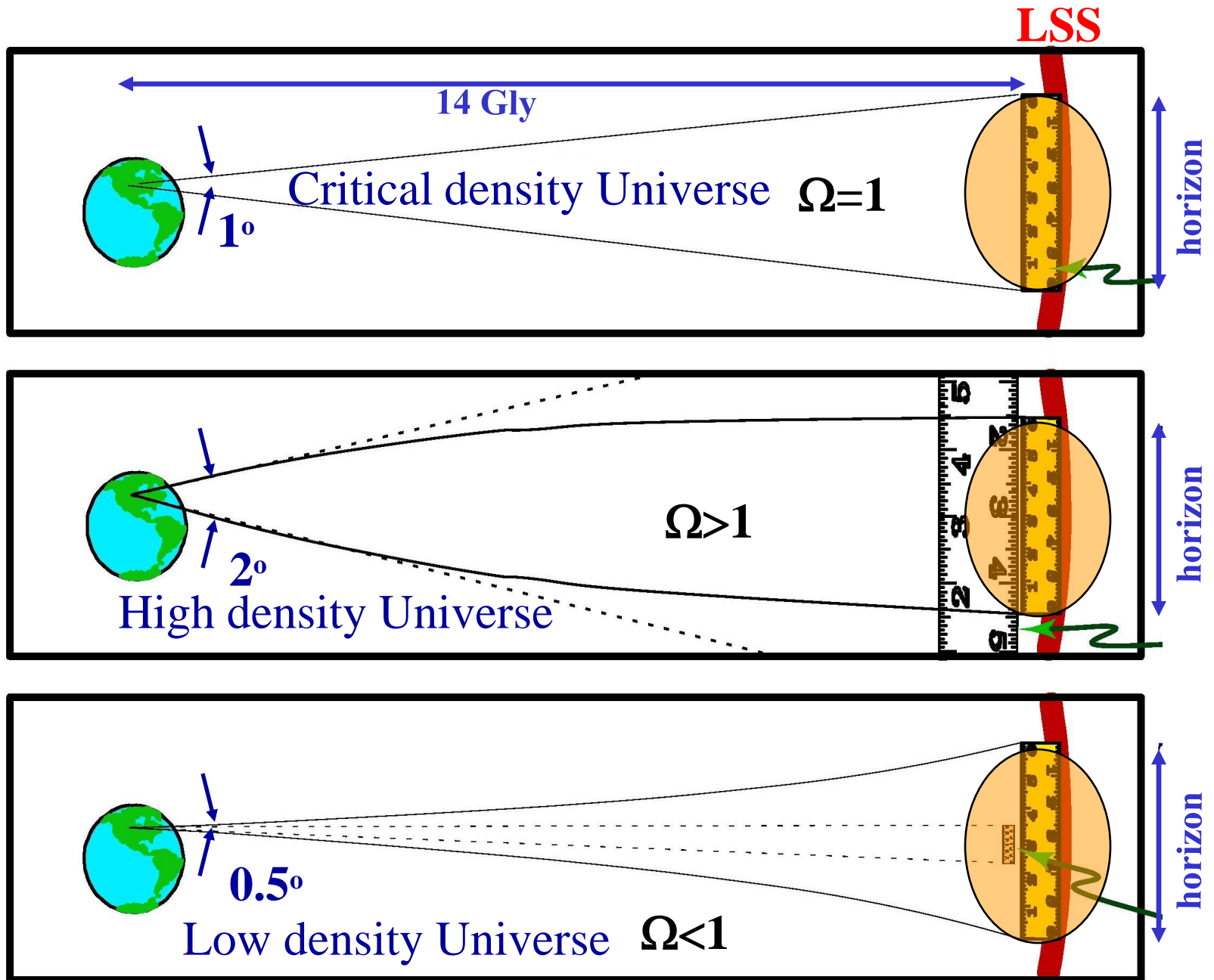
See e.g. <http://camb.info> to compute c_{ℓ} for a given cosmological model



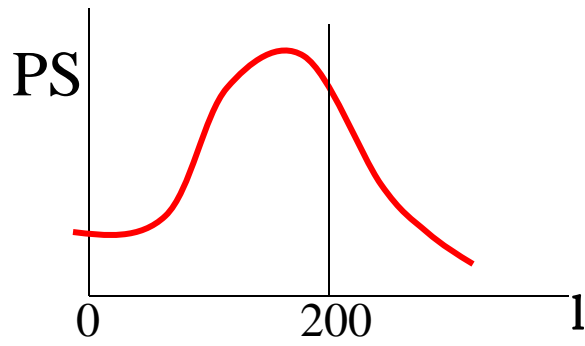
An instrument with finite angular resolution is not sensitive to the smallest scales (highest multipoles). For a gaussian beam with s.d. σ :

$$w_{\ell}^{LP} = e^{-l(l+1)\sigma^2}$$

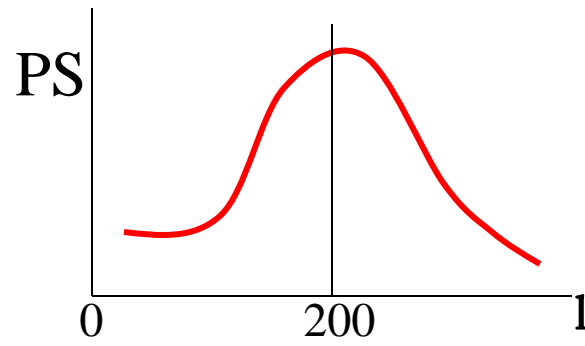




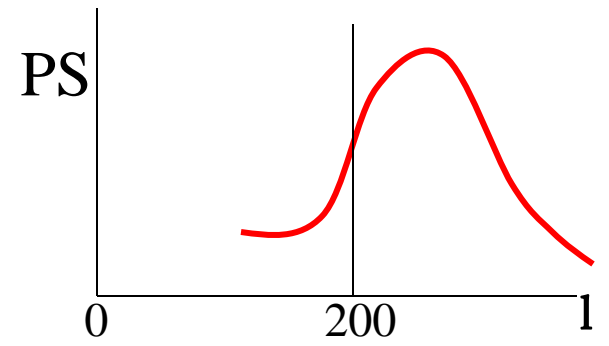
The image and PS are modified by the geometry of the universe



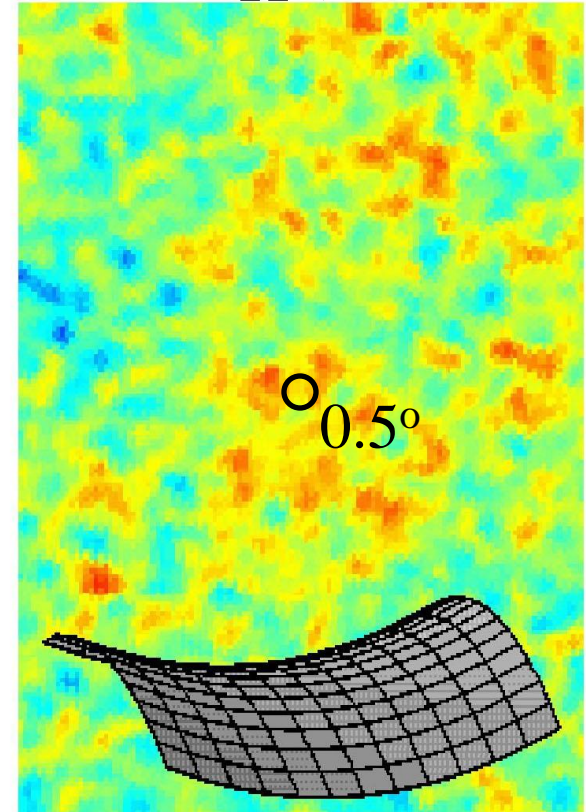
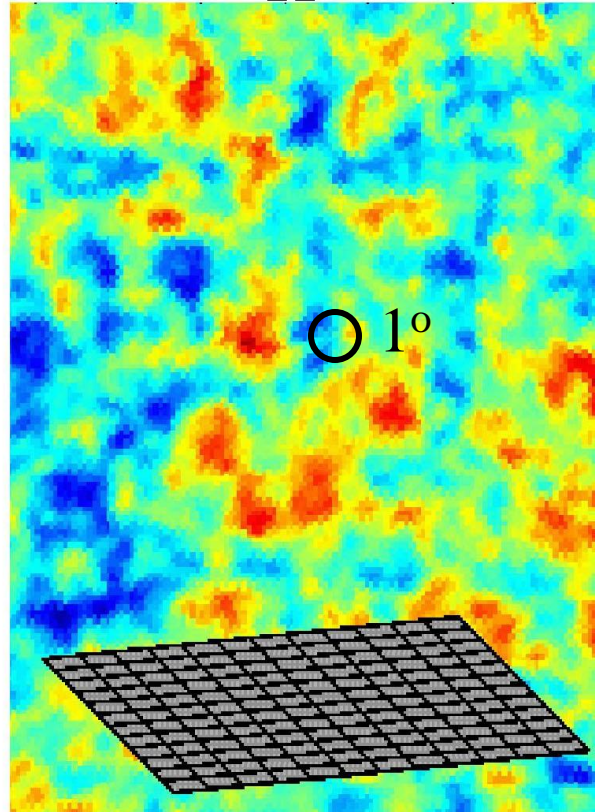
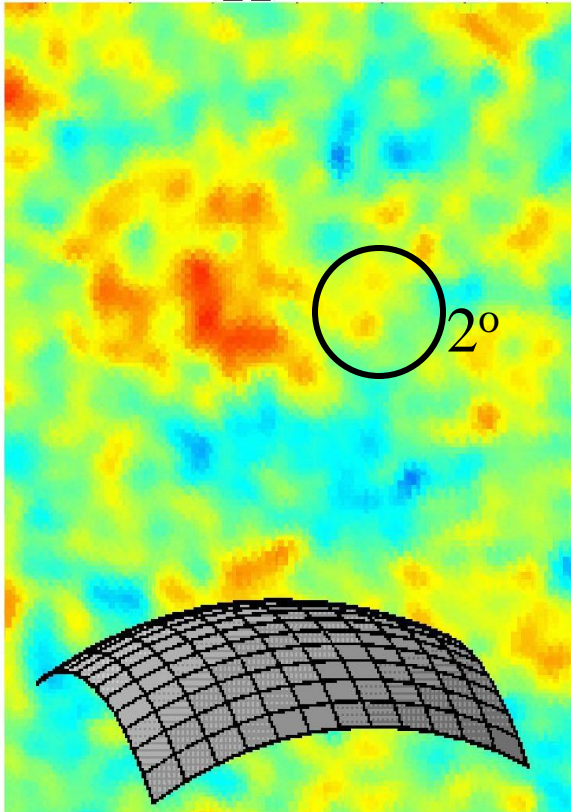
High density Universe
 $\Omega > 1$



Critical density Universe
 $\Omega = 1$



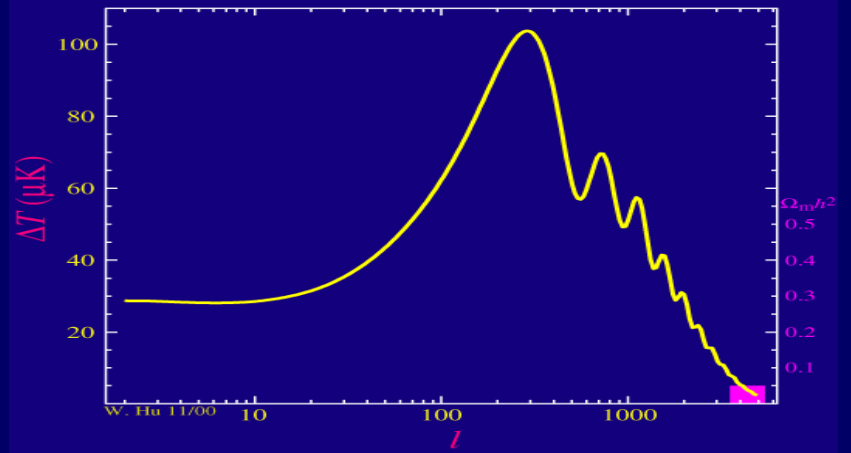
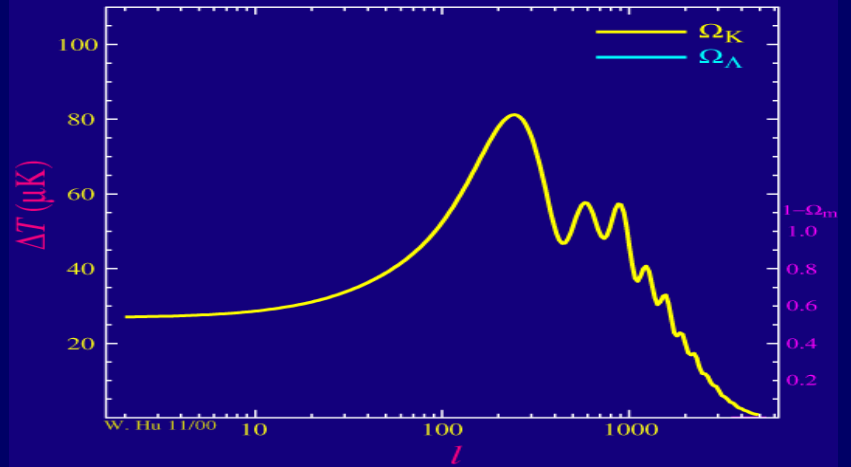
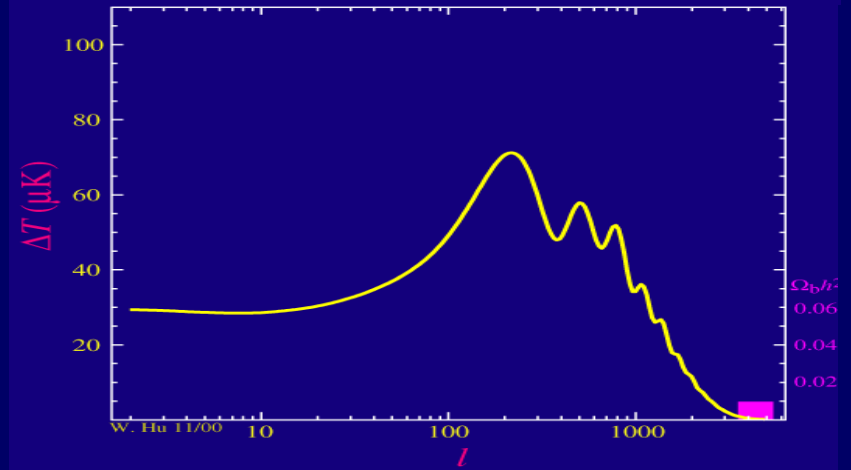
Low density Universe
 $\Omega < 1$



The mass-energy density of the Universe can be measured in this way.

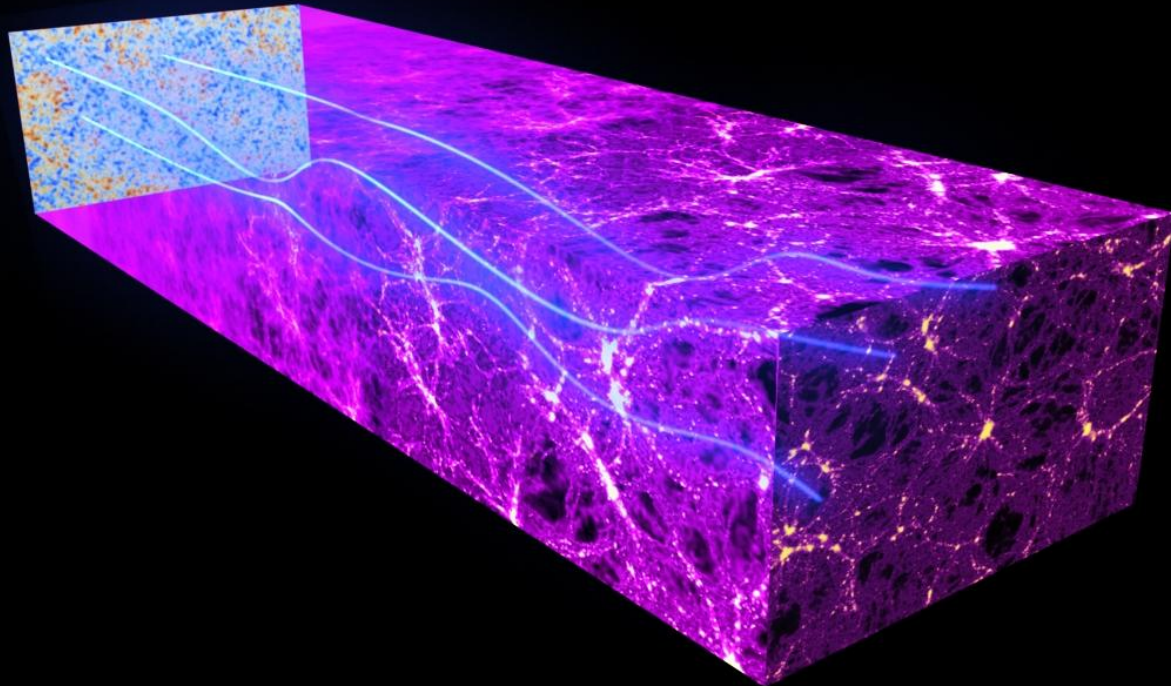
Composition

- The composition of the universe (baryons, dark matter, dark energy) affects the shape of the power spectrum.
- Accurate measurements of the power spectrum allow to constrain the energy densities of the different components of the universe.



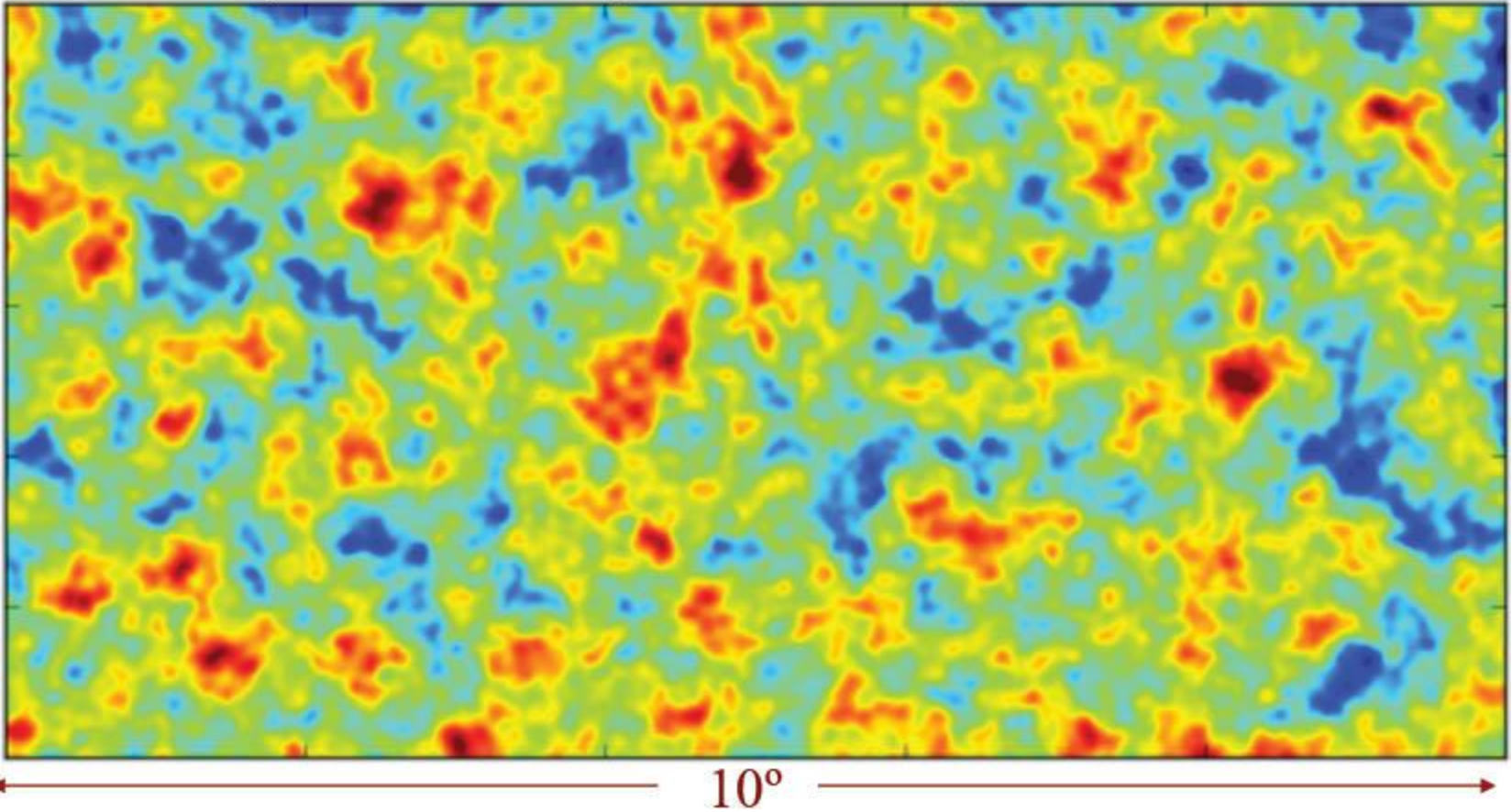
CMB anisotropy (lensing)

- Photons travelling in the universe for 13.7 Gly interact with massive structures, and are deflected (gravitational lensing)
- The result is a modified image of CMB anisotropy, which can be analyzed to study the distribution of mass (mainly dark matter) all the way to recombination.



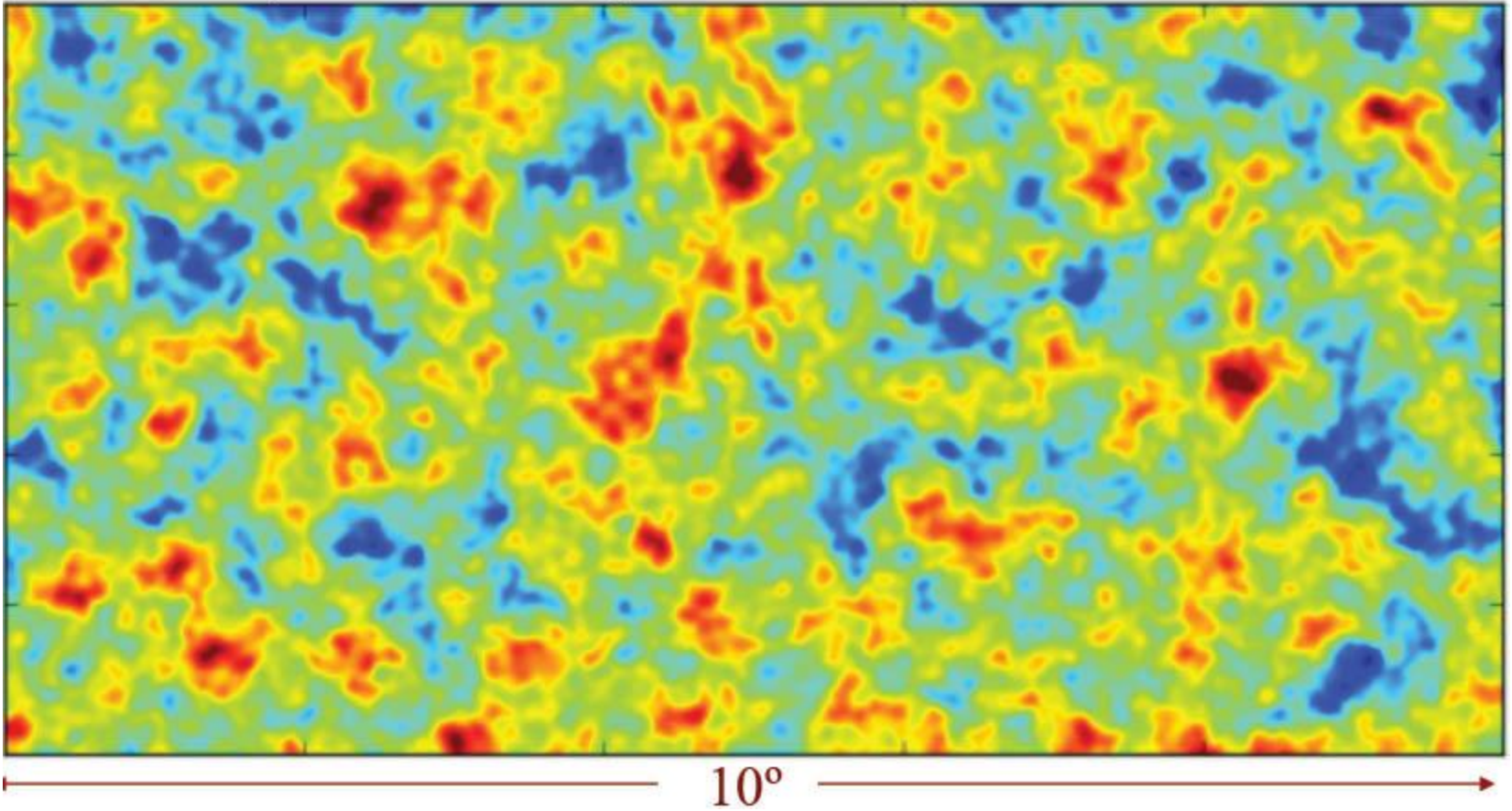
Typical deflection: 2.5'

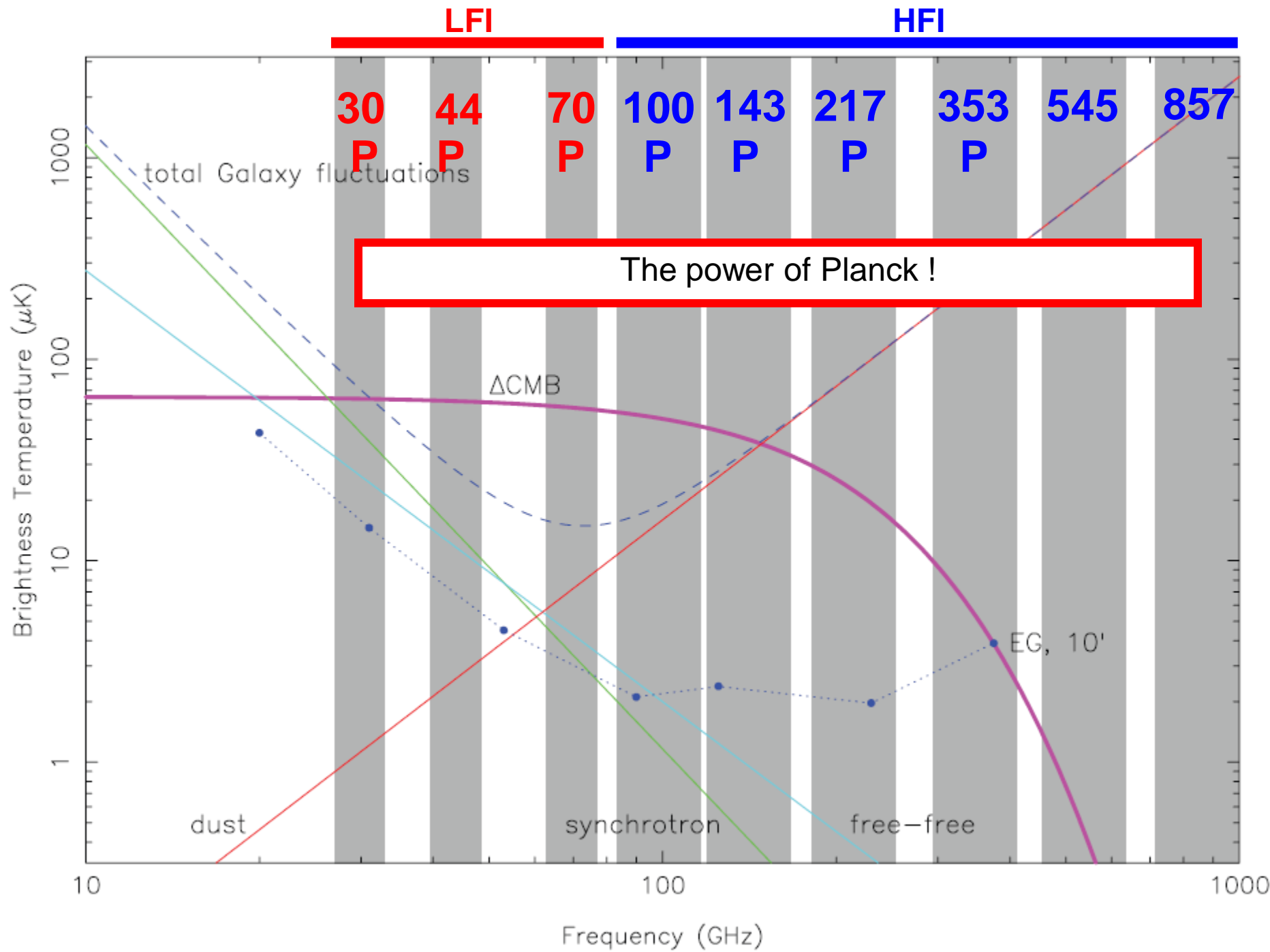
intrinsic CMB anisotropy

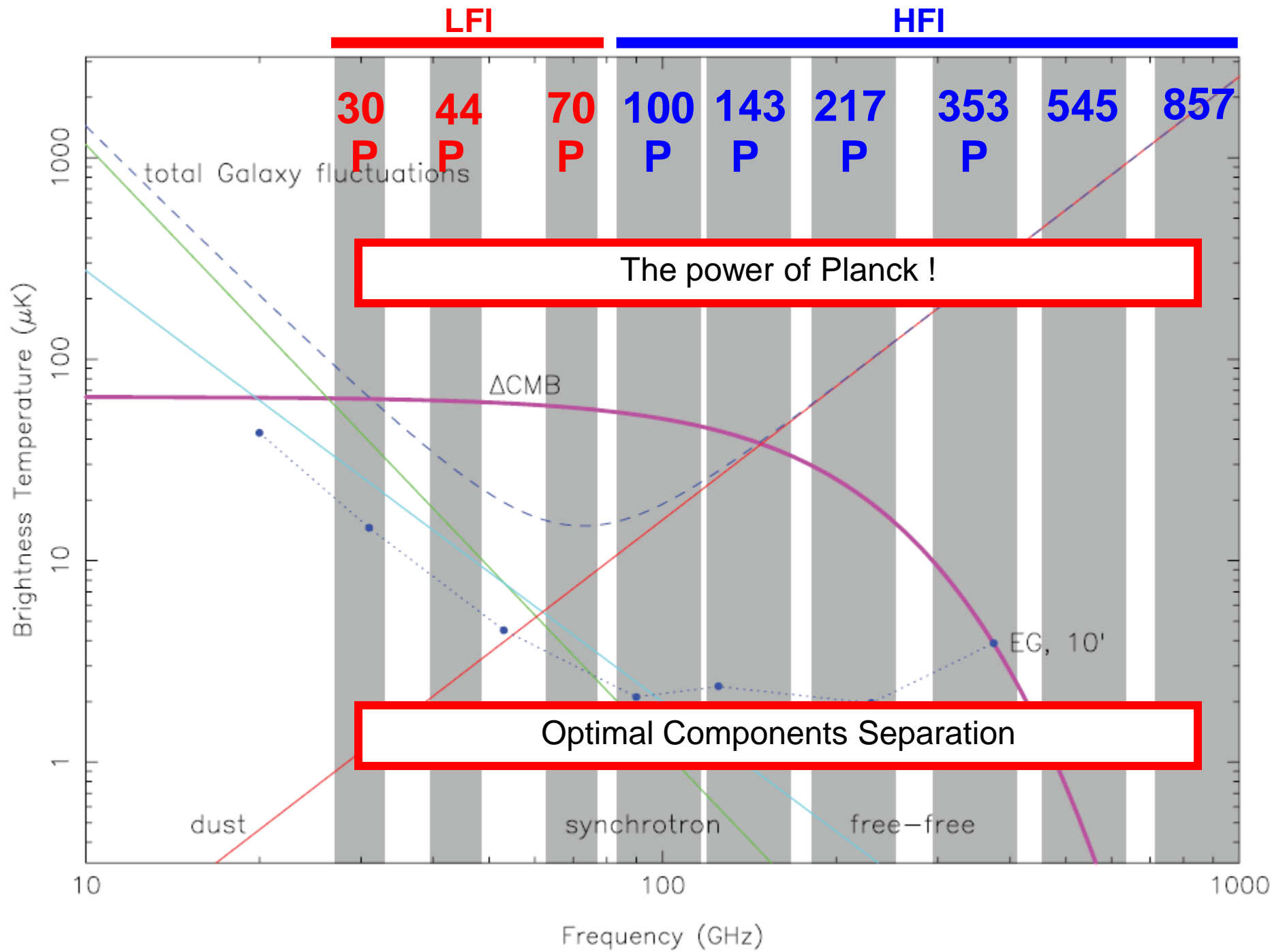


Typical deflection: 2.5'

lensed CMB anisotropy



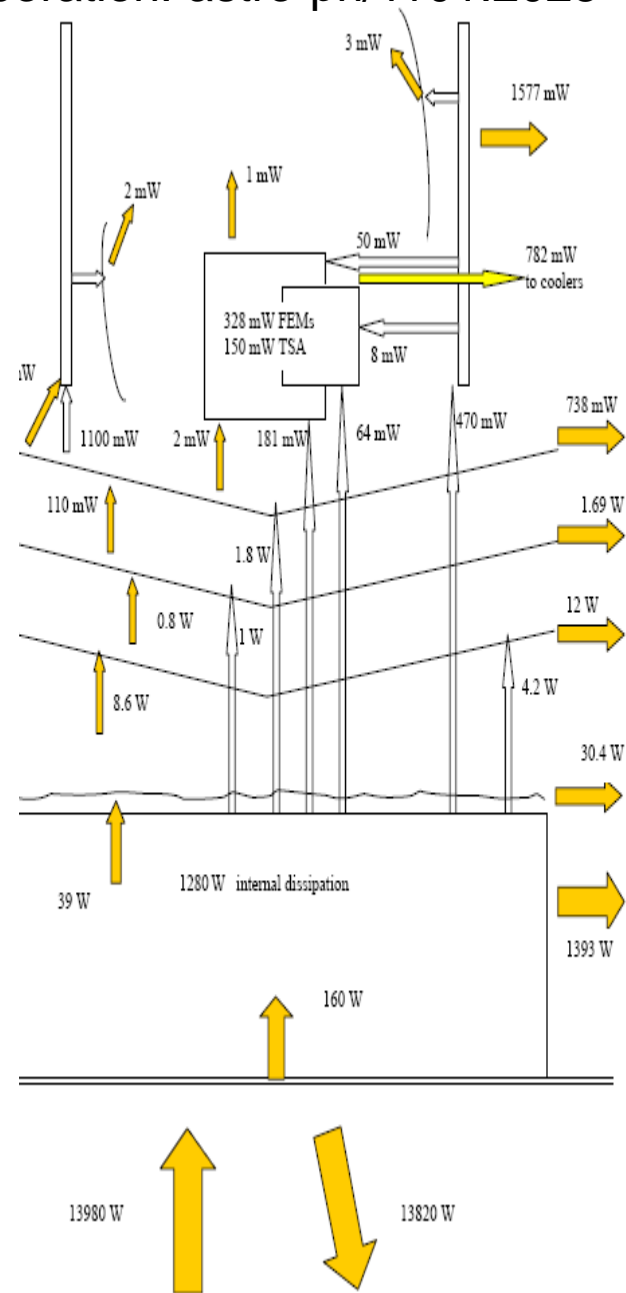
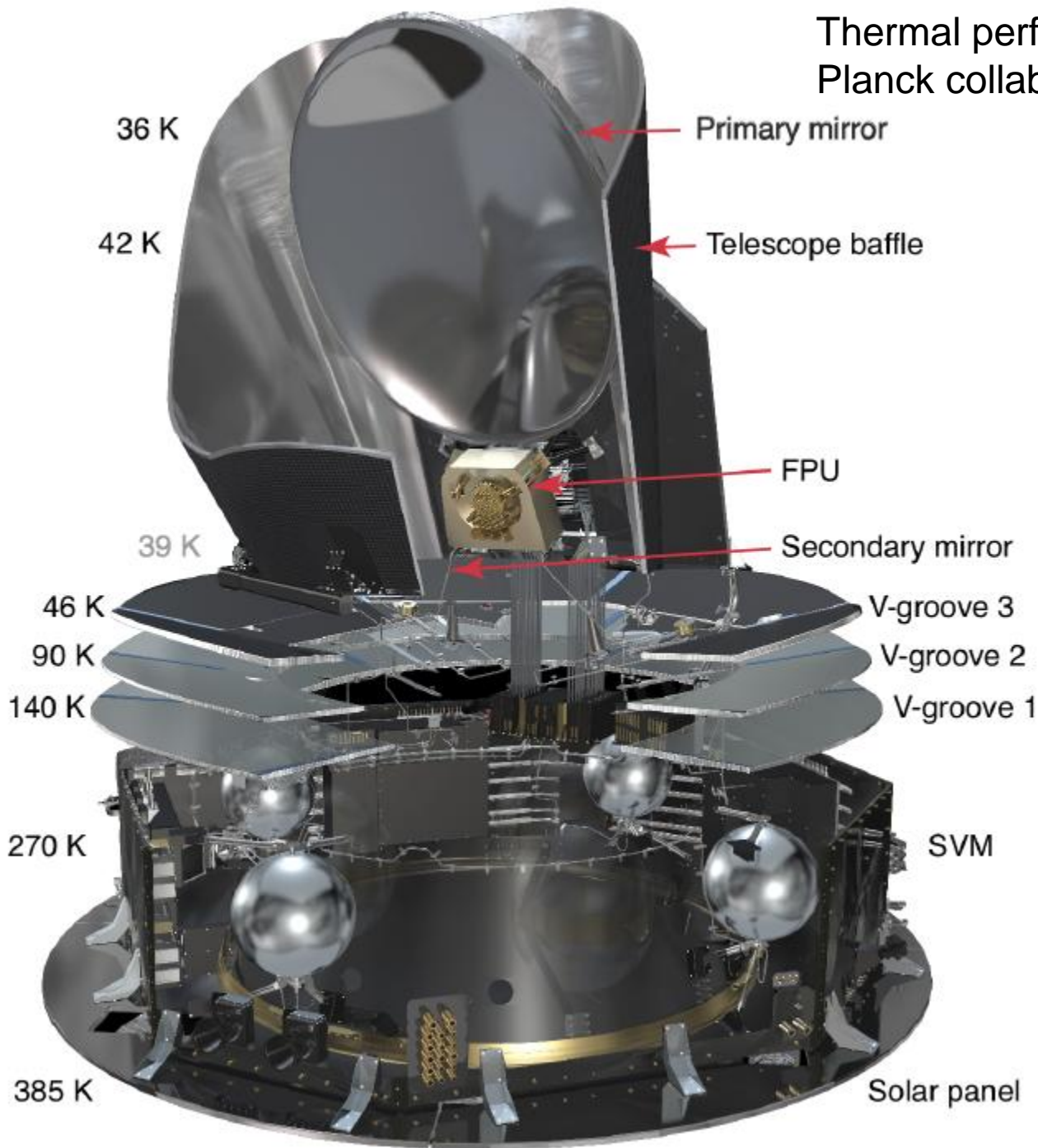




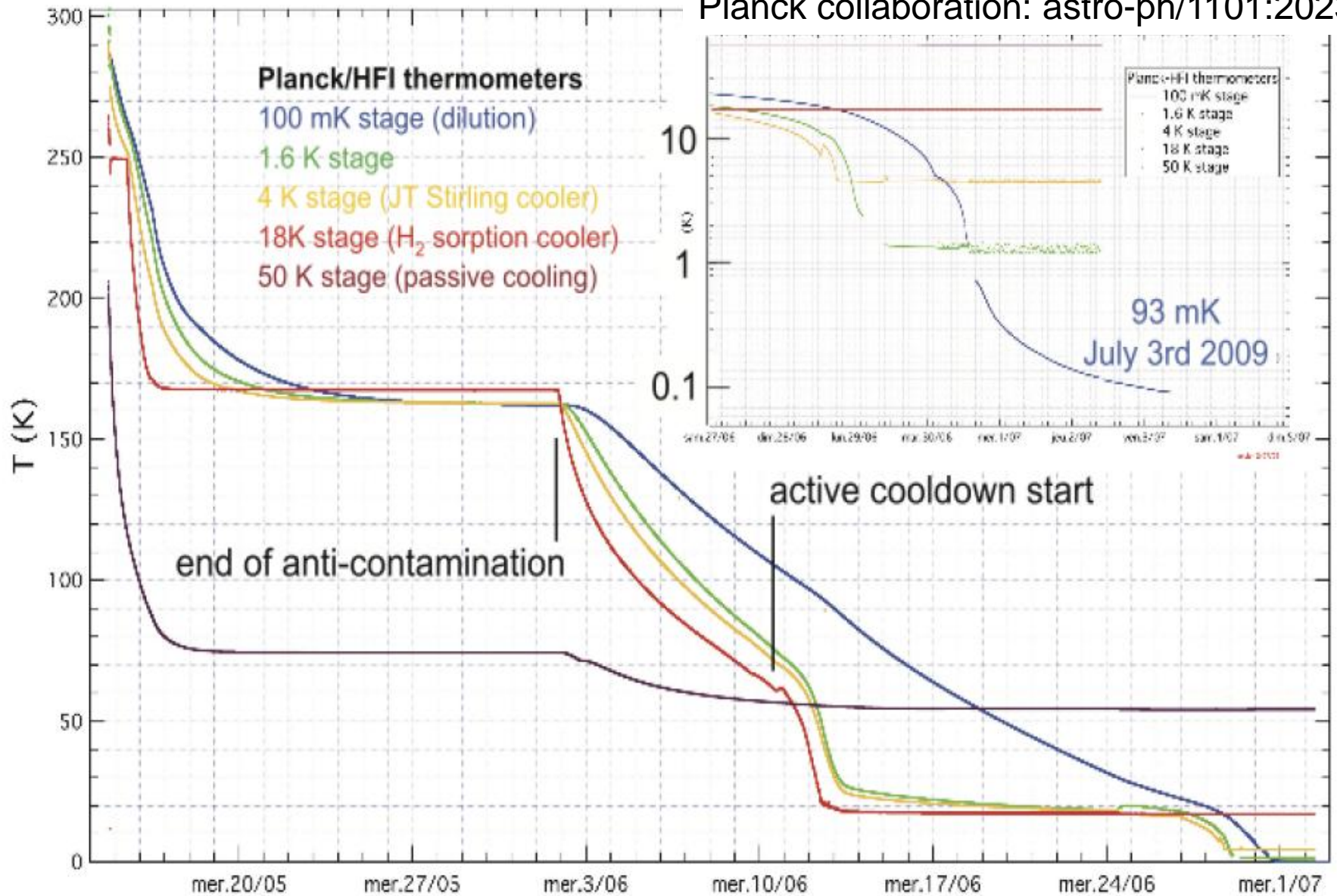


14 / May / 2009

Thermal performance :
 Planck collaboration: astro-ph/1101:2023



Thermal performance :
Planck collaboration: astro-ph/1101:2023



Mission :

Planck collaboration: astro-ph/1101:2022

Table 1. *Planck* coverage statistics.

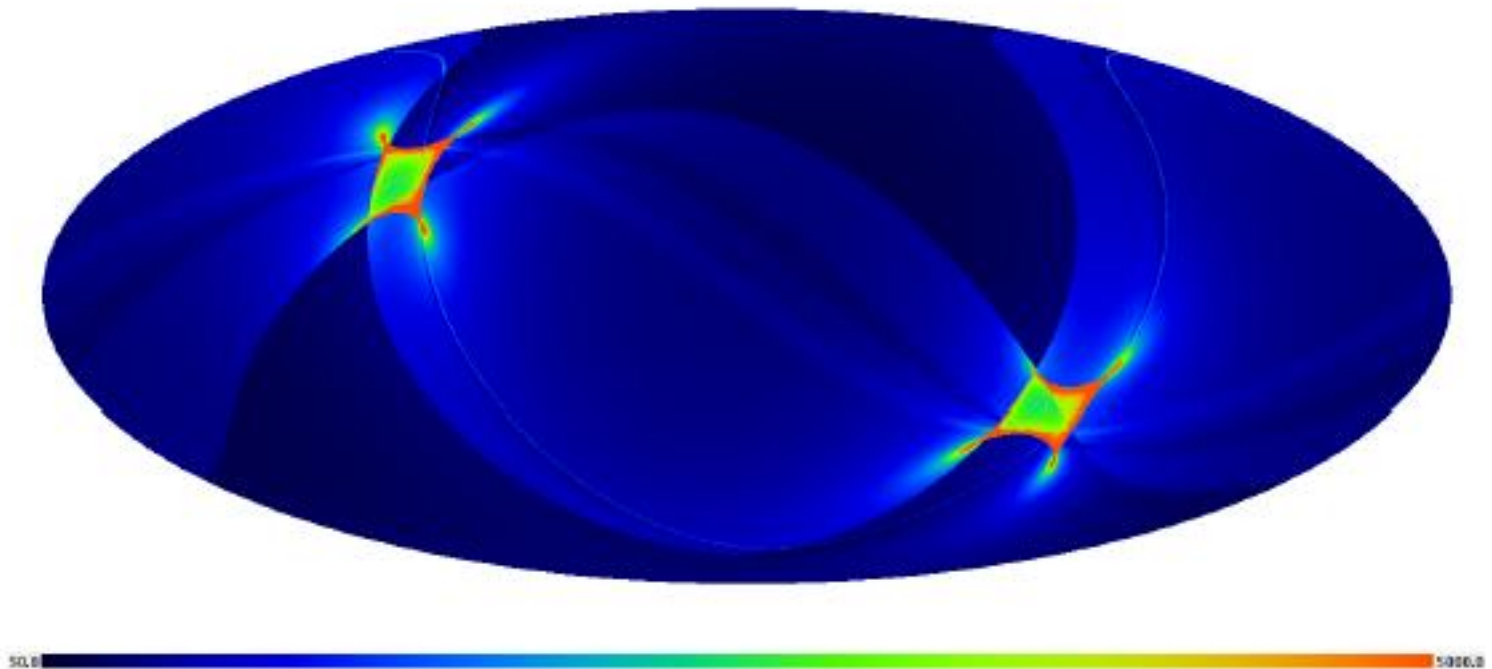
	30 GHz	100 GHz	545 GHz	
Mean ^a	2293	4575	2278	sec deg ²
Minimum	440	801	375	sec deg ²
< half Mean ^b	14.4	14.6	15.2	%
> 4× Mean ^c	1.6	1.5	1.2	%
> 9× Mean ^d	0.41	0.42	0.41	%

^a Mean over the whole sky of the integration time cumulated for all detectors (definition as in Table 3) in a given frequency channel.

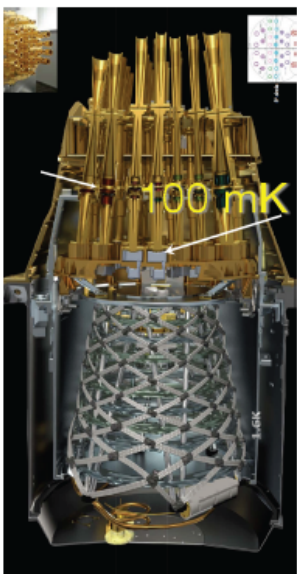
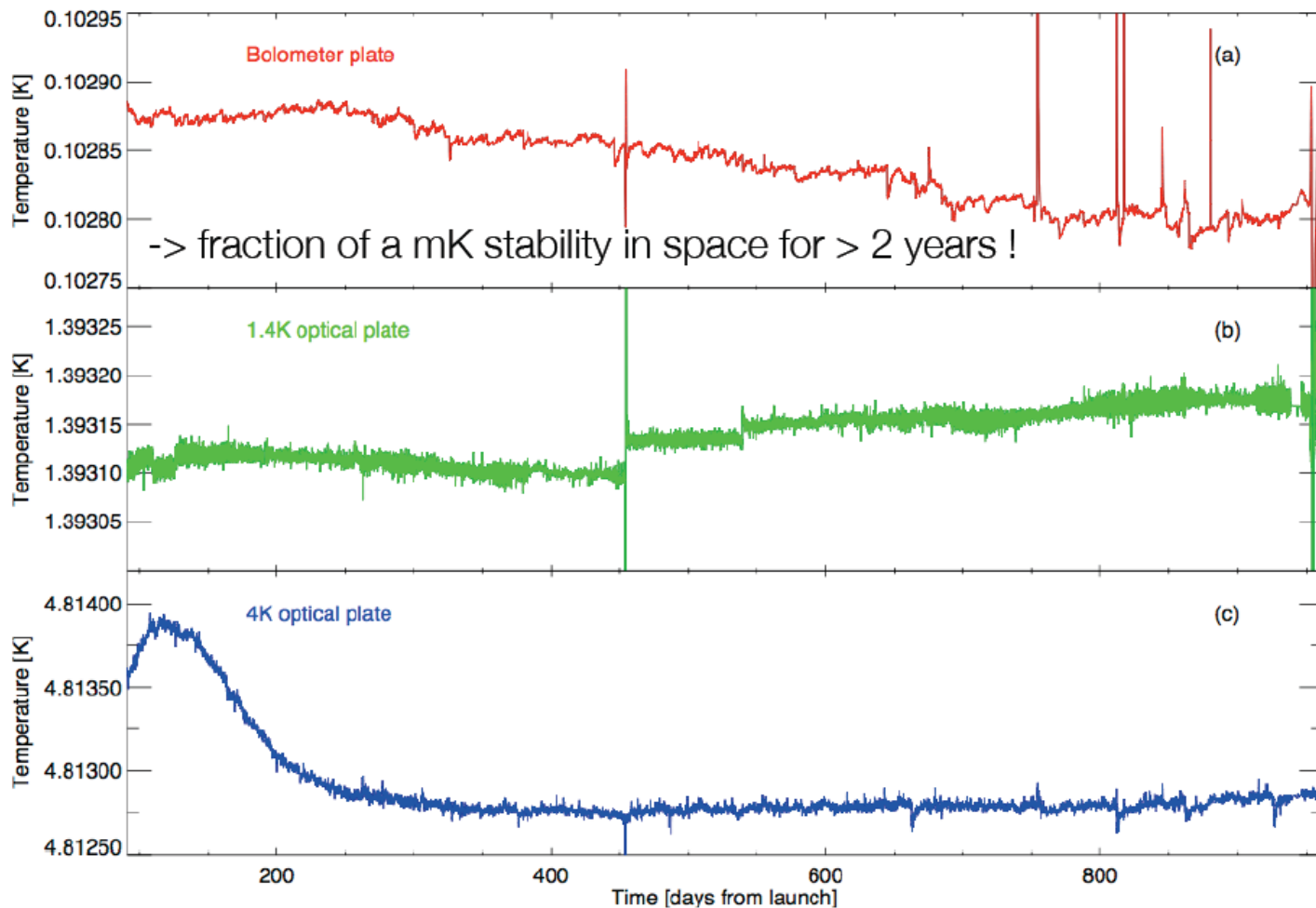
^b Fraction of the sky whose coverage is less than half the Mean.

^c Fraction of the sky whose coverage is larger than four times the Mean.

^d Fraction of the sky whose coverage is larger than nine times the Mean.



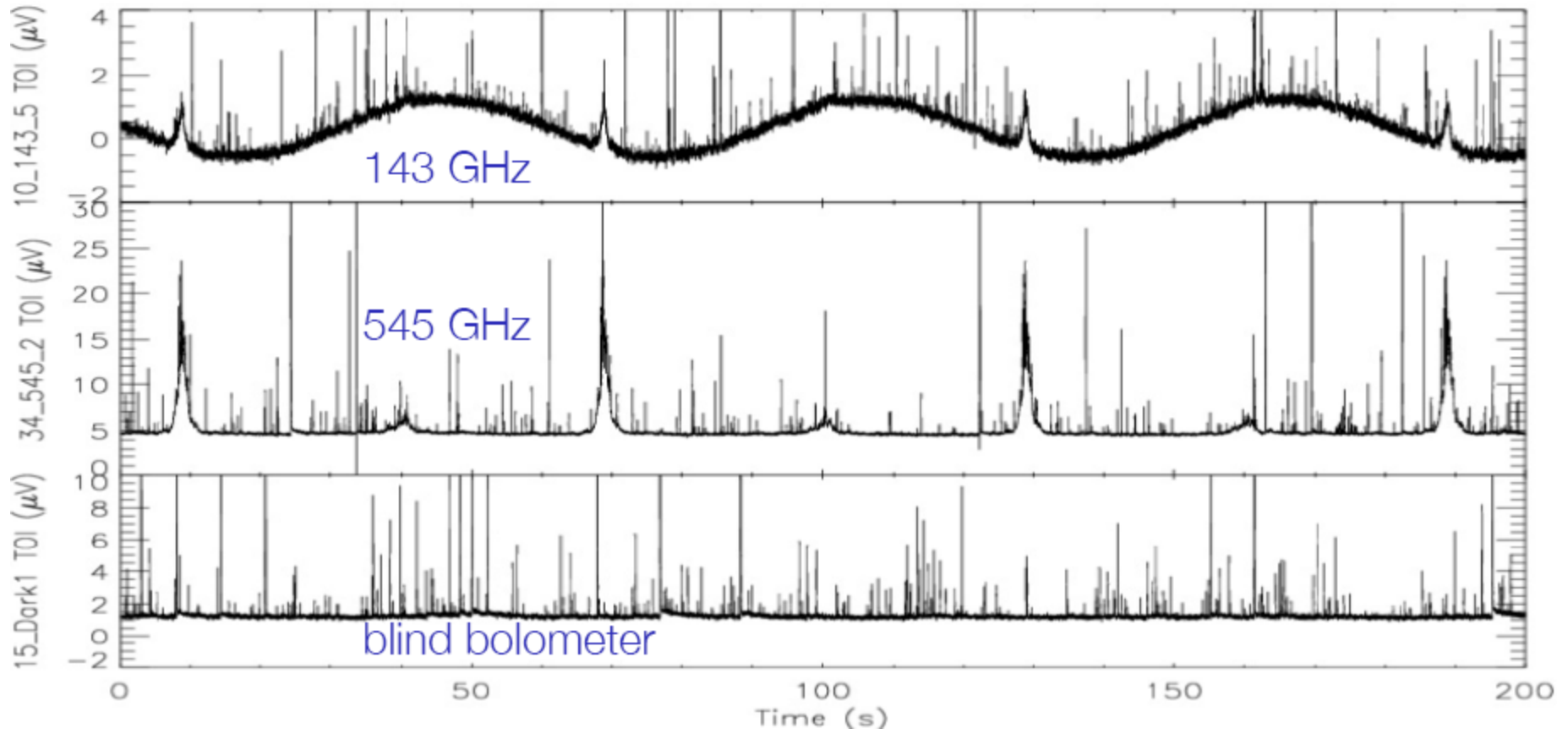
A very stable environment



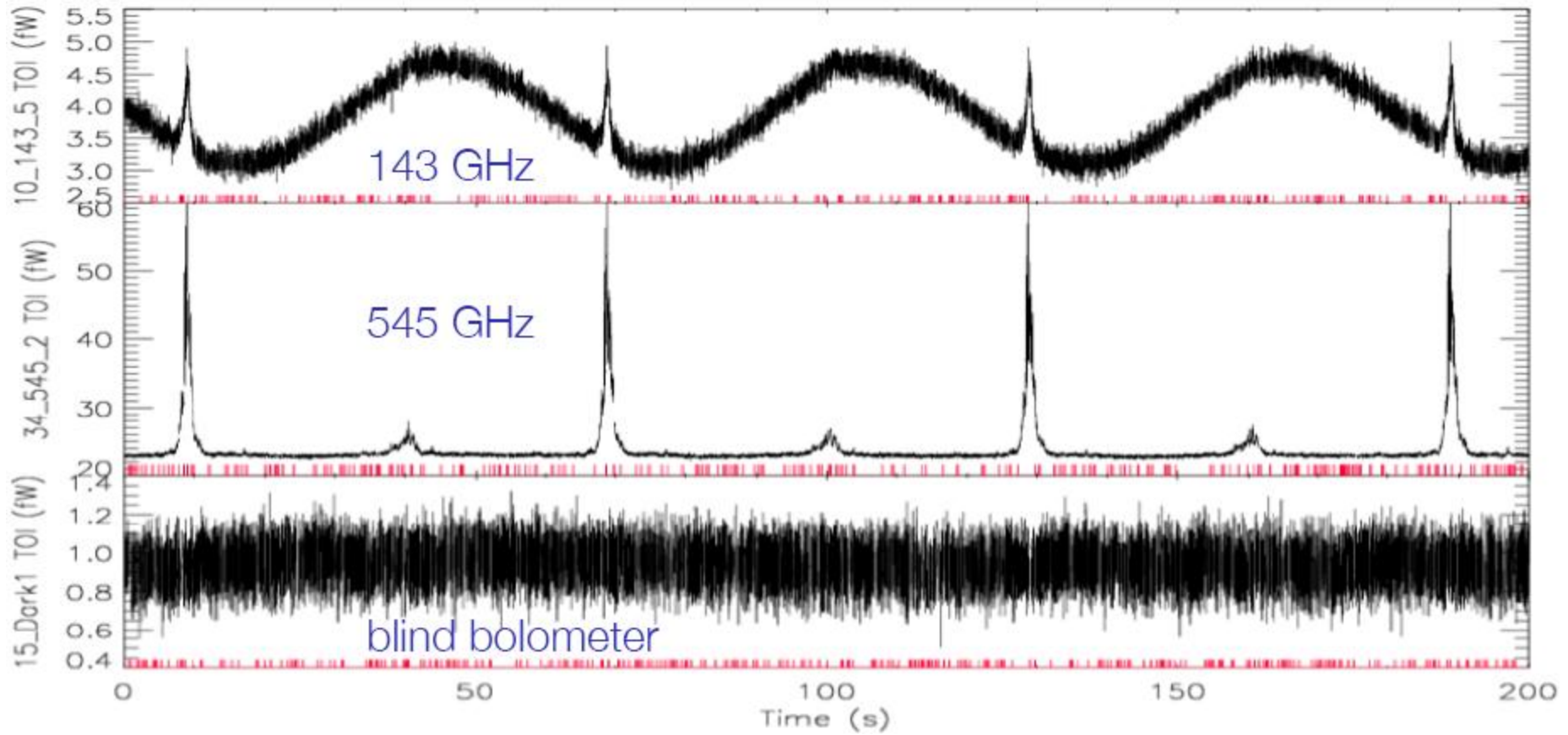
Cryostat:
dilution He3/He4

Fig. 7. The impressive stability of the HFI thermal stages during operations. Shown is the temperature evolution of the bolometer stage (*top*), the 1.6 K optical filter stage (*middle*) and the 4-K cooler reference load stage (*bottom*). The horizontal axis displays days since the beginning of the nominal mission.

Raw HFI data

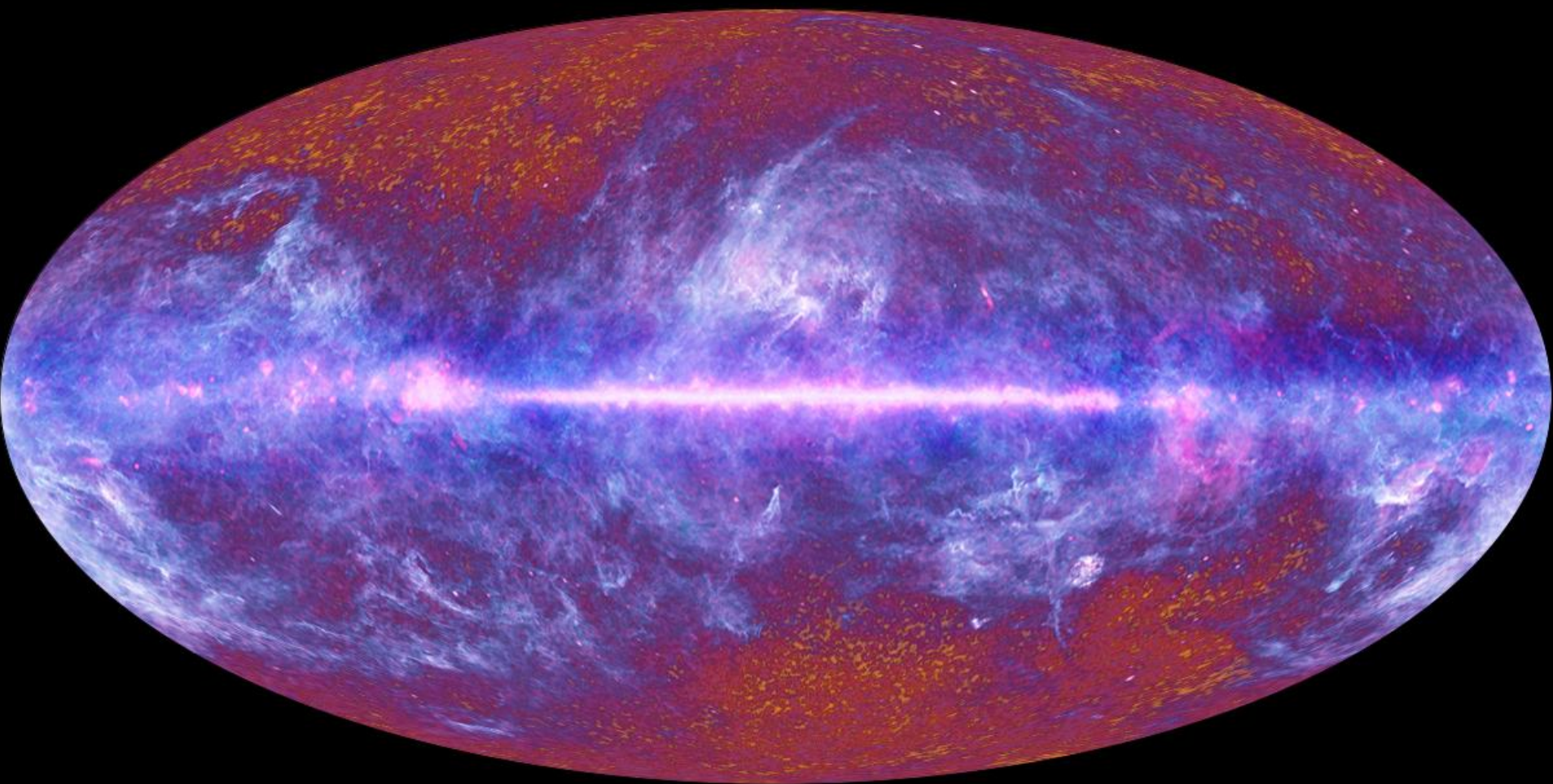


De-spiked HFI data



<20% of data flagged

2011 data release



Planck one-year all-sky survey



(c) ESA, HFI and LFI consortia, J

The 2013 Planck results

- Planck 2013 results. I. Overview of products and results
- Planck 2013 results. II. Low Frequency Instrument data processing
- Planck 2013 results. III. LFI systematic uncertainties
- Planck 2013 results. IV. LFI beams
- Planck 2013 results. V. LFI calibration
- Planck 2013 results. VI. High Frequency Instrument data processing
- Planck 2013 results. VII. HFI time response and beams
- Planck 2013 results. VIII. HFI calibration and mapmaking
- Planck 2013 results. IX. HFI spectral response
- Planck 2013 results. X. HFI energetic particle effects
- Planck 2013 results. XI. Consistency of the data
- Planck 2013 results. XII. Component separation
- Planck 2013 results. XIII. Galactic CO emission
- Planck 2013 results. XIV. Zodiacal emission
- Planck 2013 results. XV. CMB power spectra and likelihood
- Planck 2013 results. XVI. Cosmological parameters
- Planck 2013 results. XVII. Gravitational lensing by large-scale structure
- Planck 2013 results. XVIII. The gravitational lensing-infrared background correlation
- Planck 2013 results. XIX. The integrated Sachs-Wolfe effect
- Planck 2013 results. XX. Cosmology from Sunyaev-Zeldovich cluster counts
- Planck 2013 results. XXI. All-sky Compton-parameter map and characterization
- Planck 2013 results. XXII. Constraints on inflation
- Planck 2013 results. XXIII. Isotropy and statistics of the CMB
- Planck 2013 results. XXIV. Constraints on primordial non-Gaussianity
- Planck 2013 results. XXV. Searches for cosmic strings and other topological defects
- Planck 2013 results. XXVI. Background geometry and topology of the Universe
- Planck 2013 results. XXVII. Special relativistic effects on the CMB dipole
- Planck 2013 results. XXVIII. The Planck Catalogue of Compact Sources
- Planck 2013 results. XXIX. The Planck catalogue of Sunyaev-Zeldovich sources
- Planck 2013 results. Explanatory supplement

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- Planck 2013 results. I. Overview of products and results
- Planck 2013 results. II. Low Frequency Instrument data processing
- Planck 2013 results. III. LFI systematic uncertainties
- Planck 2013 results. IV. LFI beams
- Planck 2013 results. V. LFI calibration
- Planck 2013 results. VI. High Frequency Instrument data processing
- Planck 2013 results. VII. HFI time response and beams
- Planck 2013 results. VIII. HFI calibration and mapmaking
- Planck 2013 results. IX. HFI spectral response
- Planck 2013 results. X. HFI energetic particle effects
- Planck 2013 results. XI. Consistency of the data

- Planck 2013 results. XII. Component separation
- Planck 2013 results. XIII. Galactic dust emission
- Planck 2013 results. XIV. Zodiacal emission

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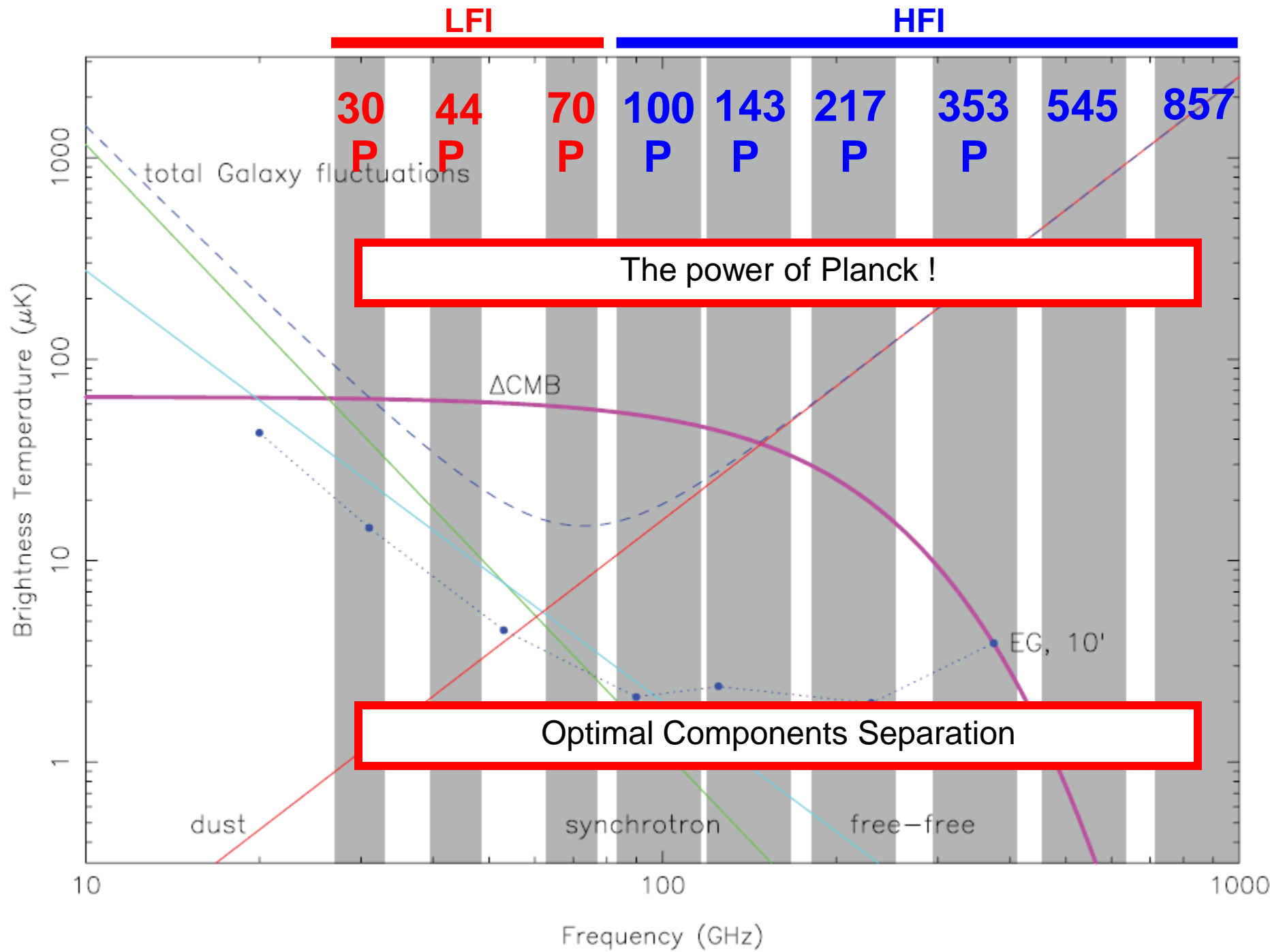
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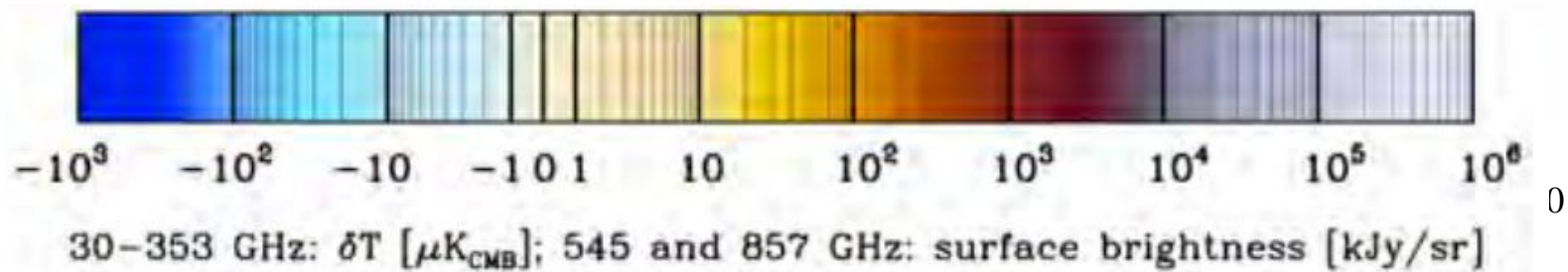
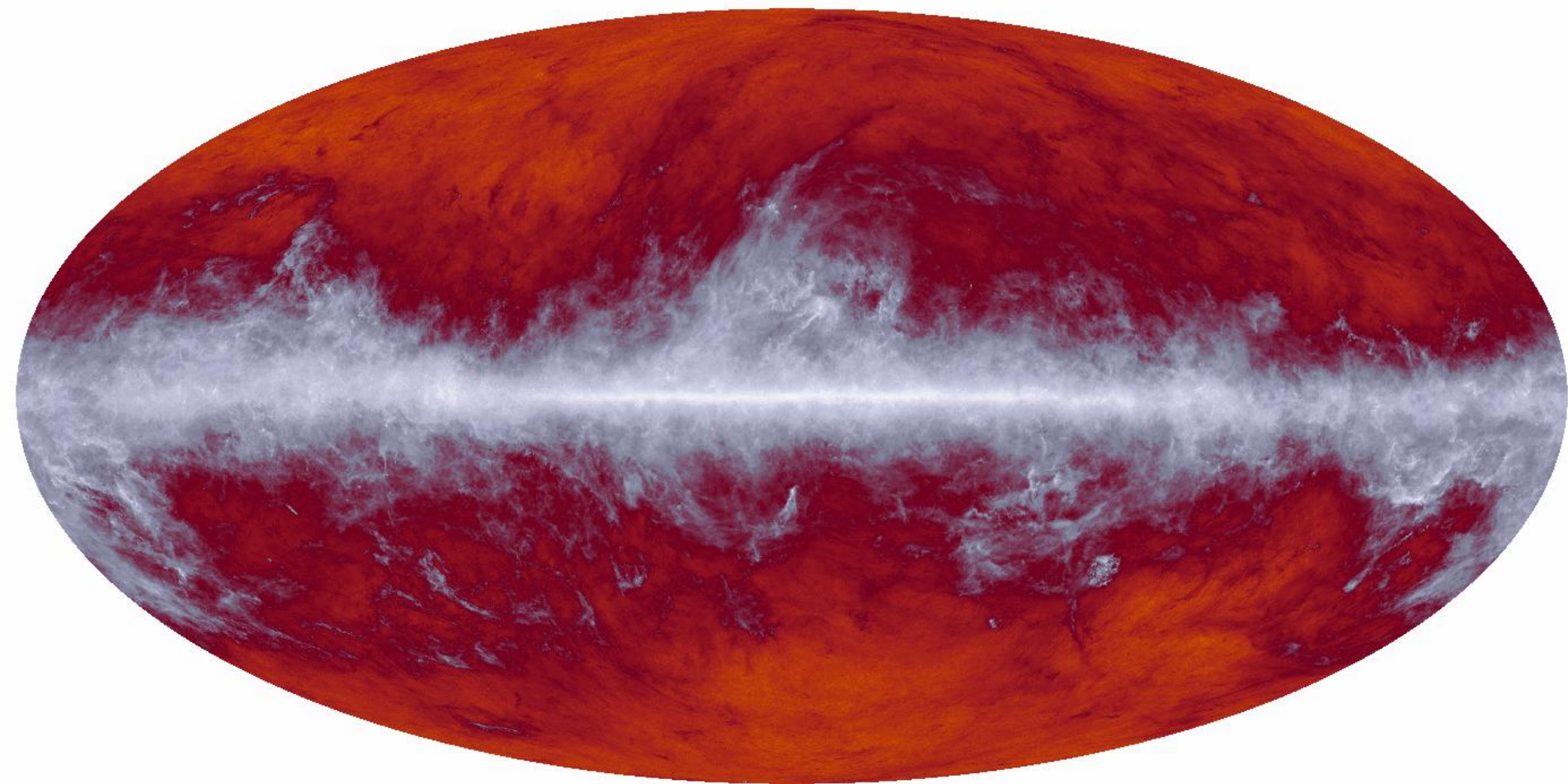
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Planck Legacy Maps

6×10^6 pixels (5')

857 GHz



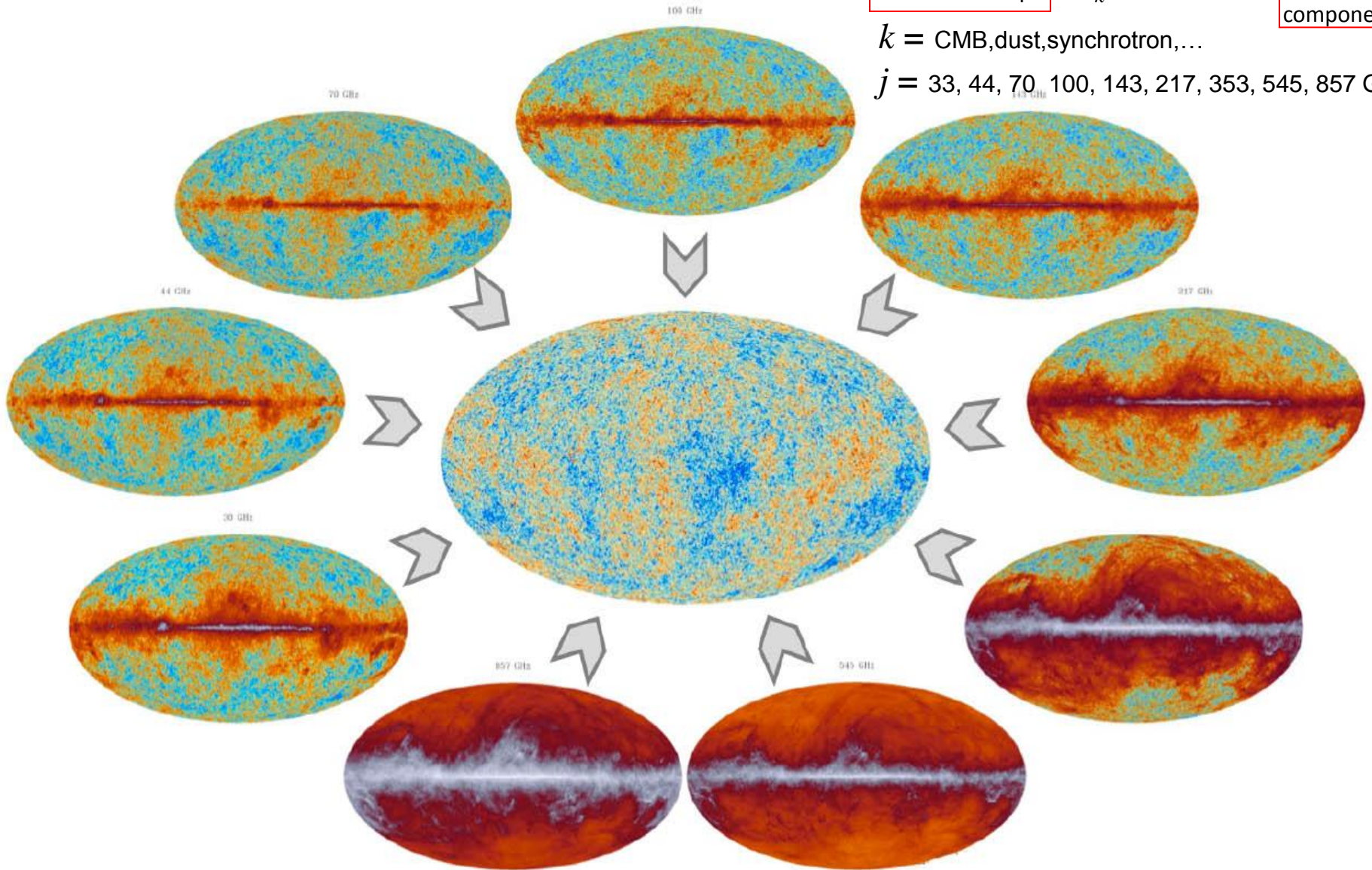
components separation

$$\Delta T(\nu_j, \ell, b) = \sum_k a_k(\nu_j, \ell, b) C_k(\ell, b)$$

Measured maps physical components

$k = \text{CMB, dust, synchrotron, ...}$

$j = 33, 44, 70, 100, 143, 217, 353, 545, 857 \text{ GHz}$



The CMB component

